

# PC5 Reaktionsdynamik

Kapitel VII  
Experimentelle Methoden

**Atomic-Scale Dynamics**

**of the Chemical Bond**

**Femtochemistry**

# Das ideale Experiment....

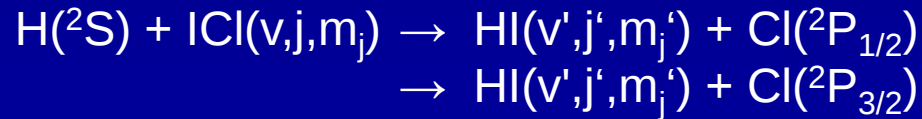
Das Idealexperiment müsste den Streuquerschnitt und die Winkelverteilung der Produkte für einen **vollständig spezifizierten Stossvorgang** bestimmen. In der Praxis versuchen wir dem möglichst nahezukommen, nicht zuletzt, um mit der Theorie vergleichen zu können. Das bedeutet in der Reihenfolge immer größeren Details die Messung folgender Größen: Integraler Reaktionsquerschnitt bei vorgegebener Stossenergie, Winkelverteilungen der Produkte, möglichst zusätzlich die Geschwindigkeitsverteilung bei jedem Winkel, aus der man wegen der Energieerhaltung ihre innere Energie rekonstruieren kann, **Zustandsanalyse der Produkte, Zustandsvorgabe der Reaktanden, Vorgabe der Orientierung der Reaktanden, Analyse der Orientierung der Produkte**. Experimente mit orientierten Molekülen würden wir auch noch die Spezifikation der Quantenzahlen  $m_j$  und  $m'_j$  verlangen, die die Orientierung der Reaktanden bzw. Produkte bezüglich einer gegebenen Richtung beschreiben. Im übrigen sind alle oben genannten Eigenschaften nicht unabhängig voneinander, so dass wir uns auch noch für die Korrelationen interessieren müssen!

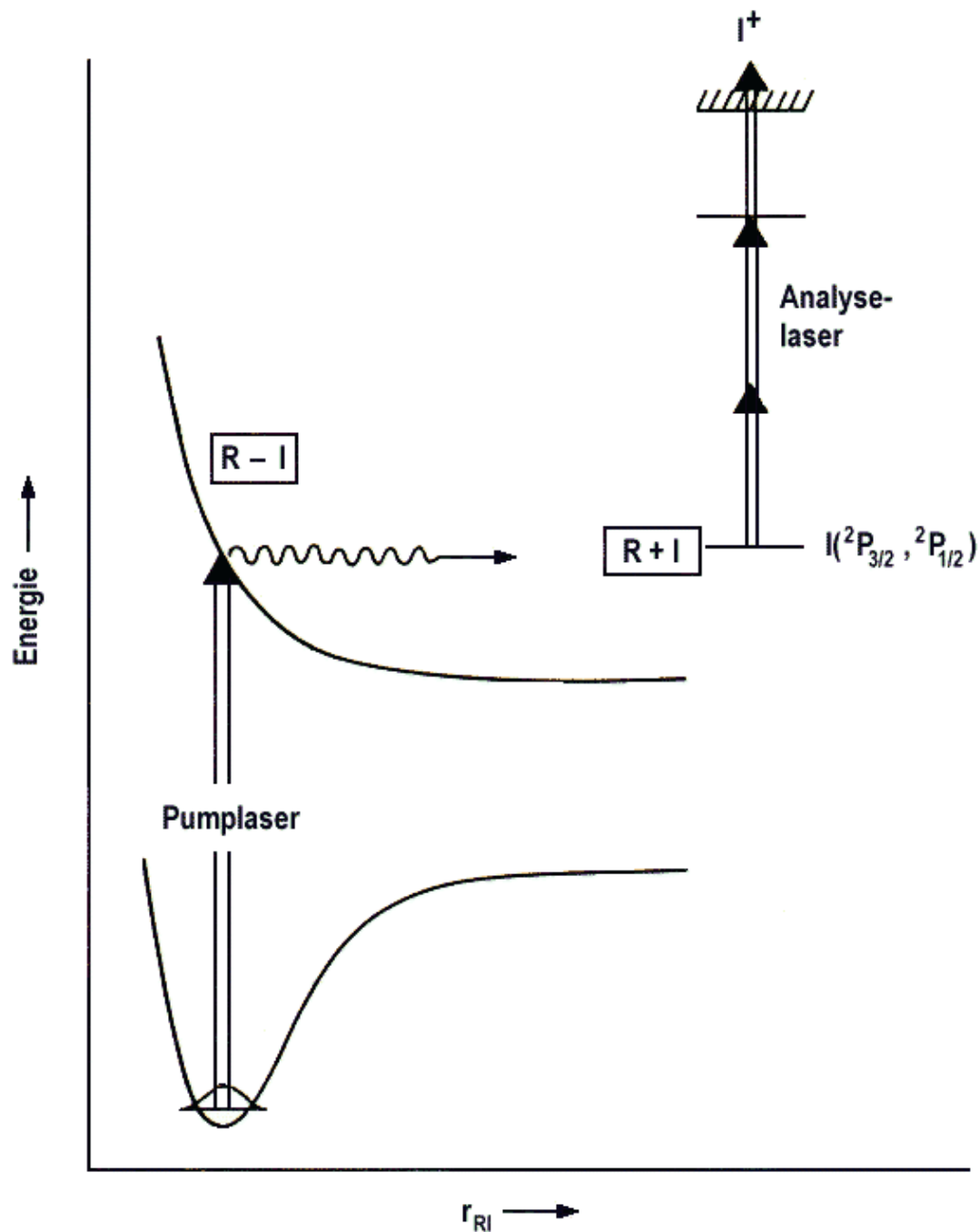
**...gibt es nicht**

## z.B. $\text{H} + \text{ICl}$

Eine vollständige Festlegung des Stoßvorgangs verlangt nicht nur die (chemische) Identifizierung des Produkts ( $\text{HCl}$  oder  $\text{HI}$ ), sondern auch die Feststellung des inneren Zustands von Edukten und Produkten, sowie deren Geschwindigkeiten (Vektoren!)

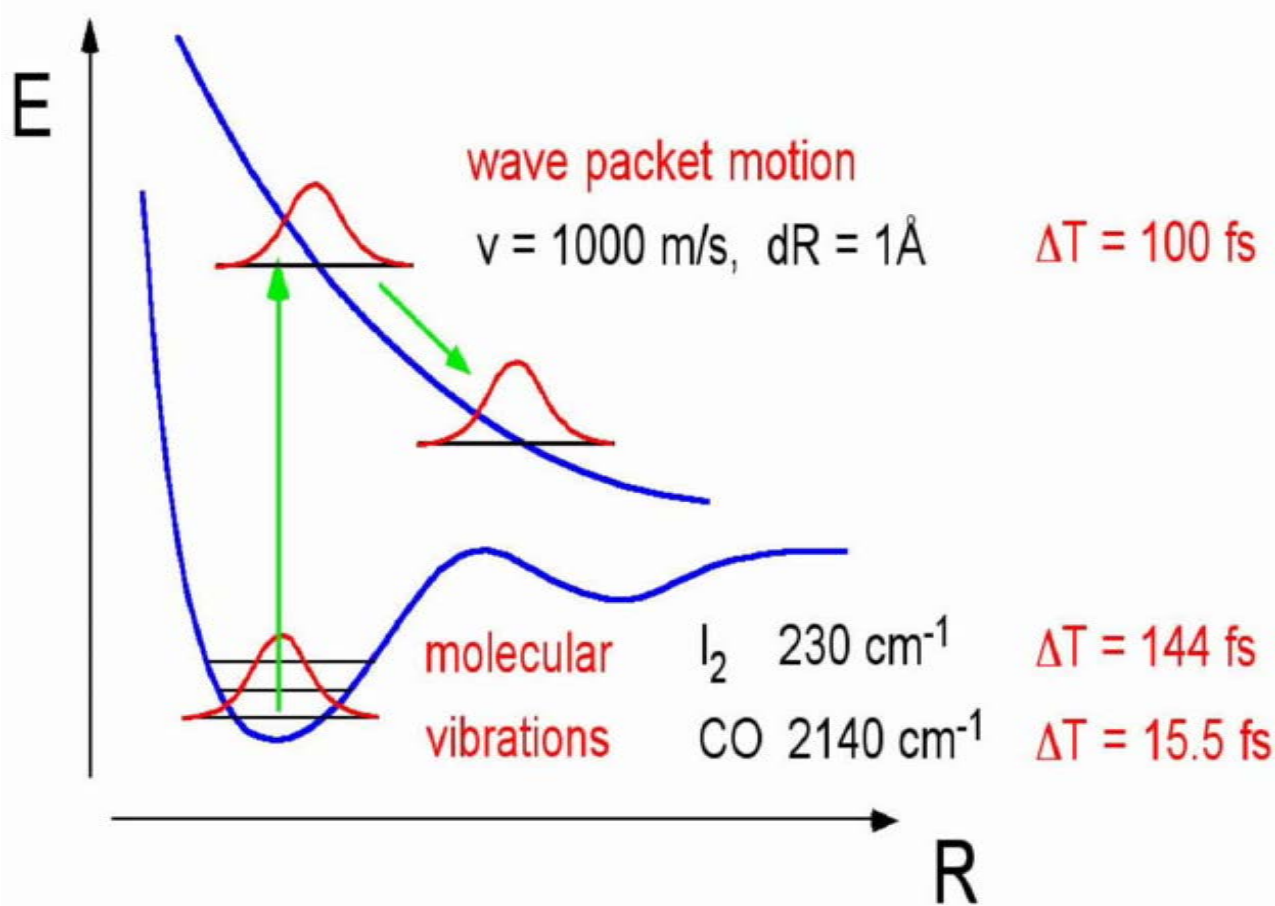
d.h. (beispielhaft für Cl-Spinzustände):





# Pump and probe experiments

Wesentliche Fortschritte auf dem Gebiet der Reaktionsdynamik wurden durch den Einsatz von Lasern erzielt. Typisch sind hier „pump and probe“-Experimente, bei denen ein Laser(puls) die Edukte präpariert und ein zweiter die Produkte probt (analysiert).

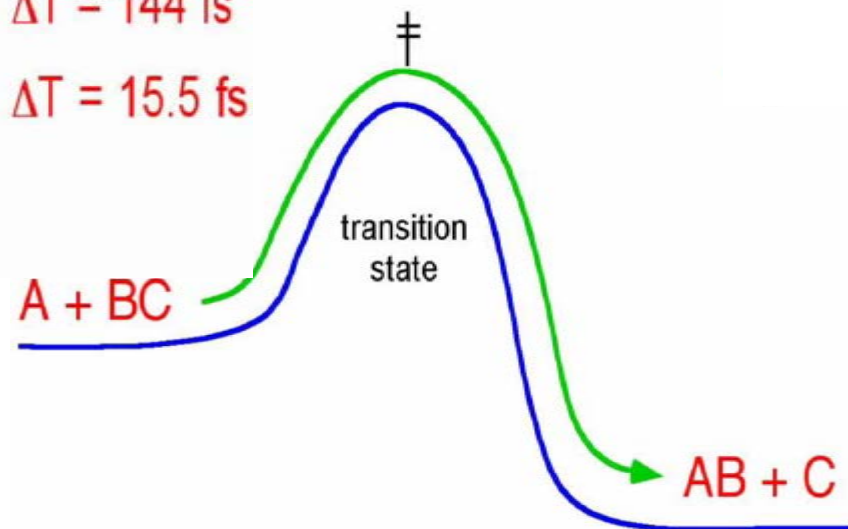


## 1. Time resolution

*Need femtosecond laser pulses for direct observation in **time domain** (low energy resolution), ...*

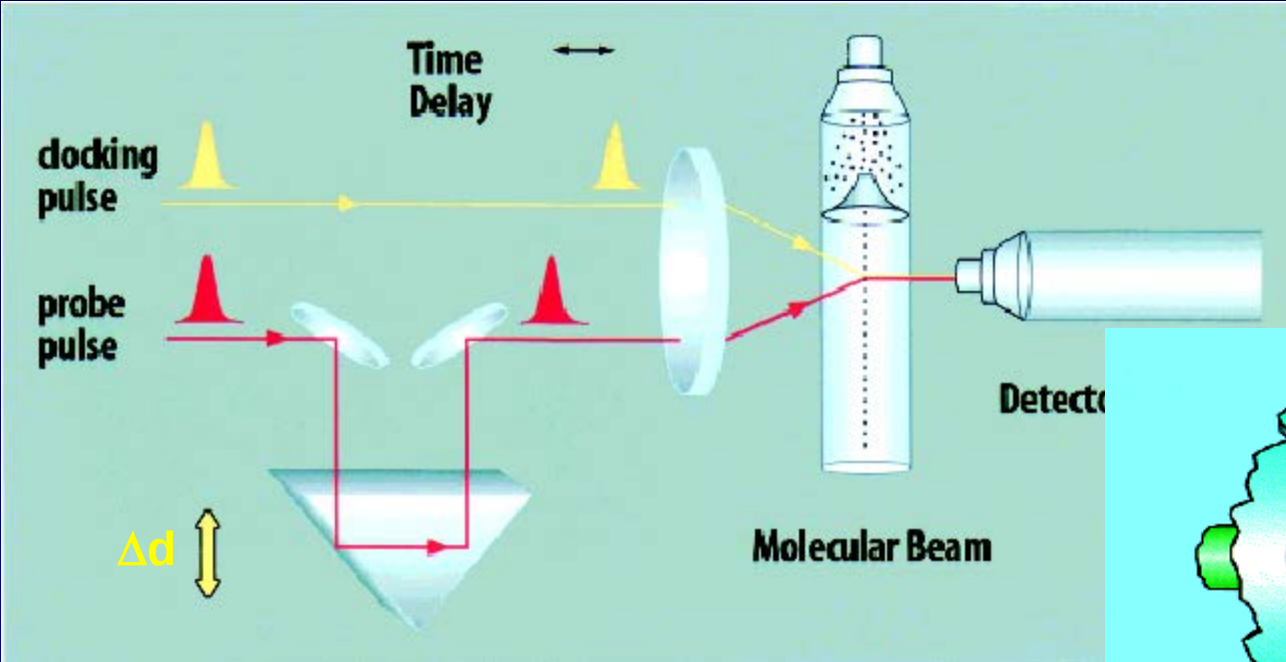
## 2. High resolution

*... but nanosecond laser pulses for sufficient energy resolution ( $v, J, s$  quantum states)*

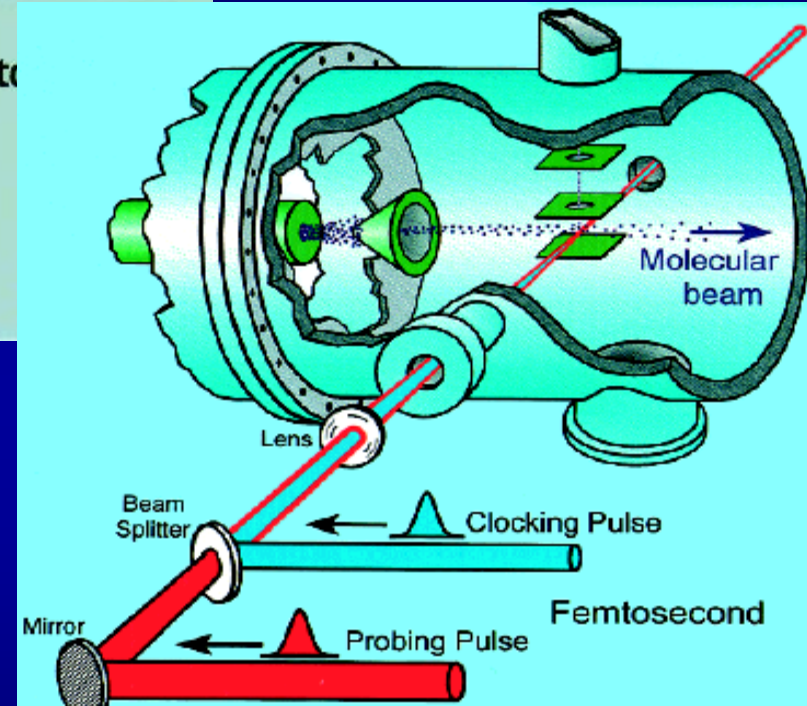


*time resolution*

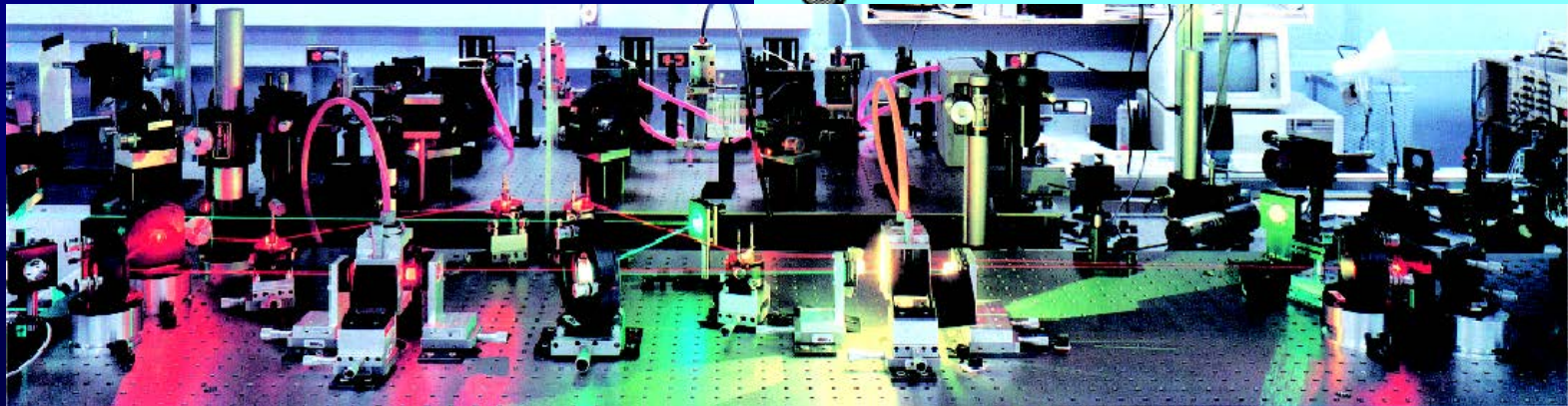
In principle...



$$\Delta t = 2 \Delta d / c \quad 1 \mu\text{m} = 6.7 \text{ fs}$$



....and  
in reality



**Dynami**  
**Fem**

**Femtosecond laser:**

**D**

**Non-linear setups**

**TOPAS: 270 nm ... 3  $\mu$ m**

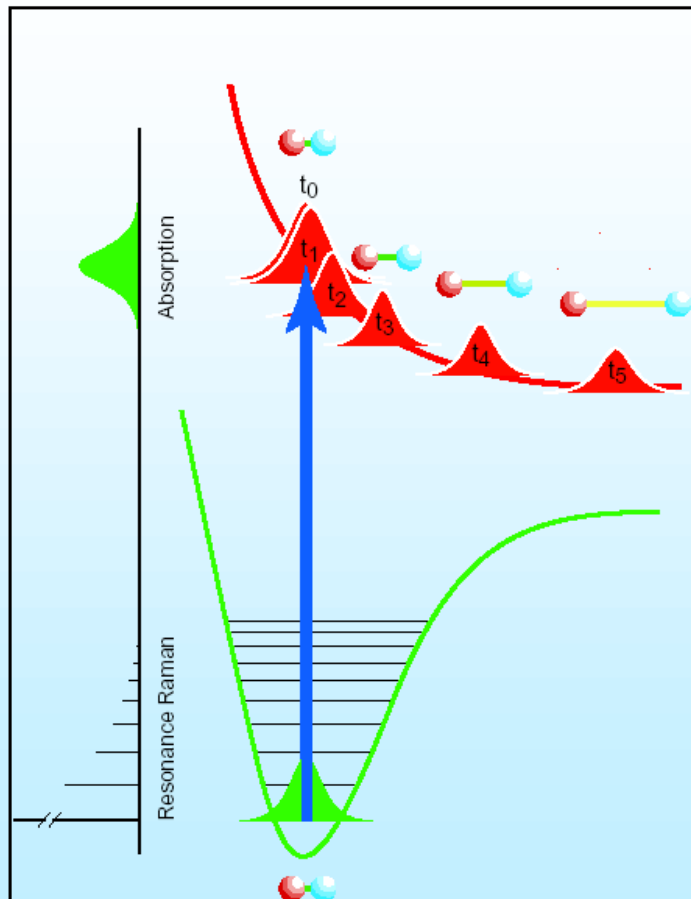
**WLC generator:**

**White light continuum**

**Mirrors, mirrors, ....**



# Wavepacket evolution in time and space



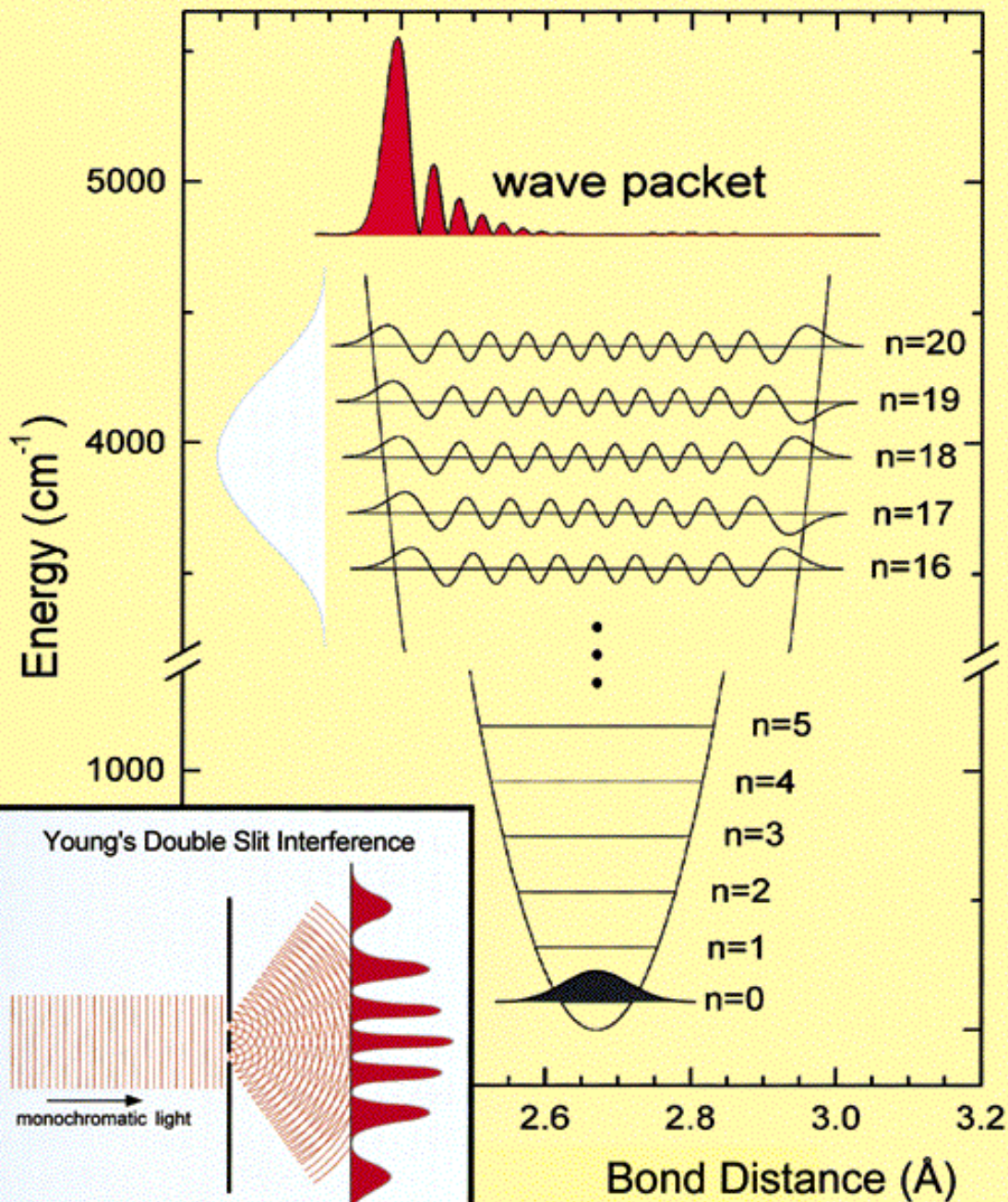
Photodissociation of an isolated diatomic molecule is the simplest of chemical reactions.

$t=0$  is easily defined

The initial wave-function is well defined

The wave-function remains localized throughout the reaction

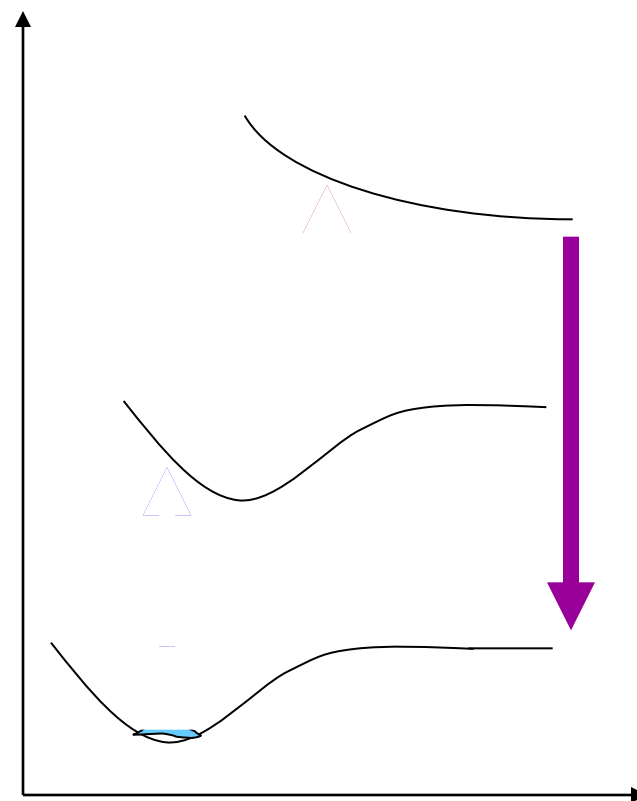
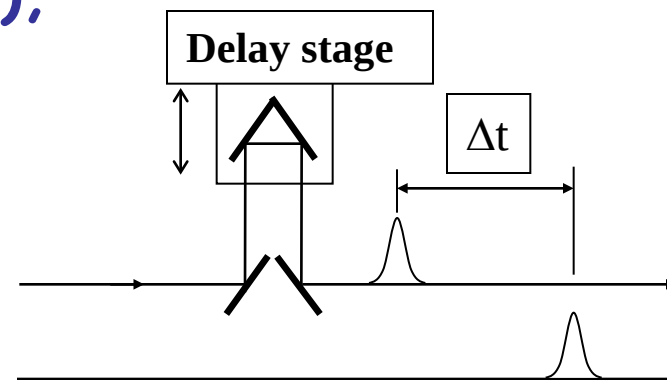
investigate these reactions



Coherent, localized wave packet (de Broglie length  $\sim 0.04 \text{ \AA}$ ) calculated for a diatomic molecule (iodine) for a 20 fs pulse. The contrast with the diffuse wave function limit (quantum number  $n$ ) is clear. The inset shows Thomas Young's experiment (1801) with the interference which is useful for analogy with light.

# Molecular quantum dynamics (MQD), Wavepacket (WP) and fs laser spectroscopy

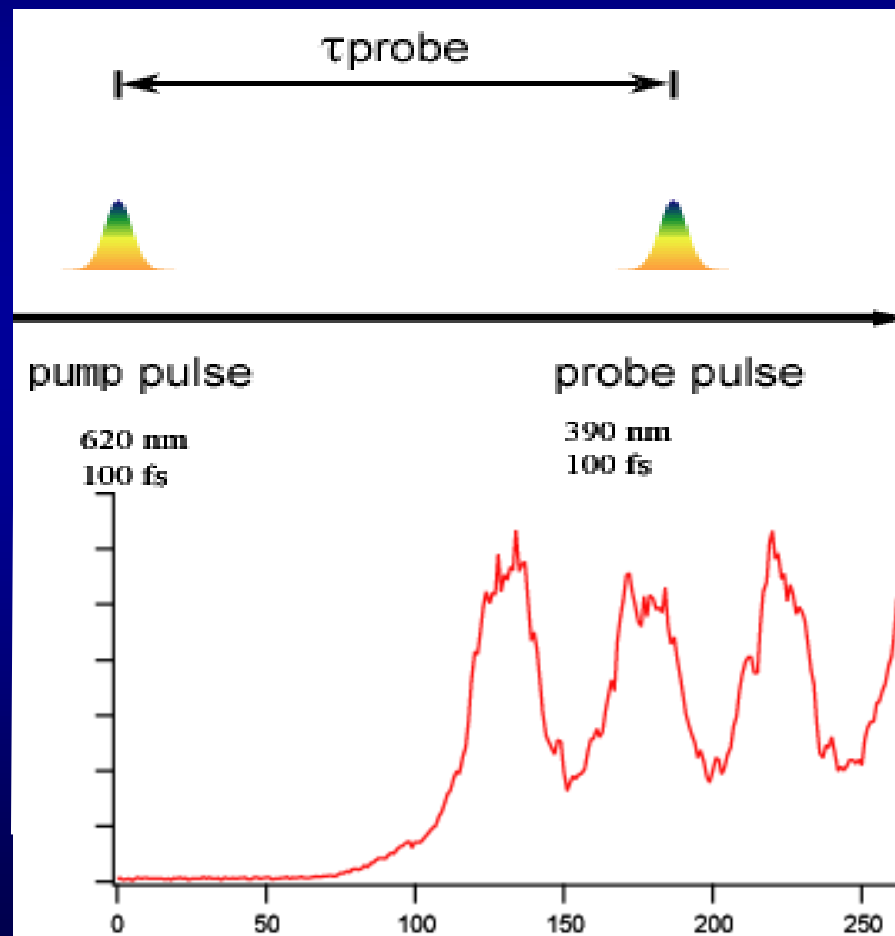
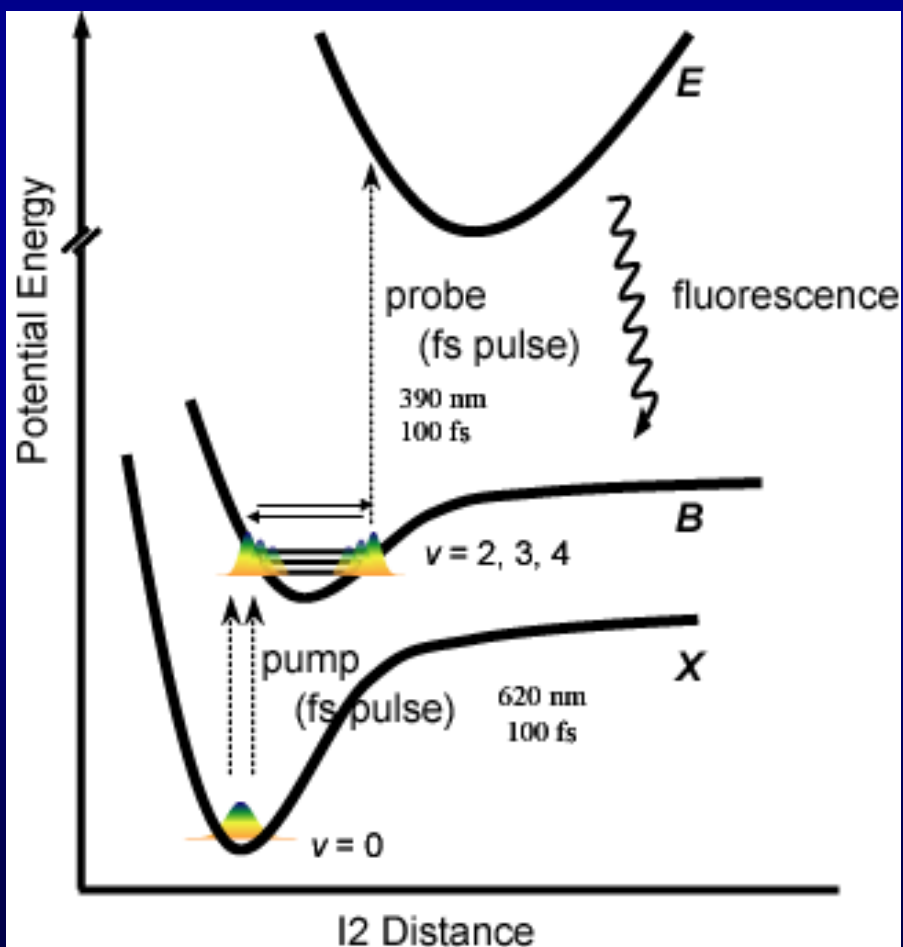
1. MQD – nuclear vibration, rotation & change of electronic configuration.
2. WP – nonstationary superposition of a set of wavefunctions with fixed phase relationship.
3. Pump-probe technique – pump process, probe process, delay time and time zero.



# Zewail's Femtochemistry

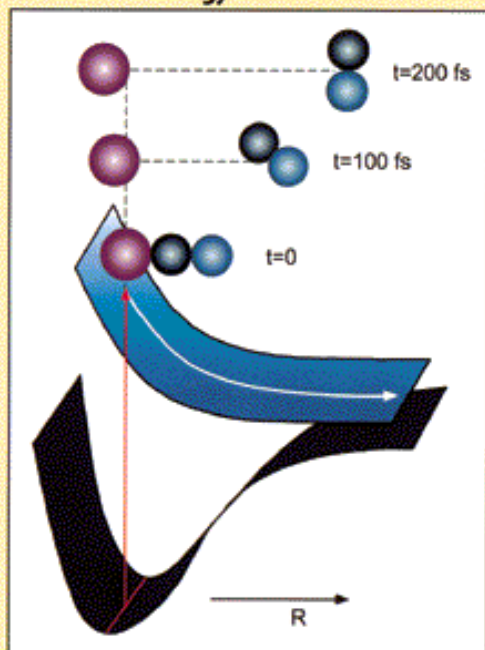
Femtosecond time-resolved pump-probe experiments made a nuclear motion of a molecular system visible.

*“Conventional” time-resolved pump-probe measurement for vibrational motion in  $I_2$  molecules*

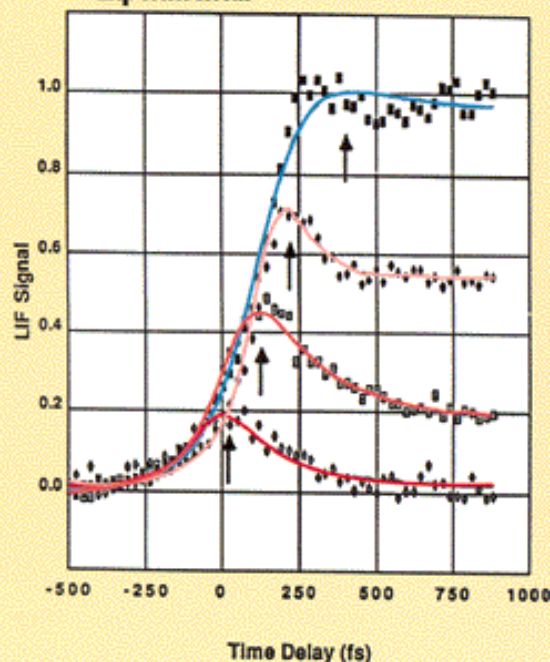


Revisit to Zewail's Nobel prize experiment.

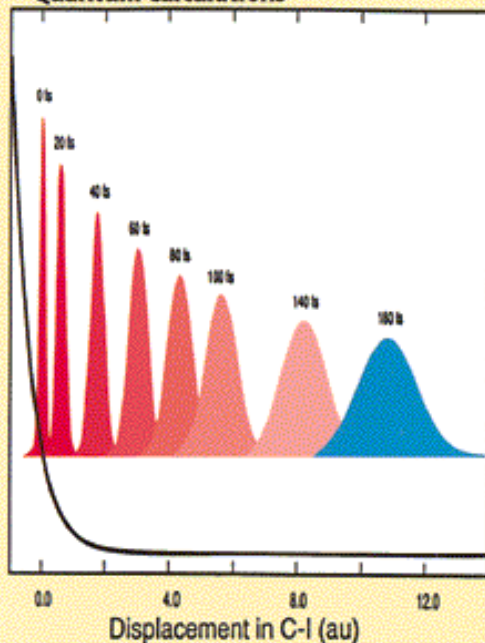
## Potential Energy Surfaces



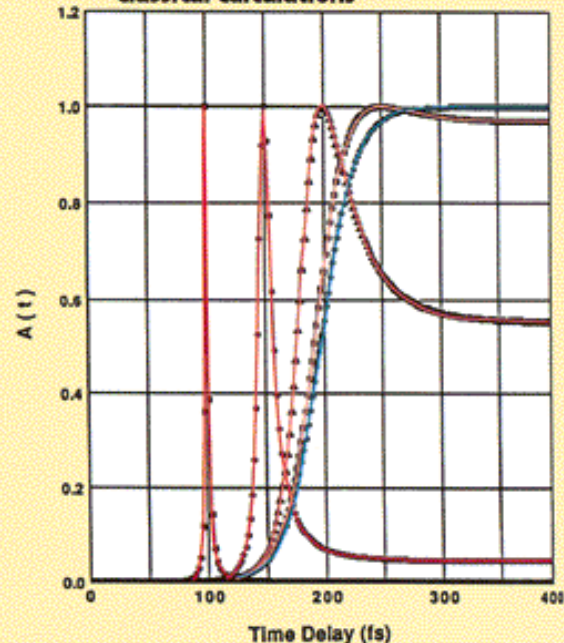
## Experimental



## Quantum Calculations



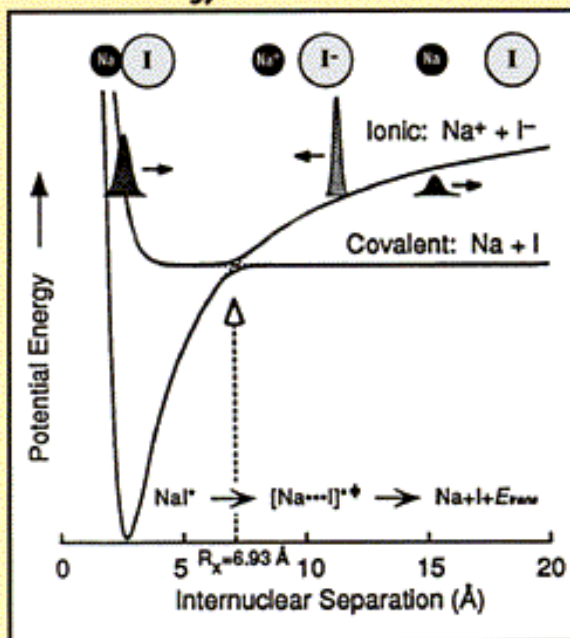
## Classical Calculations



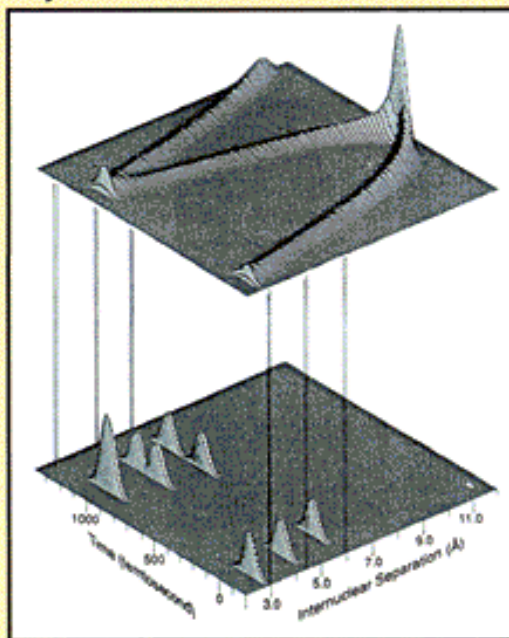
## Figure

Femtochemistry of the ICN reaction, the first to be studied. The experimental results show the probing of the reaction in the transition-state region (rise and decay) and the final CN fragment (rise and leveling) with precise clocking of the process; the total time is 200 fs. The I fragment was also detected to elucidate the translational energy change with time. Classical and quantum calculations are shown.

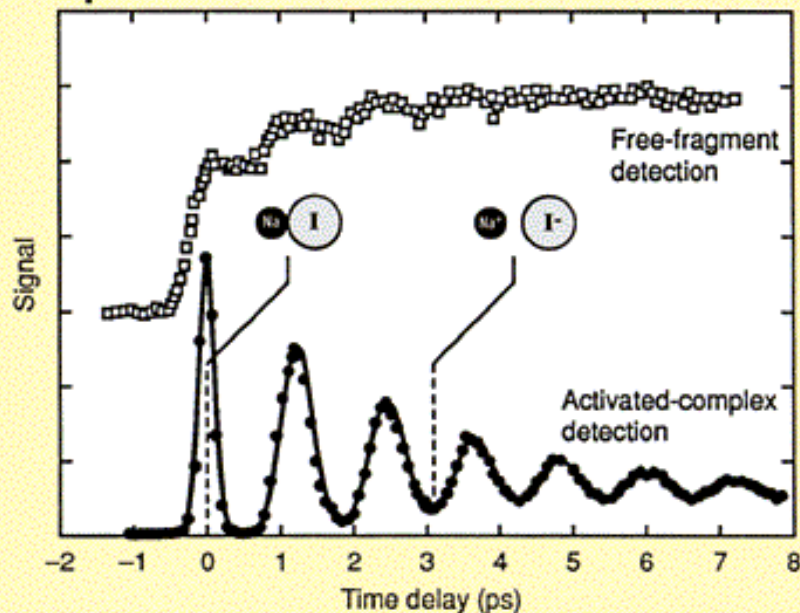
## Potential Energy Surfaces



## Trajectories R,t



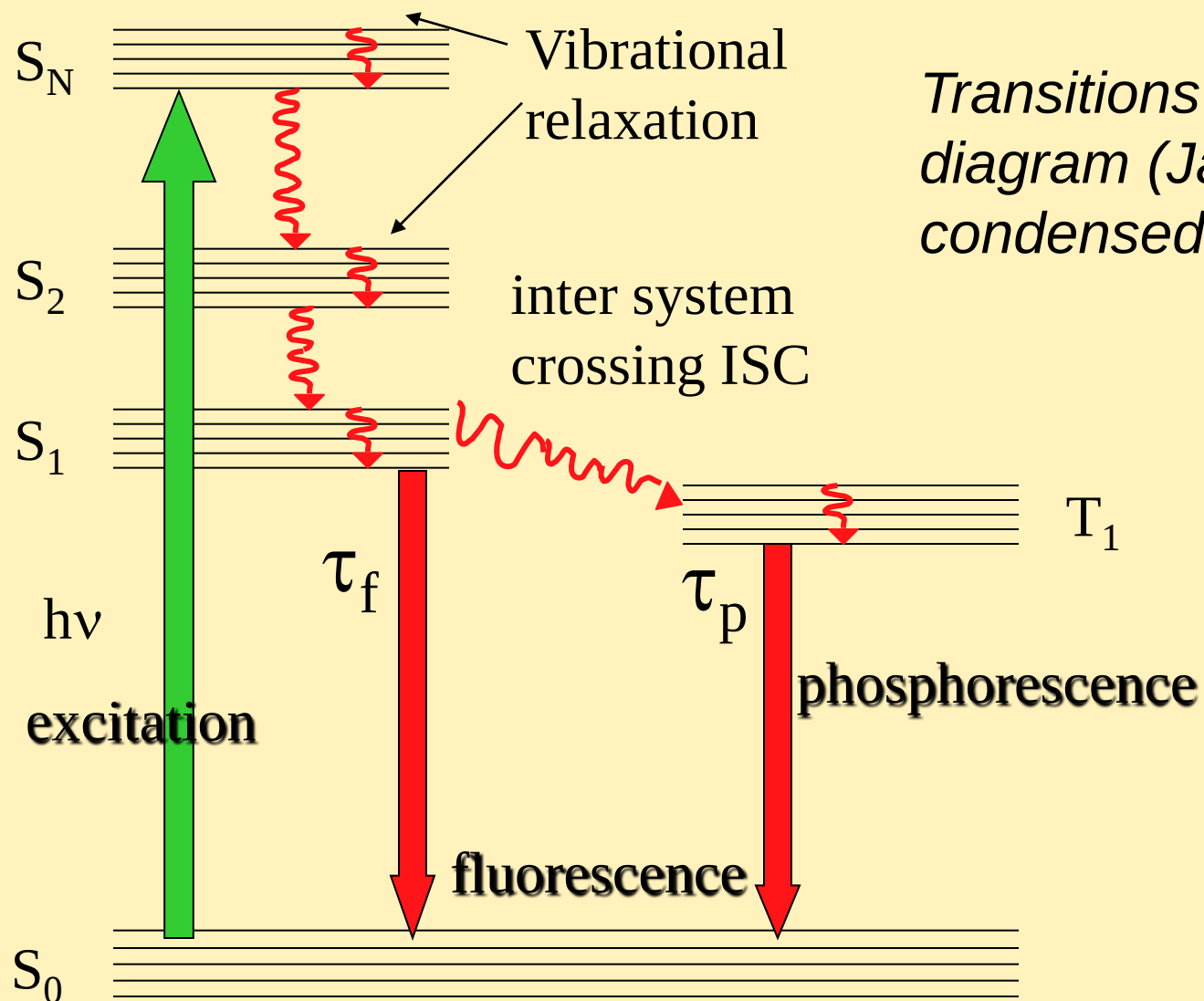
## Experimental



**Figure**

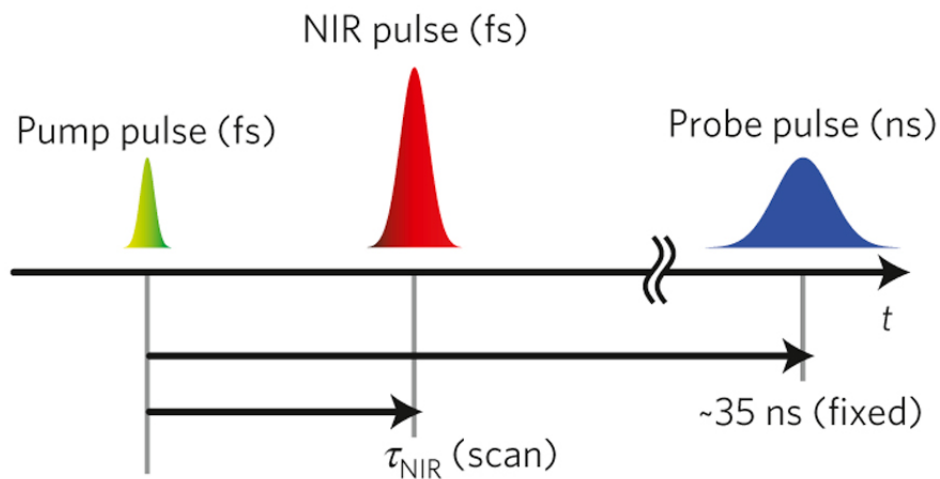
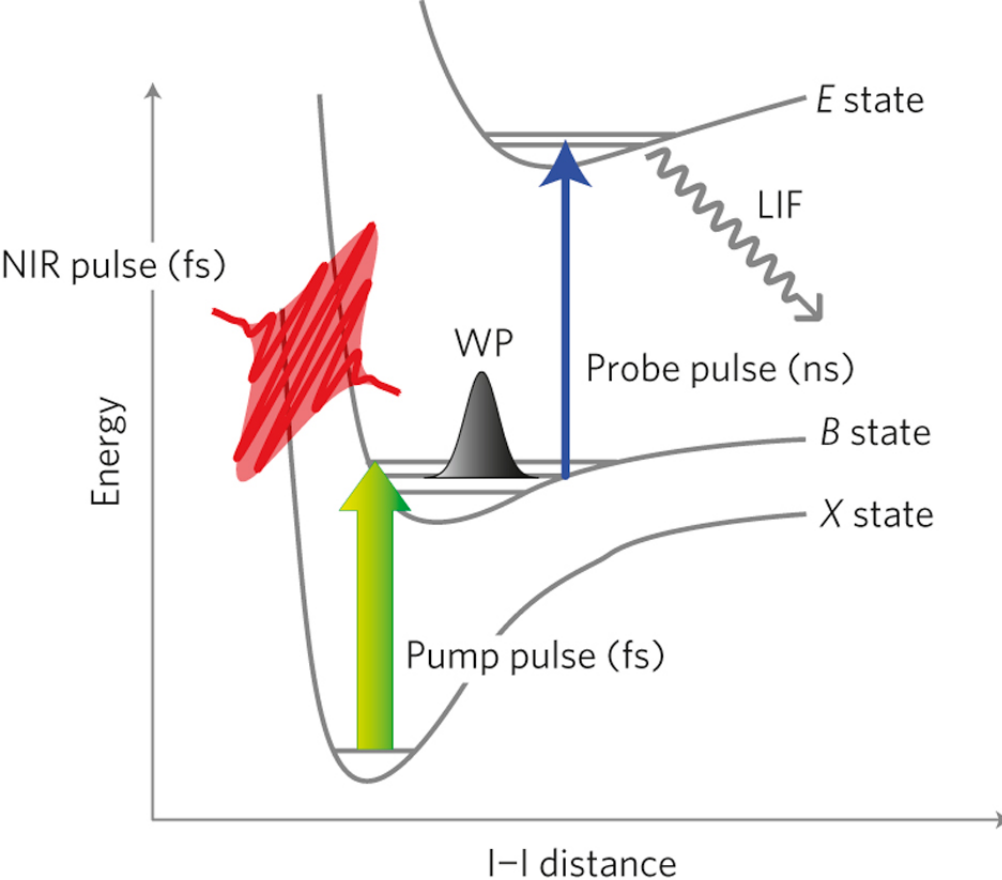
Femtochemistry of the NaI reaction, the paradigm case. The experimental results show the resonance motion between the covalent and ionic structures of the bond, and the time scales for the reaction and for the spreading of the wave packet. Two transients are shown for the activated complexes in transition states and for final fragments. Note the "quantized" behavior of the signal, not simply an exponential rise or decay of the ensemble. The classical motion is simulated as trajectories in space and time.

# Basic photophysics

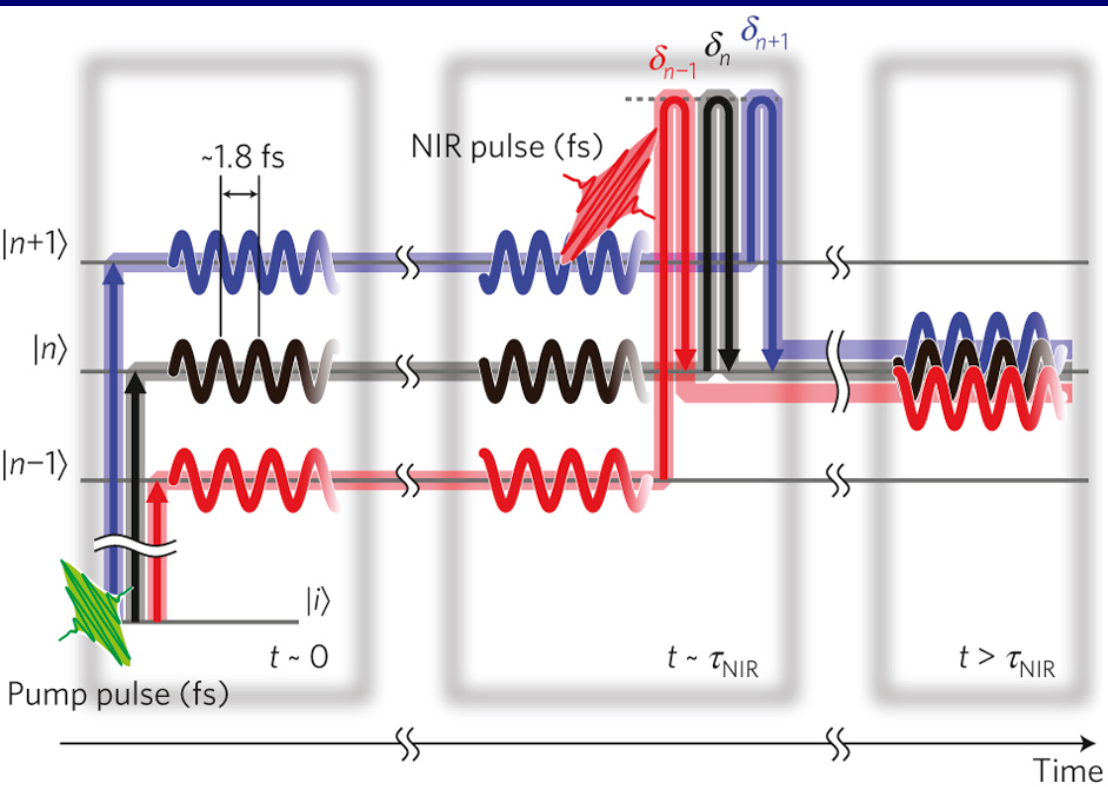


*Transitions in an energy diagram (Jablonski) of the condensed phase*

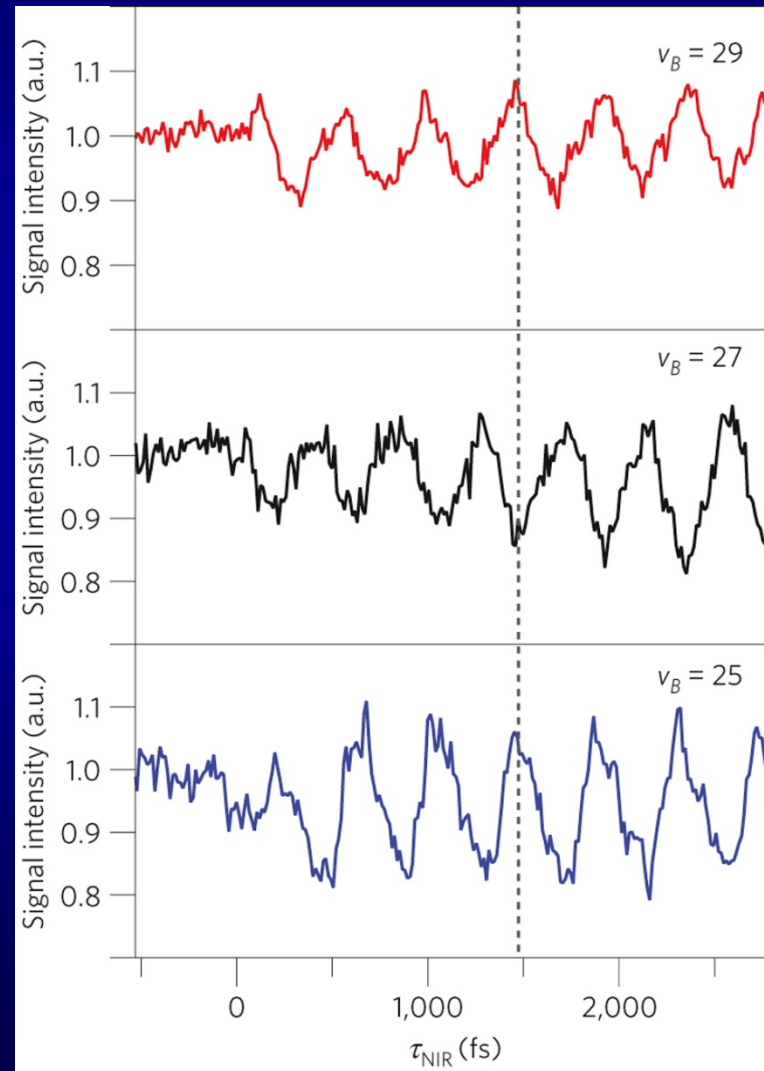
# Wellenpakete und Interferenz



Strong-laser-induced quantum interference  
Haruka Goto, Hiroyuki Katsuki, Heide Ibrahim,  
Hisashi Chiba & Kenji Ohmori  
Nature Physics, 7 (2011) 383–385  
doi:10.1038/nphys1960

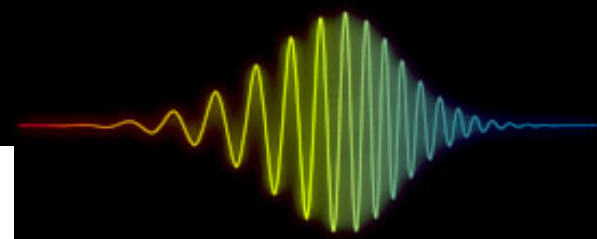
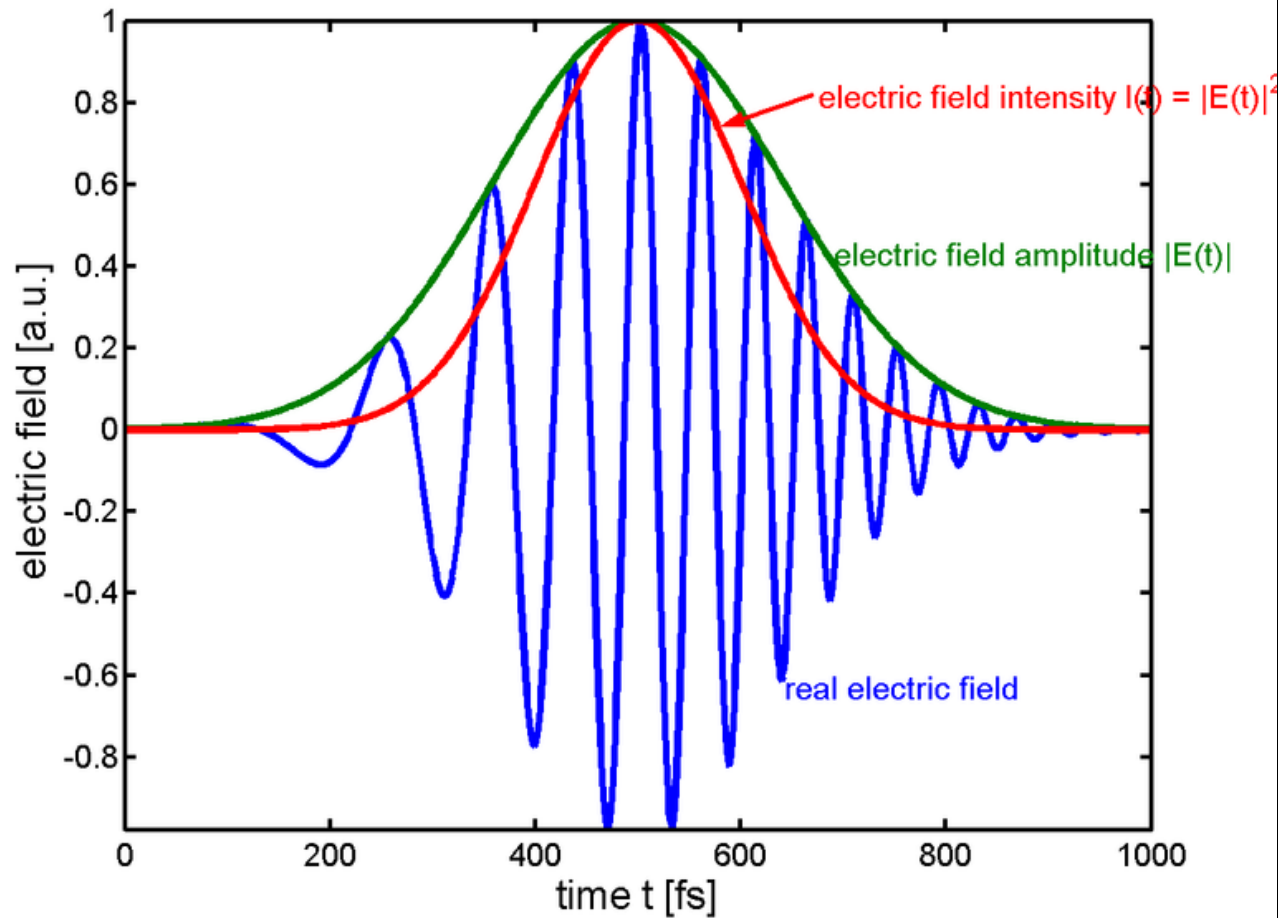


Die möglichen Wege über  $|n-1\rangle$ ,  $|n\rangle$  und  $|n+1\rangle$  interferieren miteinander.

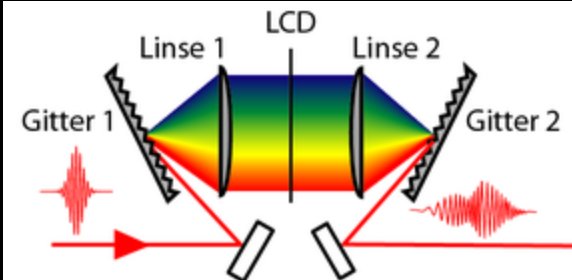


*The road ahead*

# *A chirp...*

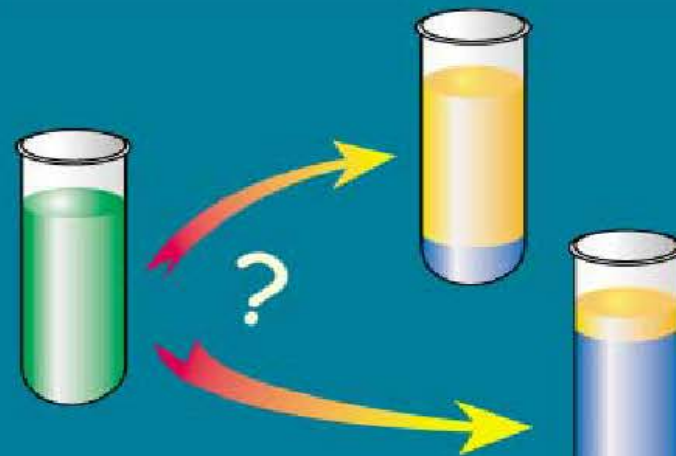
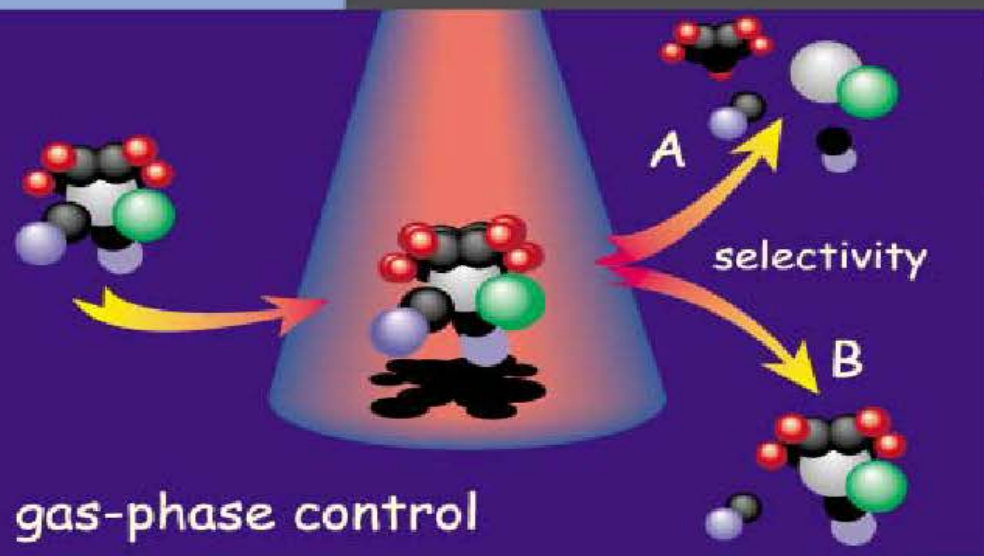
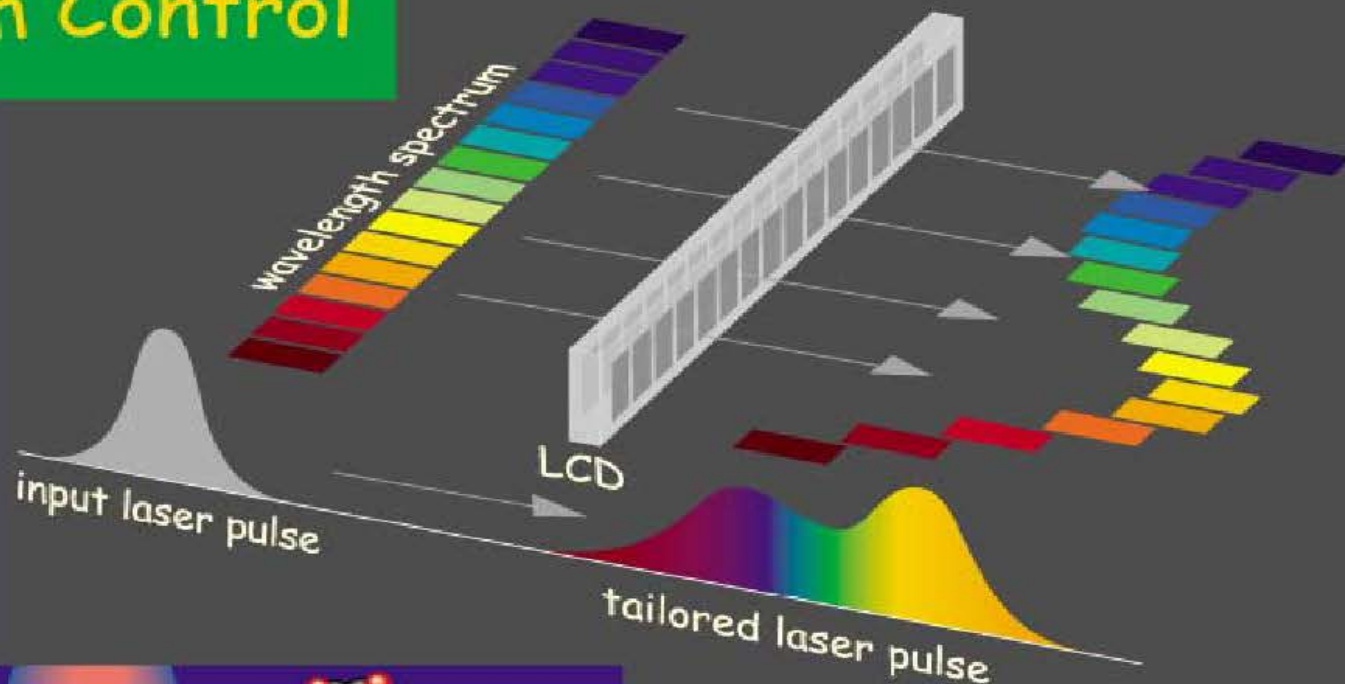


## *and it's creation...*

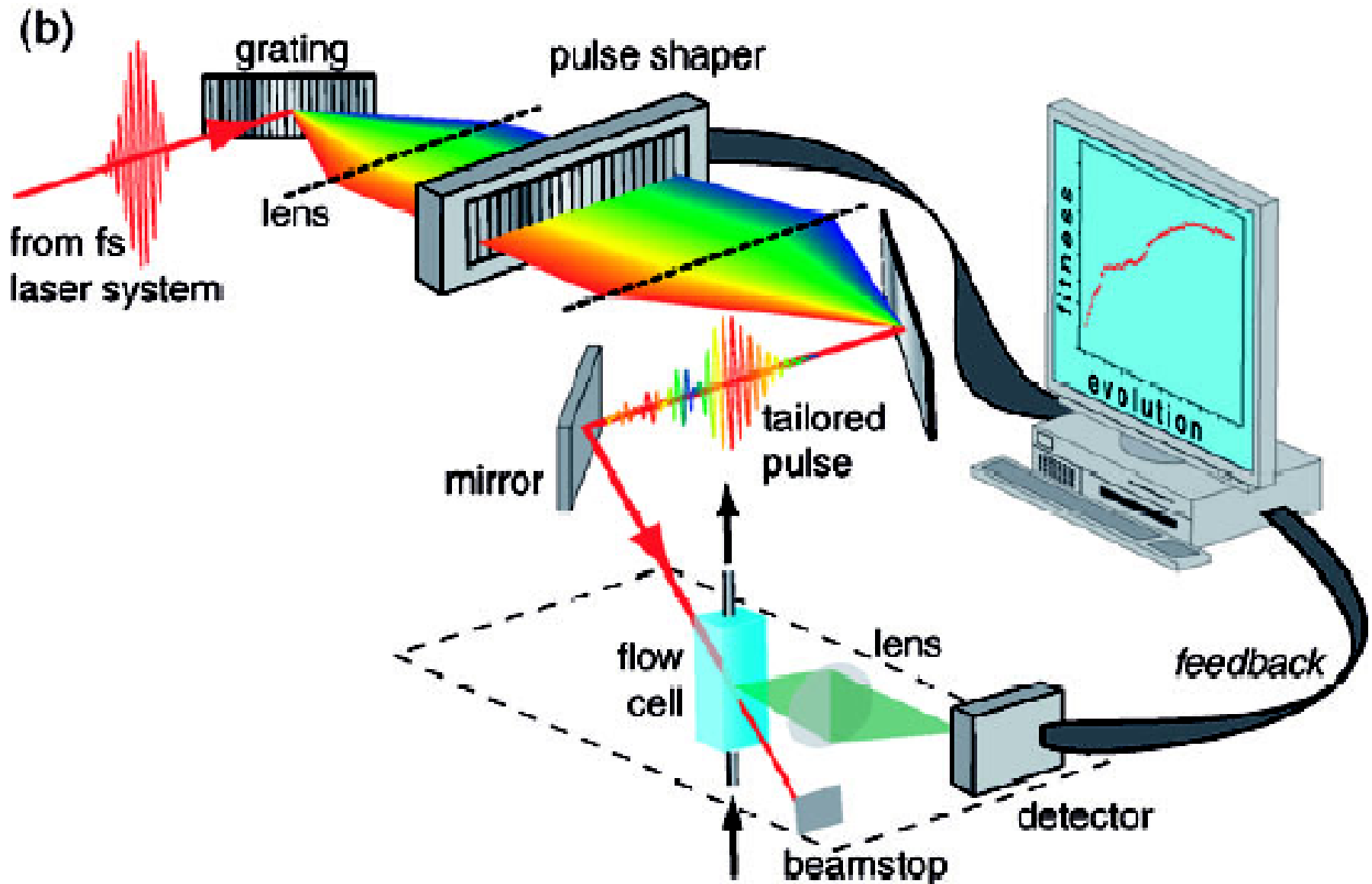


# Adaptive Quantum Control

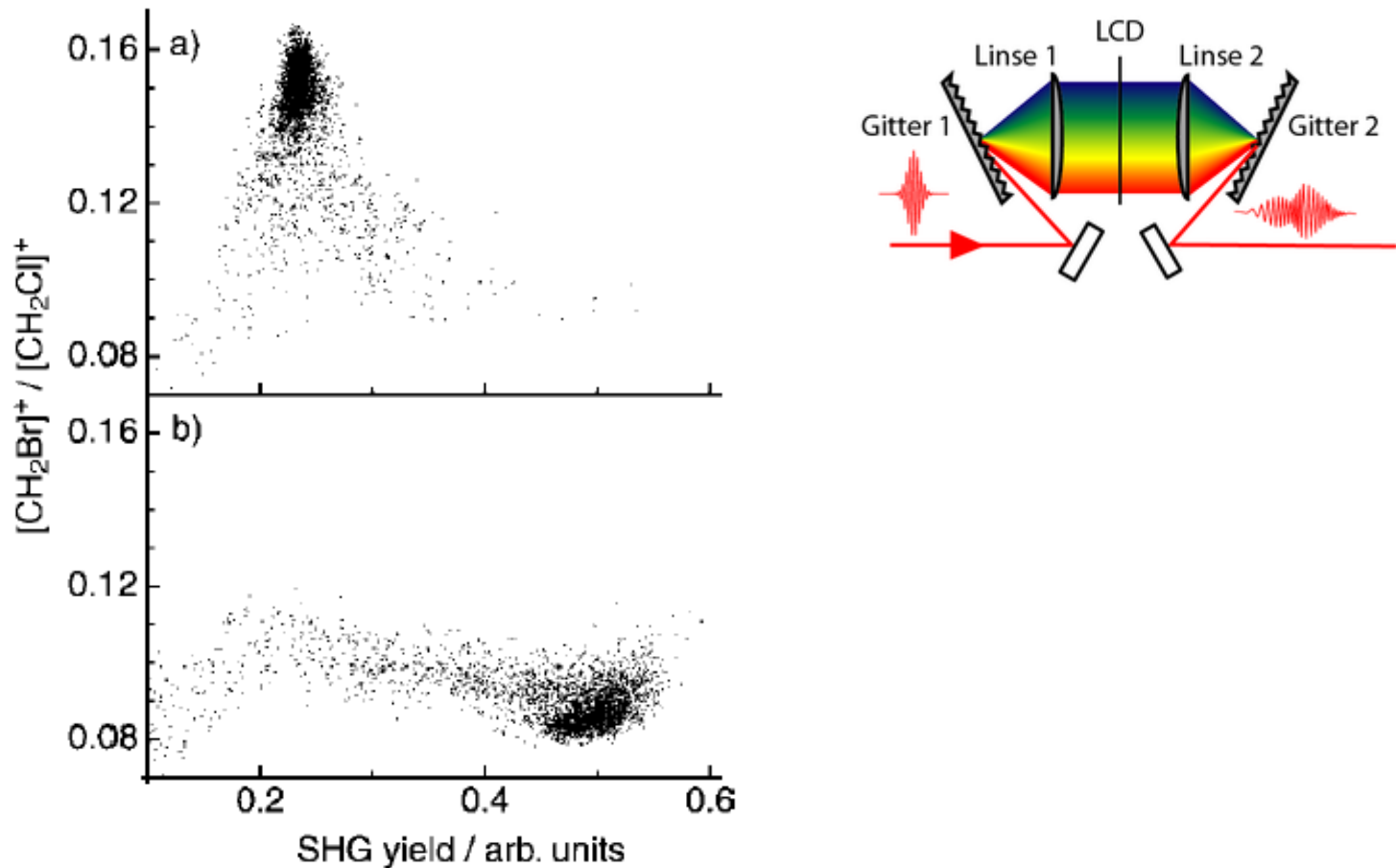
femtosecond pulse shaping



# *Adaptive Quantum Control*



# Quantum control

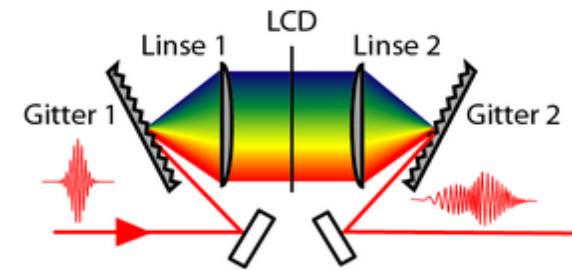
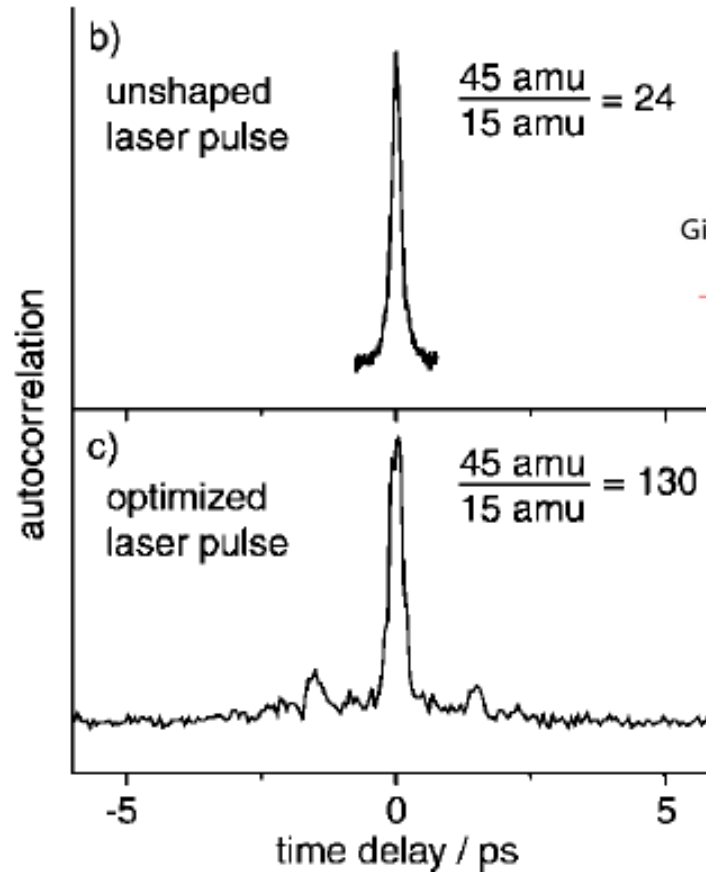
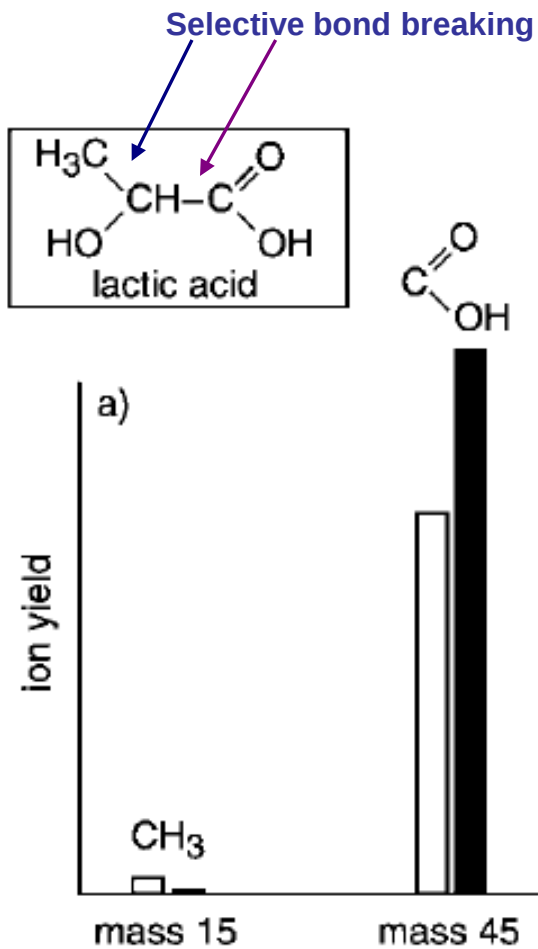


**Figure 12.** Correlation diagrams for selective bond breakage in  $\text{CH}_2\text{BrCl}$ . The value of the  $[\text{CH}_2\text{Br}]^+ / [\text{CH}_2\text{Cl}]^+$  branching ratio is plotted versus SHG yield for all laser pulses explored in the two optimizations of a)  $[\text{CH}_2\text{Br}]^+ / [\text{CH}_2\text{Cl}]^+$  maximization and b) SHG maximization.

T. Brixner, G. Gerber

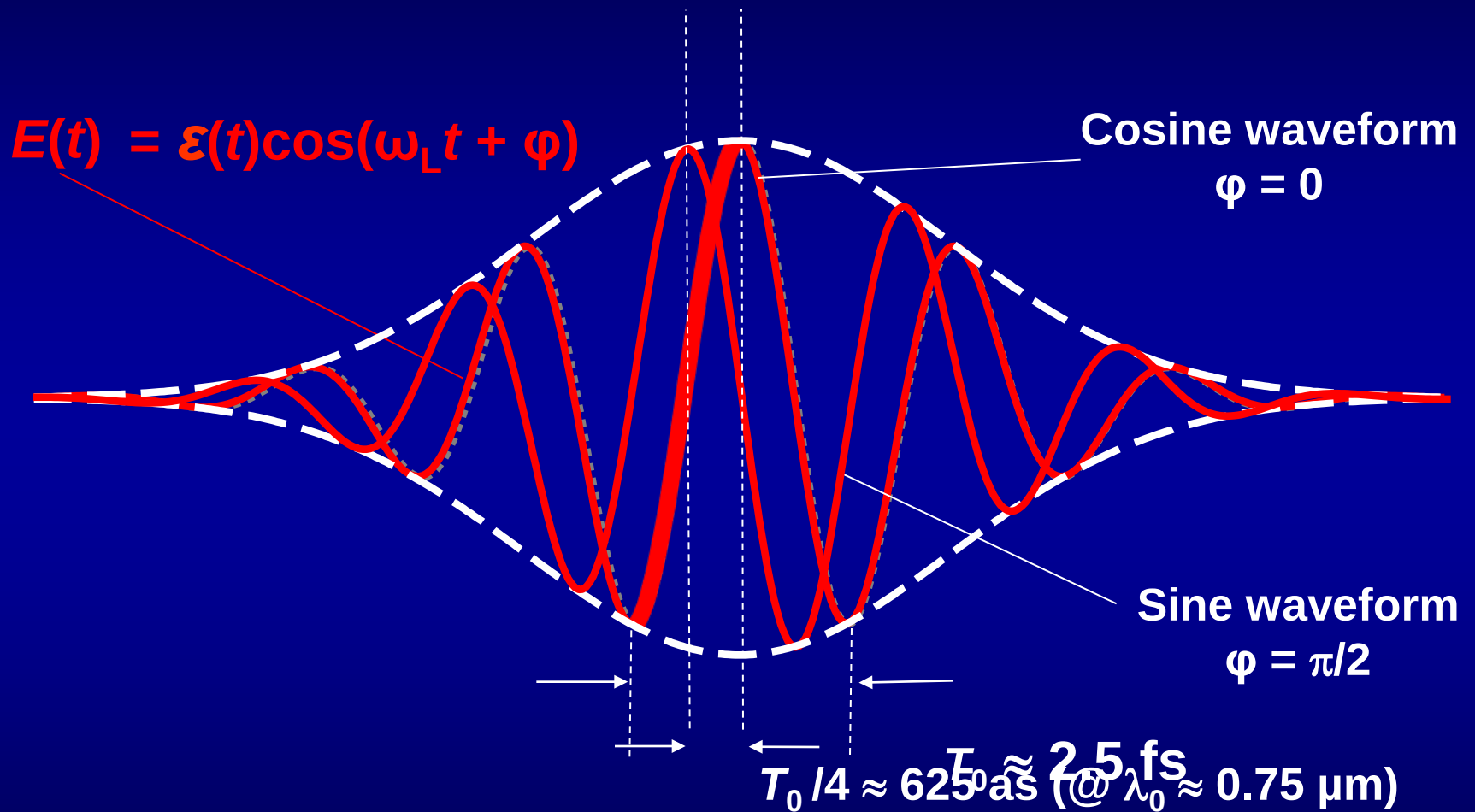
CHEMPHYSICHEM 2003,  
4, 418 - 438

# Quantum control



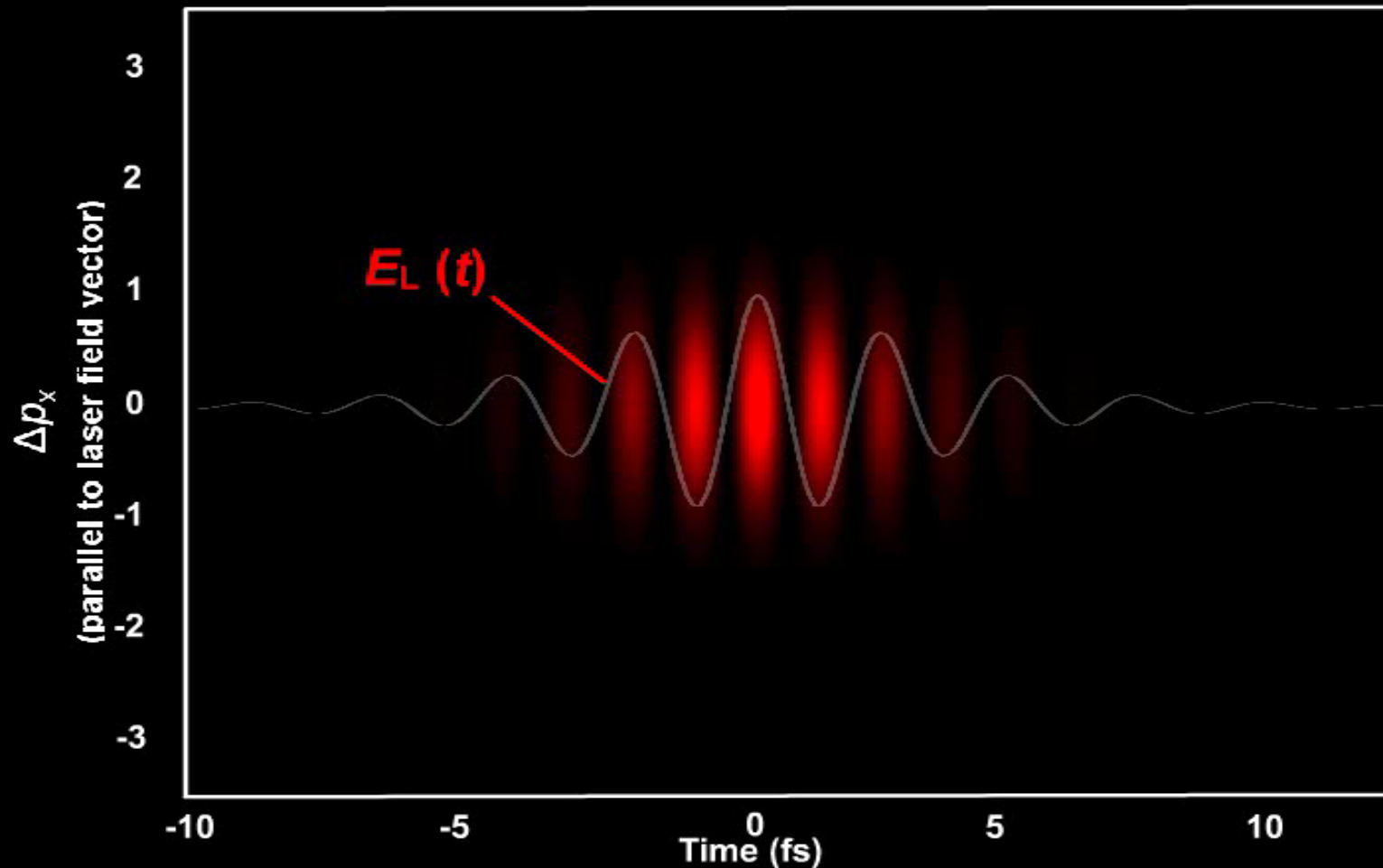
**Figure 13.** Selective bond breaking in lactic acid. The desired fragment is [COOH], the undesired fragment is [CH<sub>3</sub>]. a) Absolute ion yields of these two fragments are plotted for unmodulated laser pulses (b) and for laser pulses where the COOH<sup>+</sup>/CH<sub>3</sub><sup>+</sup> ratio was maximized (c). The branching ratio is increased by over a factor of 5 from 24 to 130. Intensity autocorrelations are shown after many-parameter [COOH]<sup>+</sup>/[CH<sub>3</sub>]<sup>+</sup> maximization.

Attosecond metrology: requires *controlled* variation of a physical quantity within 1 femtosecond

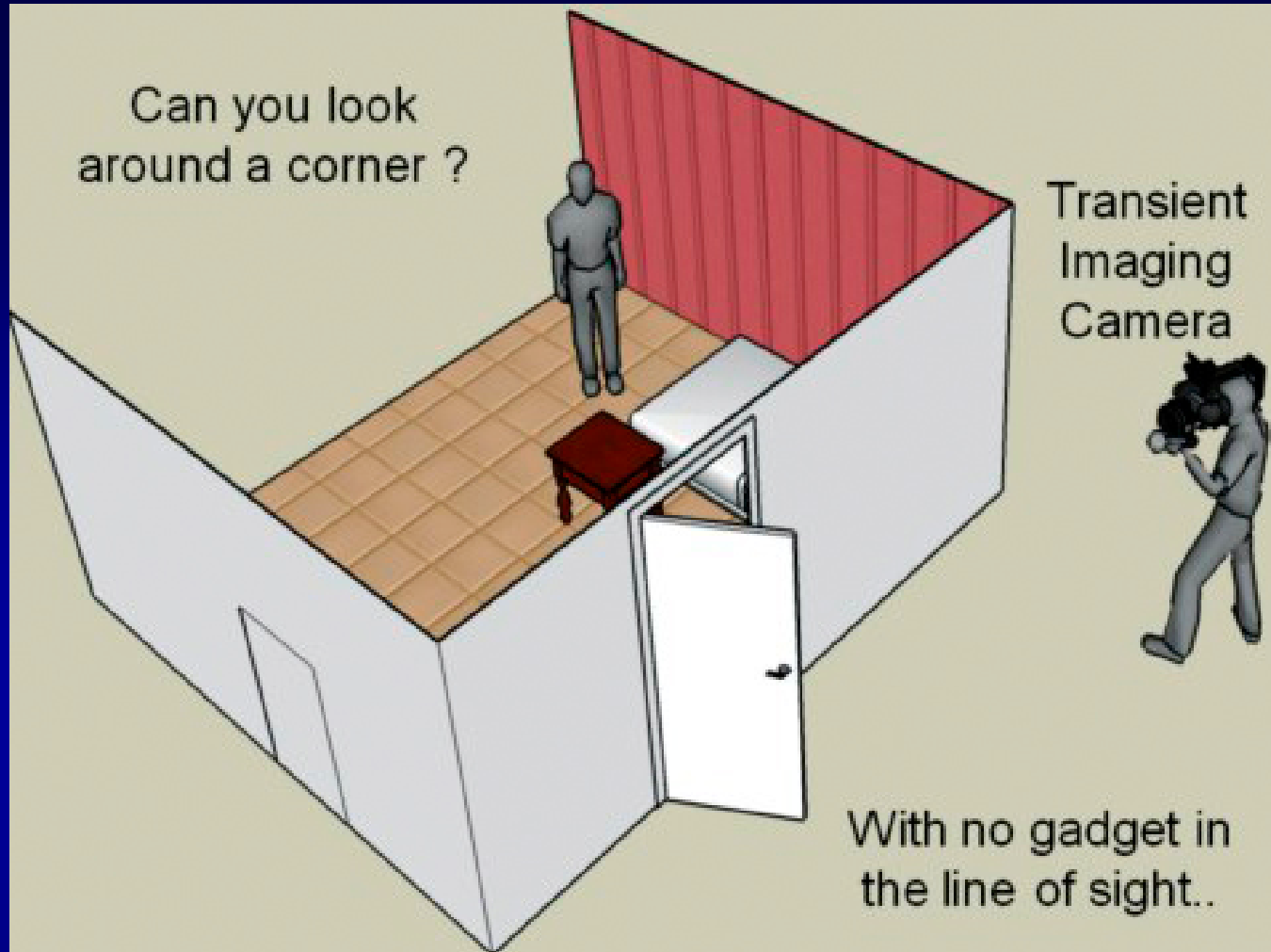


Requires measurement & control of  $\varphi$

# Momentum transfer depends on instant of electron release within the wave cycle

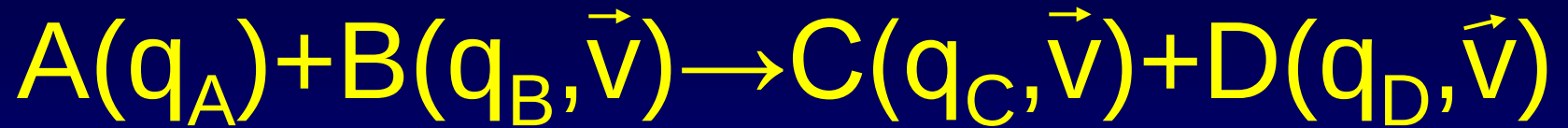


$$\Delta p(t) = e \int_t^{\infty} E_L(t') dt' = eA_L(t)$$



Über ihren Blitz schickt eine Kamera extrem kurze, genau gerichtete Lichtpulse aus, die von der Tür abprallen und von dort aus in alle Richtungen verstreut werden. Teils gelangen die Photonen direkt zur Kamera zurück, teils dringen sie auch in den Raum ein und erfassen unter anderem die Person. Ein Bruchteil dieser Teilchen erreicht wieder die Tür, die der Kamera ja bereits bekannt ist, wiederum nur ein Teil davon gelangt zurück in die Linse und wird von einem Computer analysiert.

# *High resolution experiments*



- Präparation der Edukte  
Einfluss der Translation und der inneren Energie, wie Vibration, Rotation, Feinstrukturzustände
- Beobachtung der Produkte  
in den einzelnen Quantenzuständen,  
Geschwindigkeitsvektoren (räumliche Verteilung)

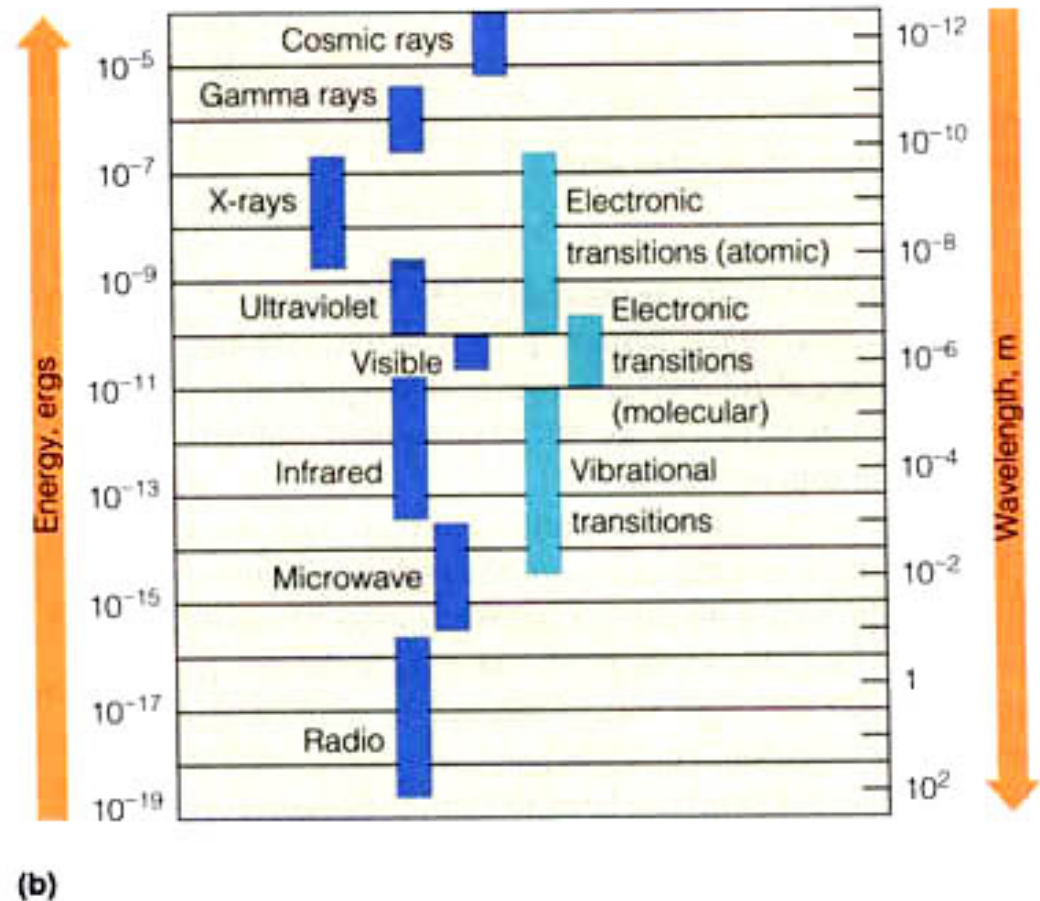
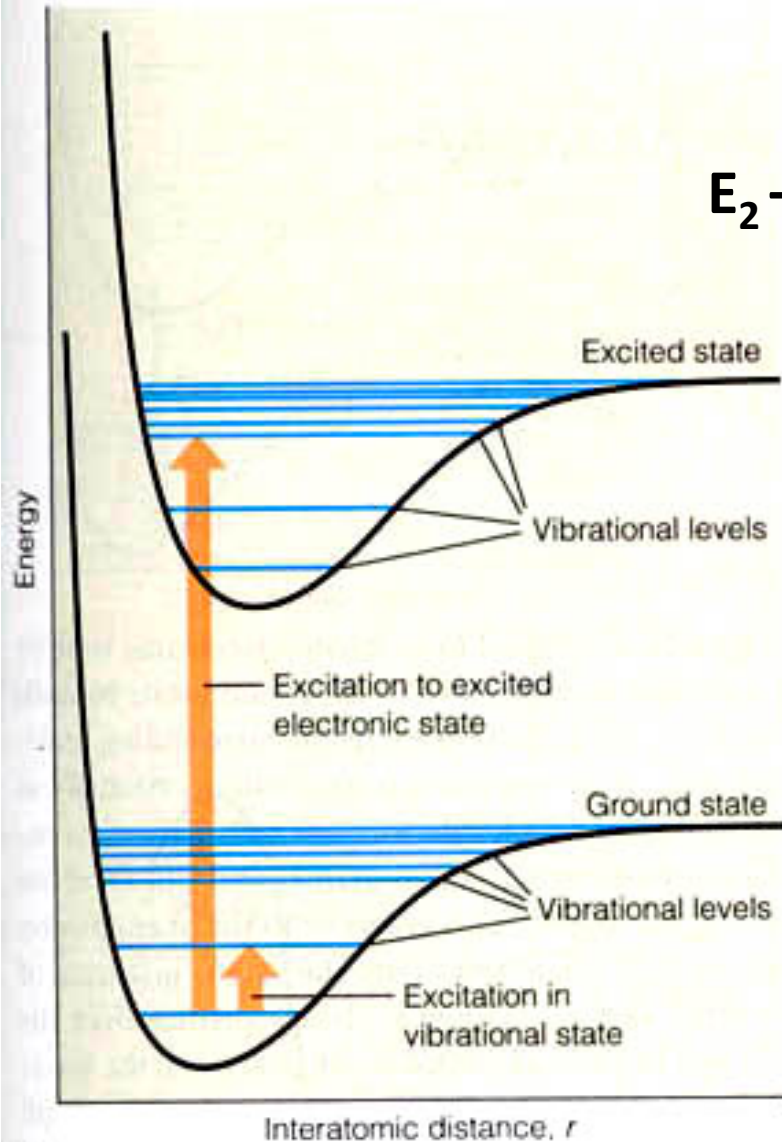
# Detection Techniques - Requirements

- Selectivity
- Sensitivity
- Dynamic Range
- No Interference (with surrounding)
- Universal
- Time Resolution (to observe nascent products)

## Laser & Spectroscopy

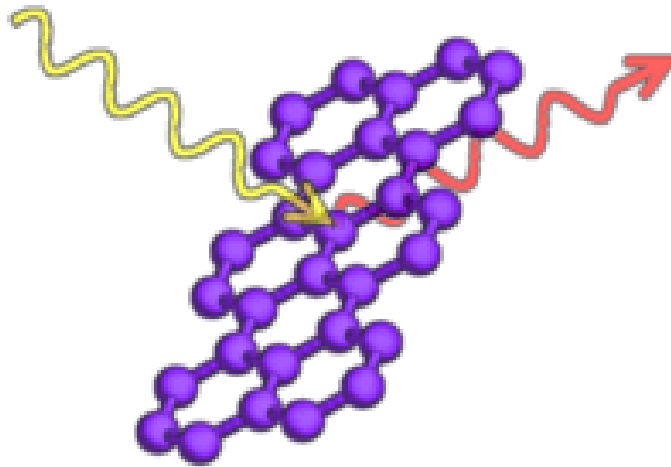
# Spektroskopie

$$E_2 - E_1 = h\nu, \quad \lambda = c/\nu$$



## Was ist hier falsch?

Solch schöne Bilder findet man für gewöhnlich in Lehrbüchern über die Absorption oder Fluoreszenz eines Moleküls:



# Properties of Laser Radiation

1. The laser light can be very monochromatic and can be effectively used for **high resolution spectroscopy**:  $\Delta\lambda/\lambda \approx 10^{-15}$ .
2. The laser beam can be of very low divergent (spatial coherence), i.e. its diameter is increased only slowly in space. With laser beams the diffraction limit is reached:
$$\theta \approx 2\lambda / \pi D$$
It is possible to focus a laser beam of diameter D on a spot of the diameter d:
$$d \approx 2\lambda f / \pi D \approx \lambda / 2$$
where, f denotes the focal distance of the lens.
3. Extremely short laser pulses can be produced. Pulse durations in the **nanosecond** ( $10^{-9}$ ), **picosecond**  $10^{-12}$ , and **femtosecond**  $10^{-15}$  range are now commercially available. Particularly, **femtosecond** laser pulses are of great importance, because they allow to investigate chemical processes **in the real-time domain**.
4. High power output. The continuous CO<sub>2</sub> lasers can produce a high power output of up to 100 kW. These technological lasers are now widely used in industry and military. The pulsed lasers, especially those operating in the pico- and femtosecond time-domain can have peak powers from  **$10^9$  to  $10^{12}$  Watt**. High power pulsed lasers are widely used for investigation of **nonlinear** and **multiple photon processes**.

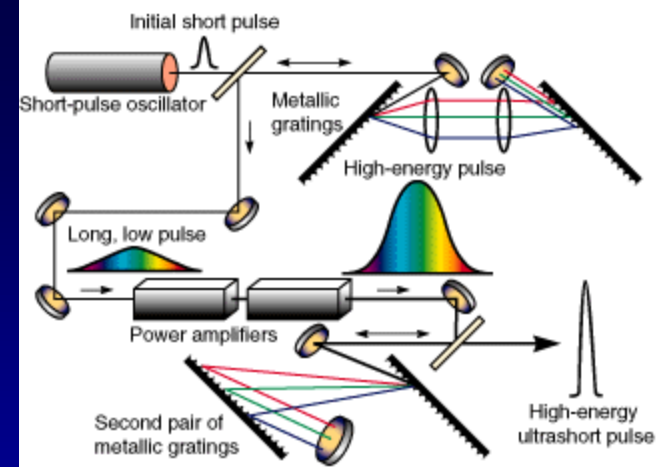
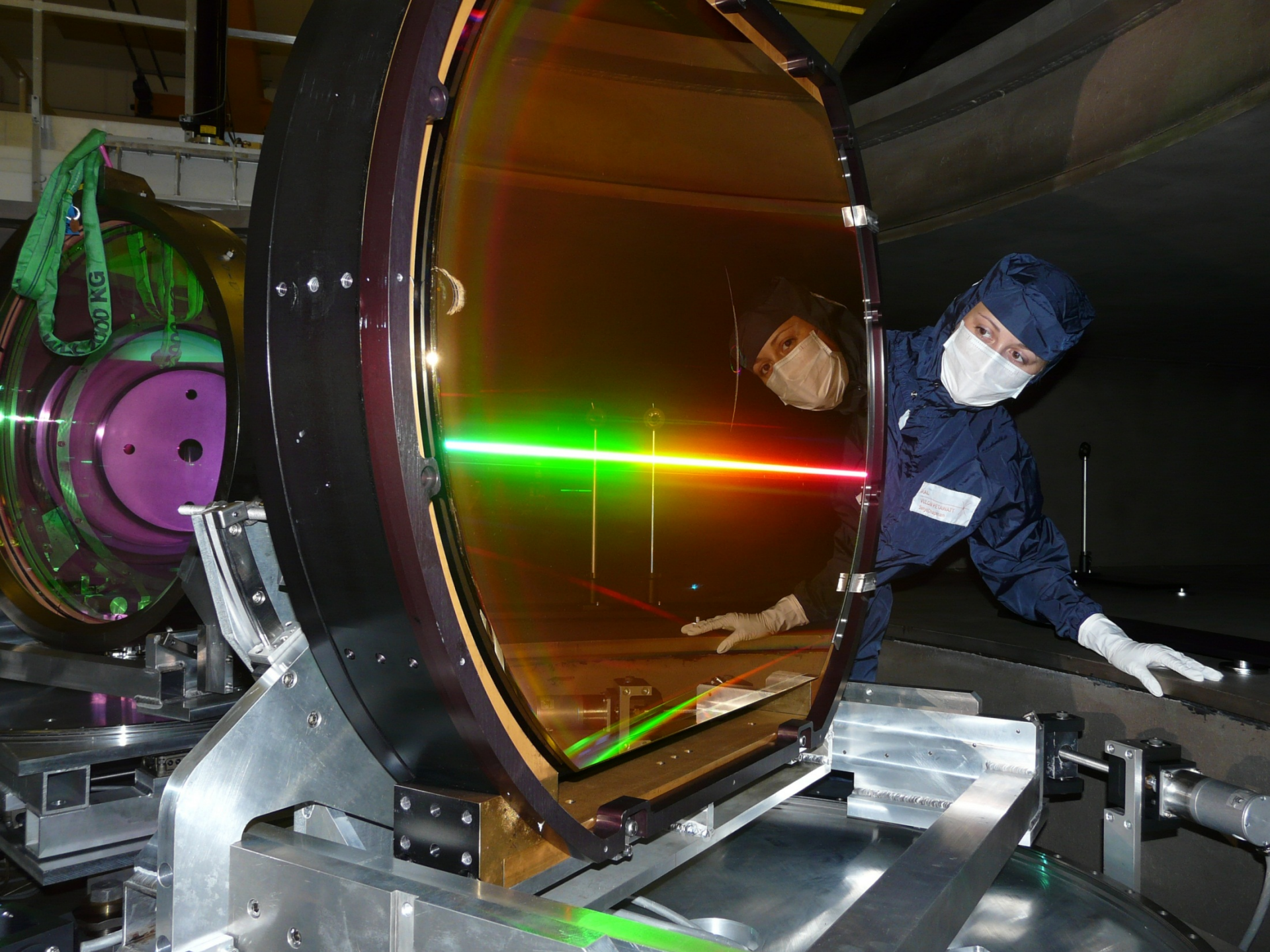
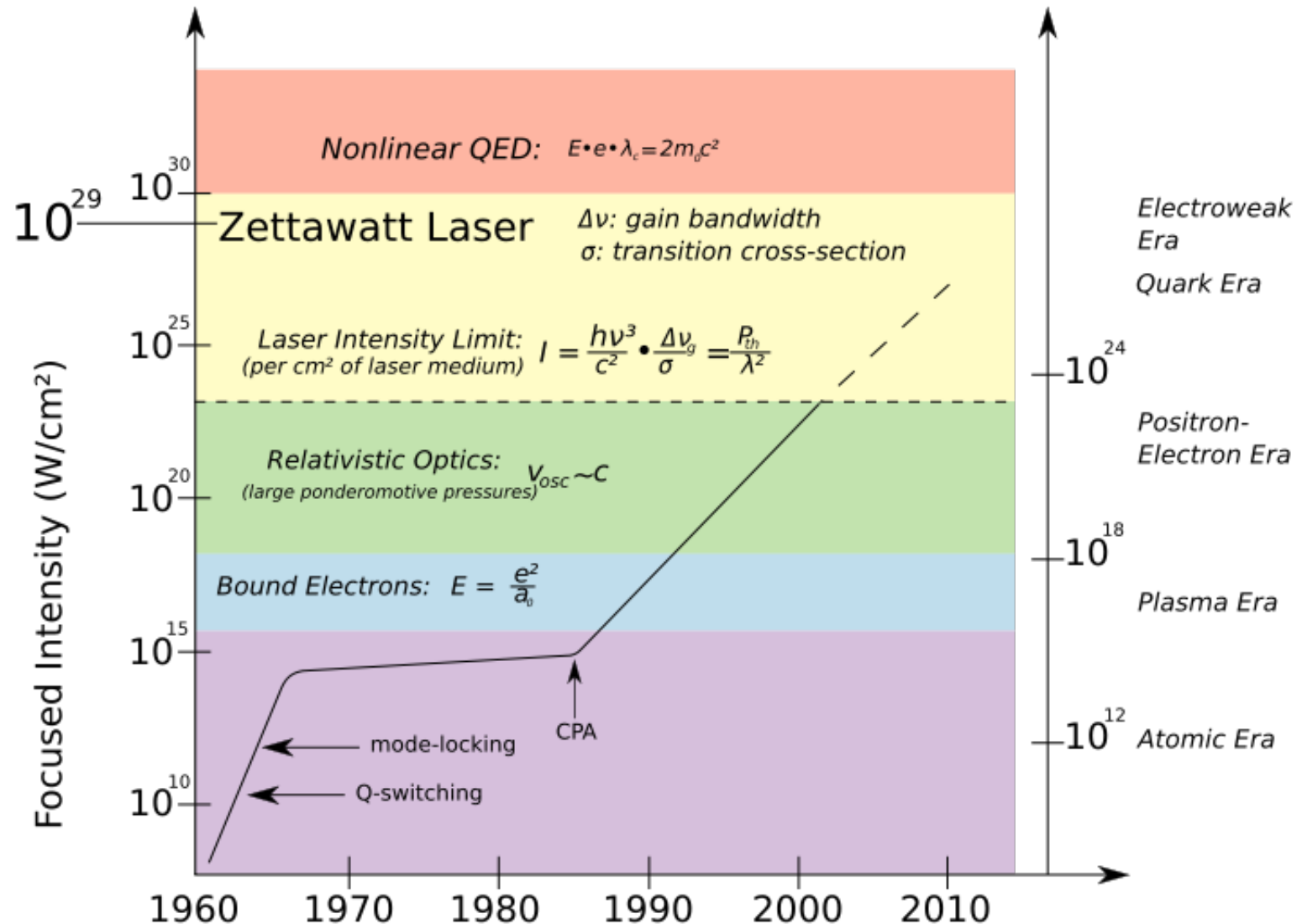


Figure 3. The concept of how chirped-pulse amplification and other new technologies enable the production of the petawatt (quadrillion-watt) pulses.





# Laser (pulse) power



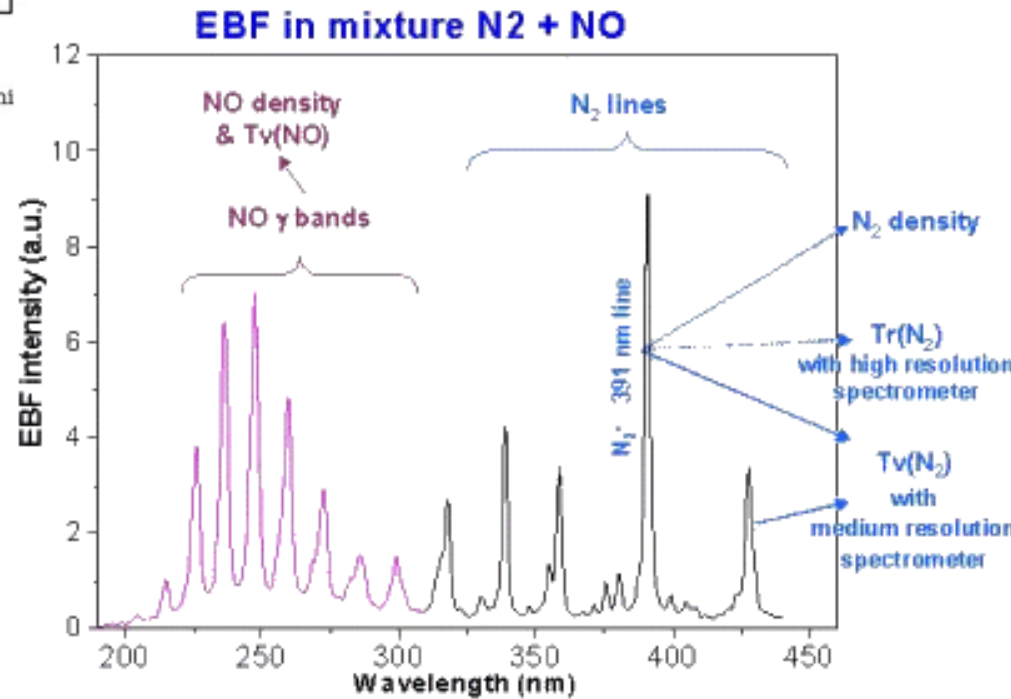
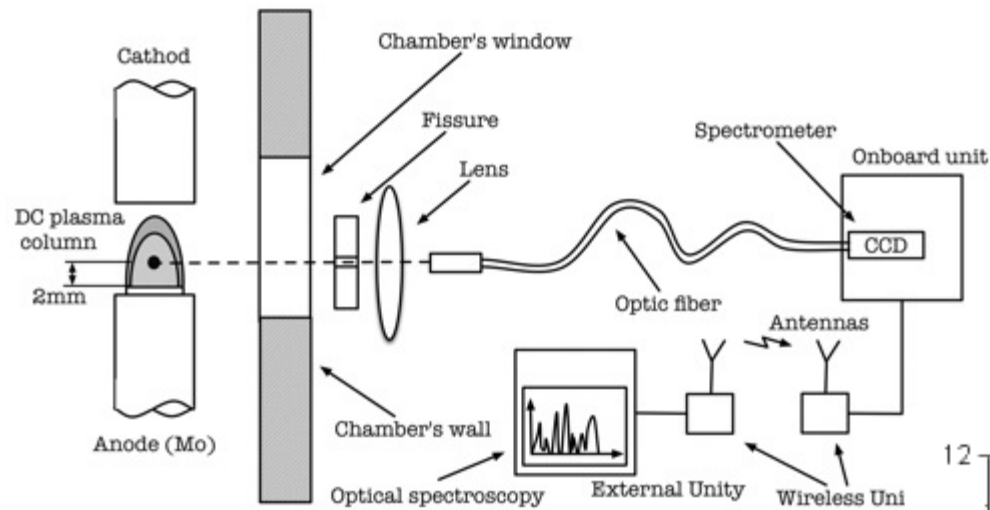
# SI-Präfixe

| Factor    | Name  | Symbol | Factor     | Name  | Symbol |
|-----------|-------|--------|------------|-------|--------|
| $10^1$    | deca  | da     | $10^{-1}$  | deci  | d      |
| $10^2$    | hecto | h      | $10^{-2}$  | centi | c      |
| $10^3$    | kilo  | k      | $10^{-3}$  | milli | m      |
| $10^6$    | mega  | M      | $10^{-6}$  | micro | $\mu$  |
| $10^9$    | giga  | G      | $10^{-9}$  | nano  | n      |
| $10^{12}$ | tera  | T      | $10^{-12}$ | pico  | p      |
| $10^{15}$ | peta  | P      | $10^{-15}$ | femto | f      |
| $10^{18}$ | exa   | E      | $10^{-18}$ | atto  | a      |
| $10^{21}$ | zetta | Z      | $10^{-21}$ | zepto | z      |
| $10^{24}$ | yotta | Y      | $10^{-24}$ | yocto | y      |

# Detection Techniques

- Optical Emission Spectroscopy (OES)
- Absorption techniques
- Photoacoustic Spectroscopy
- Laser induced fluorescence (LIF)
- Resonant Enhanced Multi Photon Ionisation (REMPI)

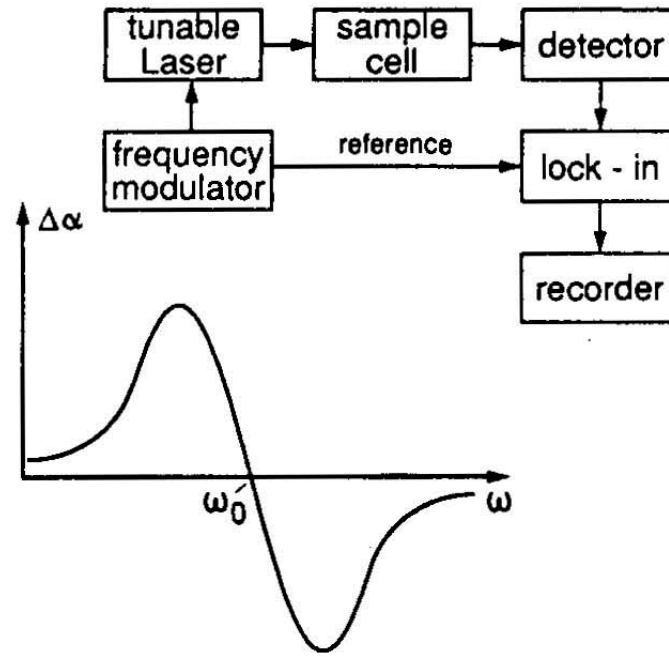
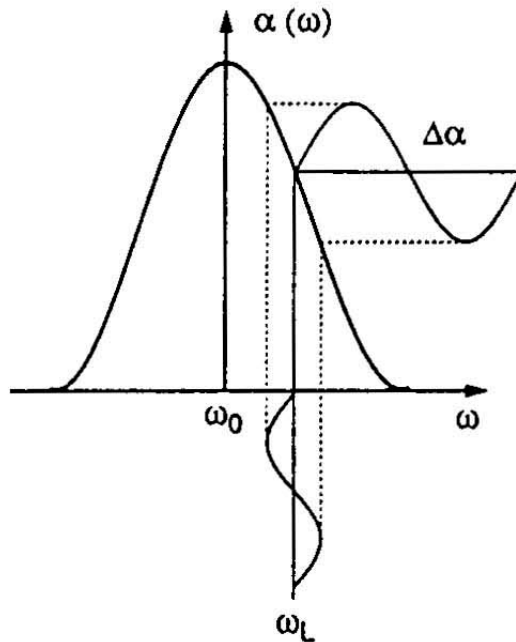
# OES: Optical Emission Spectroscopy



# Absorption Spectroscopy with a Frequency Modulated Laser

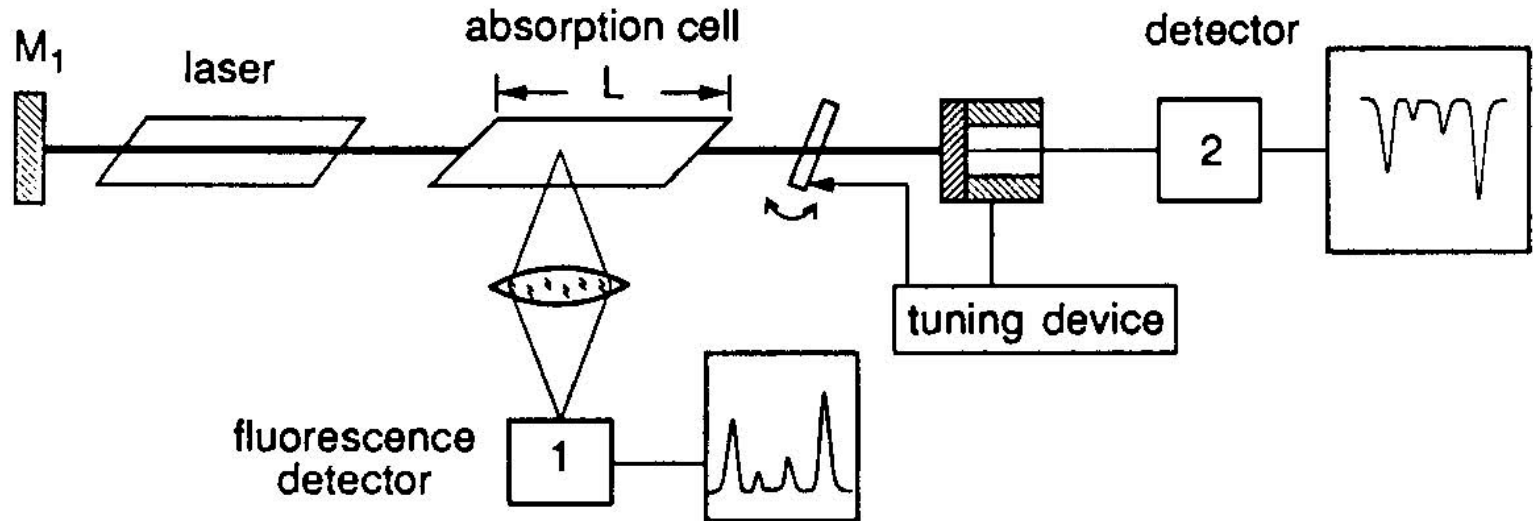
$$(I - I_0)/I_0 = \sigma N l = \text{Absorbance} \quad \text{Detection limit } A=10^{-3}$$

$$\sigma = 10^{-18} \text{ cm}^2 \quad l = 10 \text{ cm} \Rightarrow N = 10^{-3} / (10^{-18} \cdot 10) = 10^{14} \text{ molecules/cm}^3$$



Detection limit  $A=10^{-6}$

# Intracavity Absorption Technique



Operation close to laser threshold

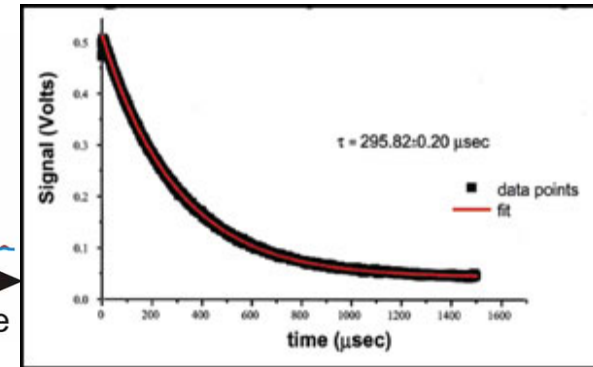
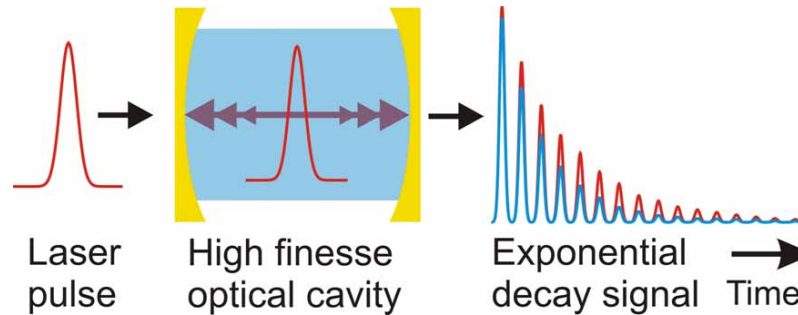
- + high sensitivity ( $A=10^{-8}$ )

- non linear response

- interference with other absorber within resonator

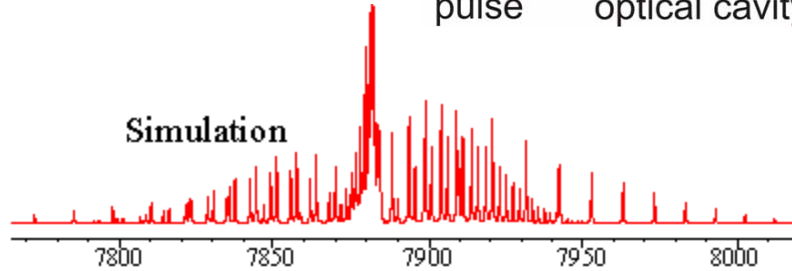
# CRD: Cavity Ring Down Spectroscopy

CRD spectroscopy is a highly sensitive direct absorption technique.

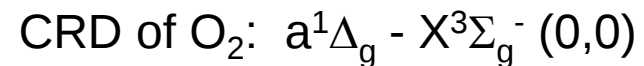
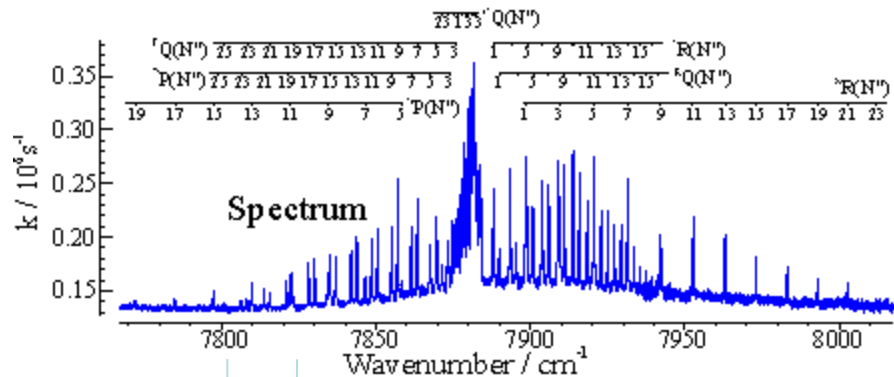


$$I = I_0 e^{-t/\tau} \rightarrow \text{absorption cross section}$$

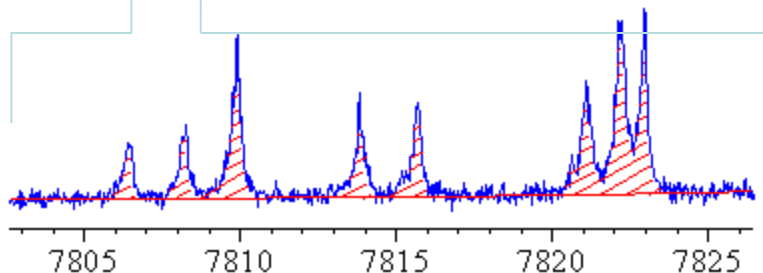
Simulation



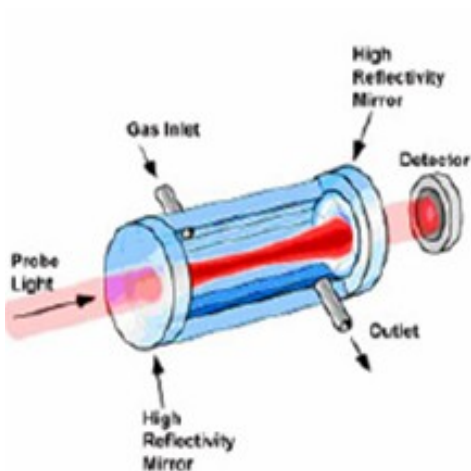
Spectrum



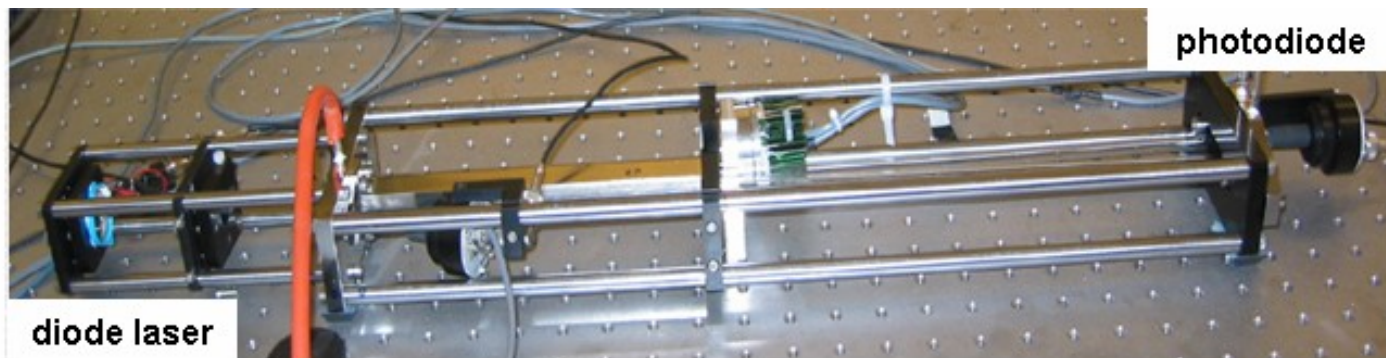
Integrated absorption → B → A → lifetime 0.2 ms



# CRD: Cavity Ring Down



Schematic drawing of the optical nose components (NIST)



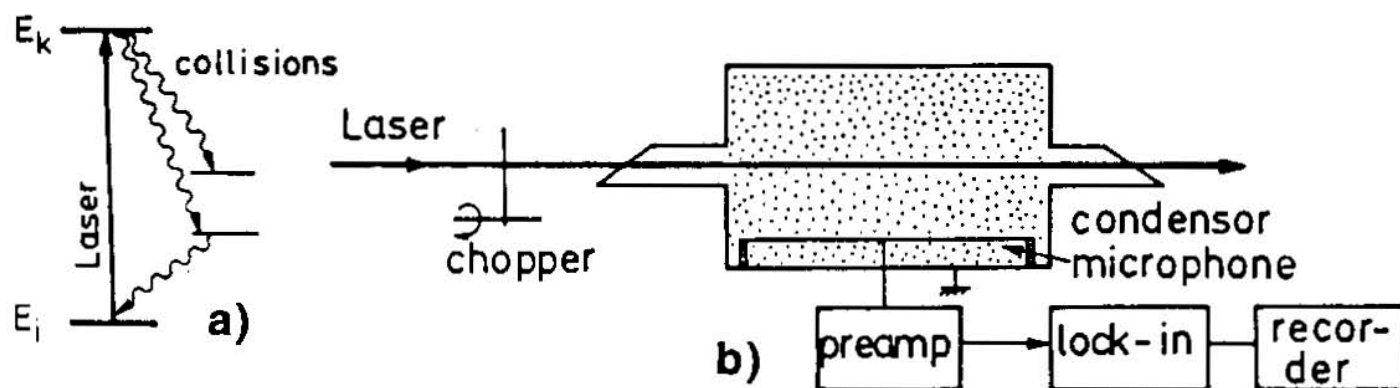
cavité

| Species                       | 1Hz detection limit [ppb] | $\lambda$ [nm] |
|-------------------------------|---------------------------|----------------|
| CO <sub>2</sub>               | 300                       | 1600           |
| CO                            | 300                       | 1566           |
| H <sub>2</sub> S              | 100                       | 1600           |
| C <sub>2</sub> H <sub>4</sub> | 50                        | 1620           |
| CH <sub>4</sub>               | 0.5                       | 1653           |
| NH <sub>3</sub>               | 2                         | 1530           |
| H <sub>2</sub> O              | 1                         | 1390           |
| HCl                           | 1                         | 1742           |
| HF                            | 0.1                       | 1297           |

Improvement:  $\frac{1}{(1-\text{Reflectivity of mirrors})}$

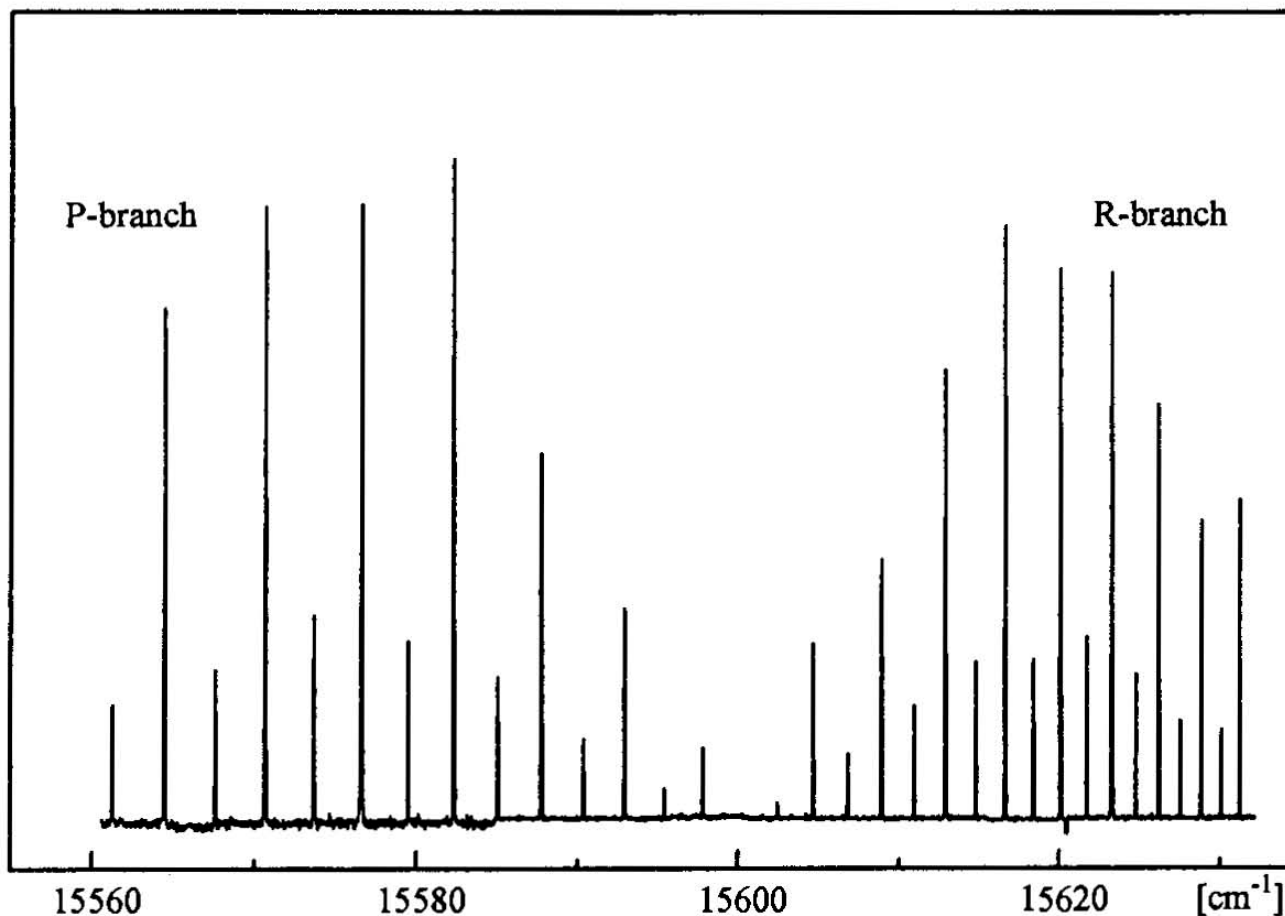
R=99.999%

# Photoacoustic Spectroscopy



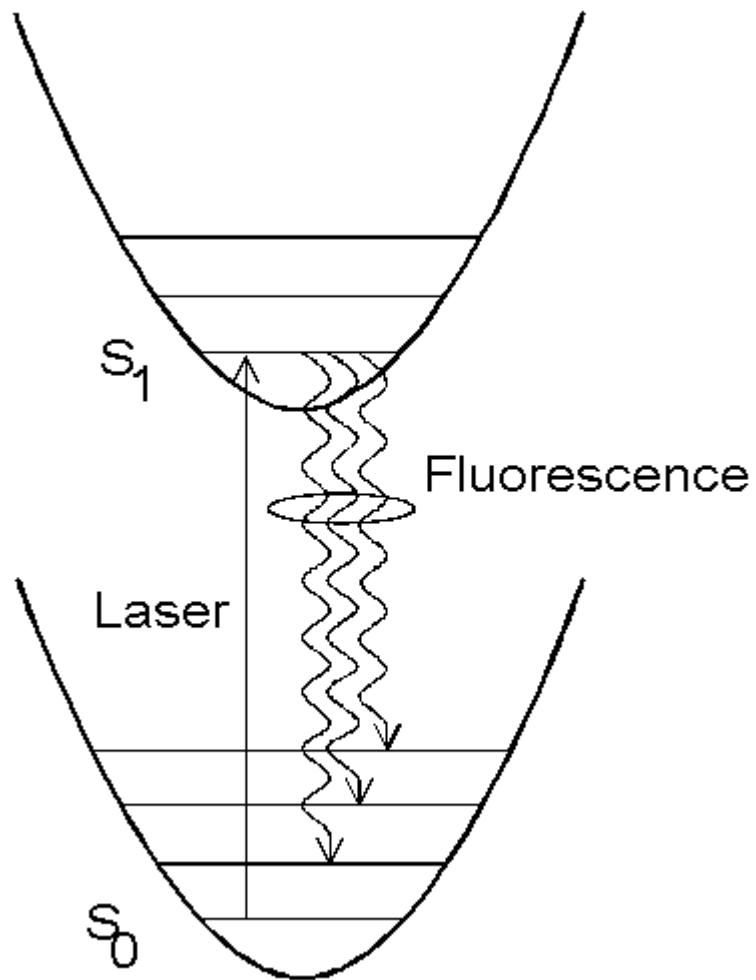
**Fig.6.13.** Photoacoustic spectroscopy (a) level scheme (b) schematic experimental arrangement

# Photoacoustic Spectroscopy: C<sub>2</sub>H<sub>2</sub>

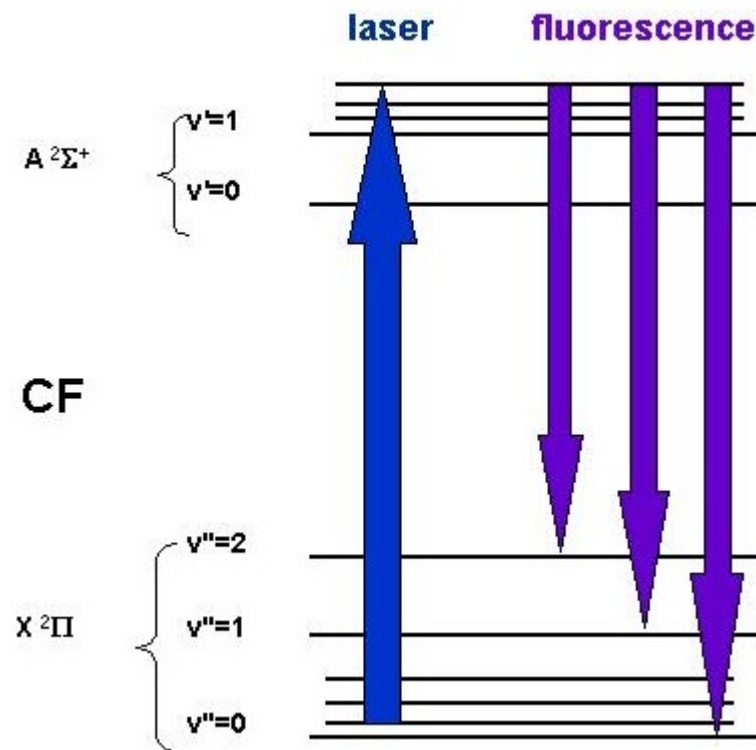


**Fig.6.15.** Optoacoustic overtone absorption spectrum of acetylene around  $\bar{\nu} = 15600$  cm<sup>-1</sup> corresponding to the excitation of a local mode by 5 quanta vibrations [6.45]

# Laser induced fluorescence (LIF)



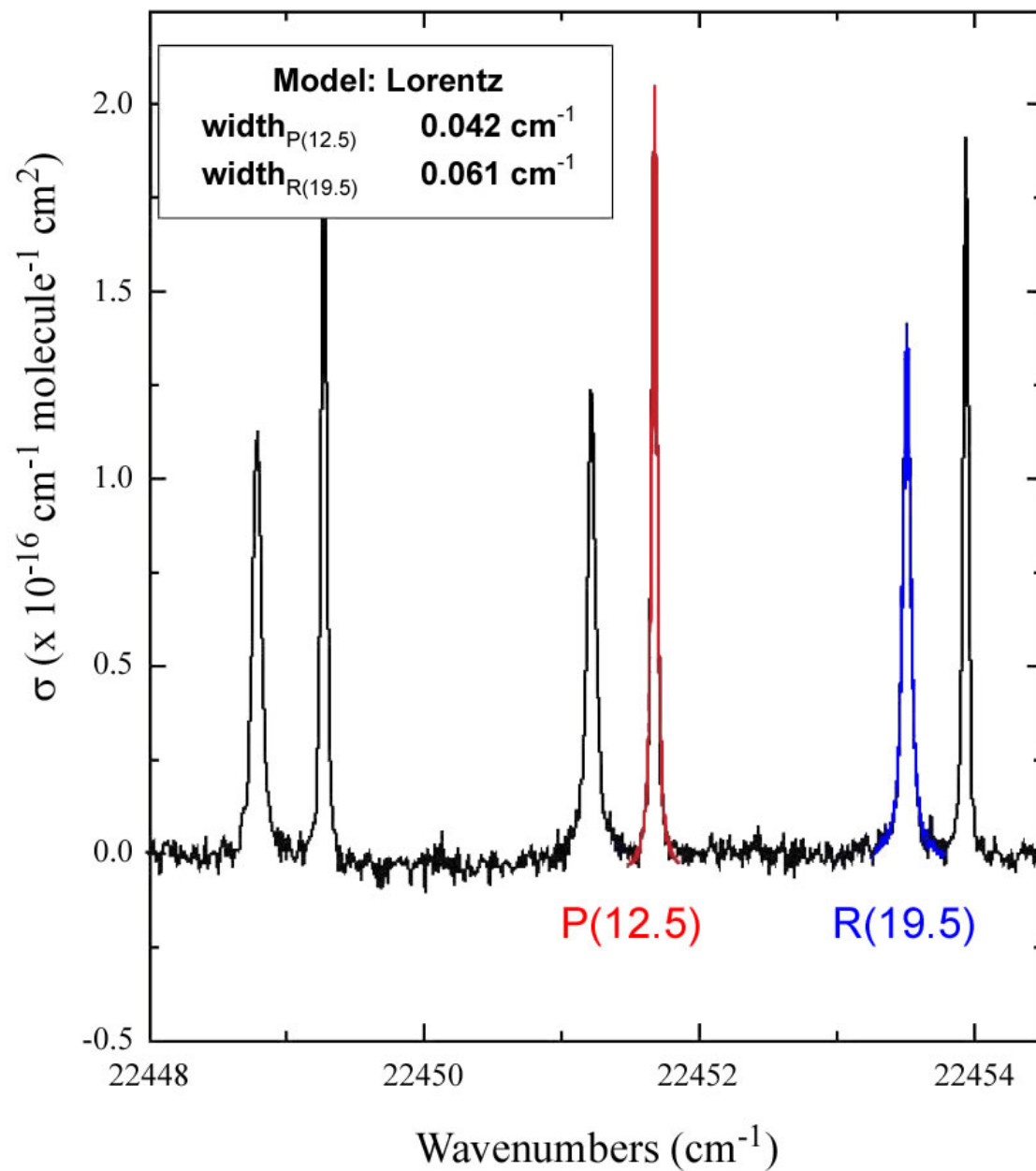
Energy Level Diagram of CF Radical



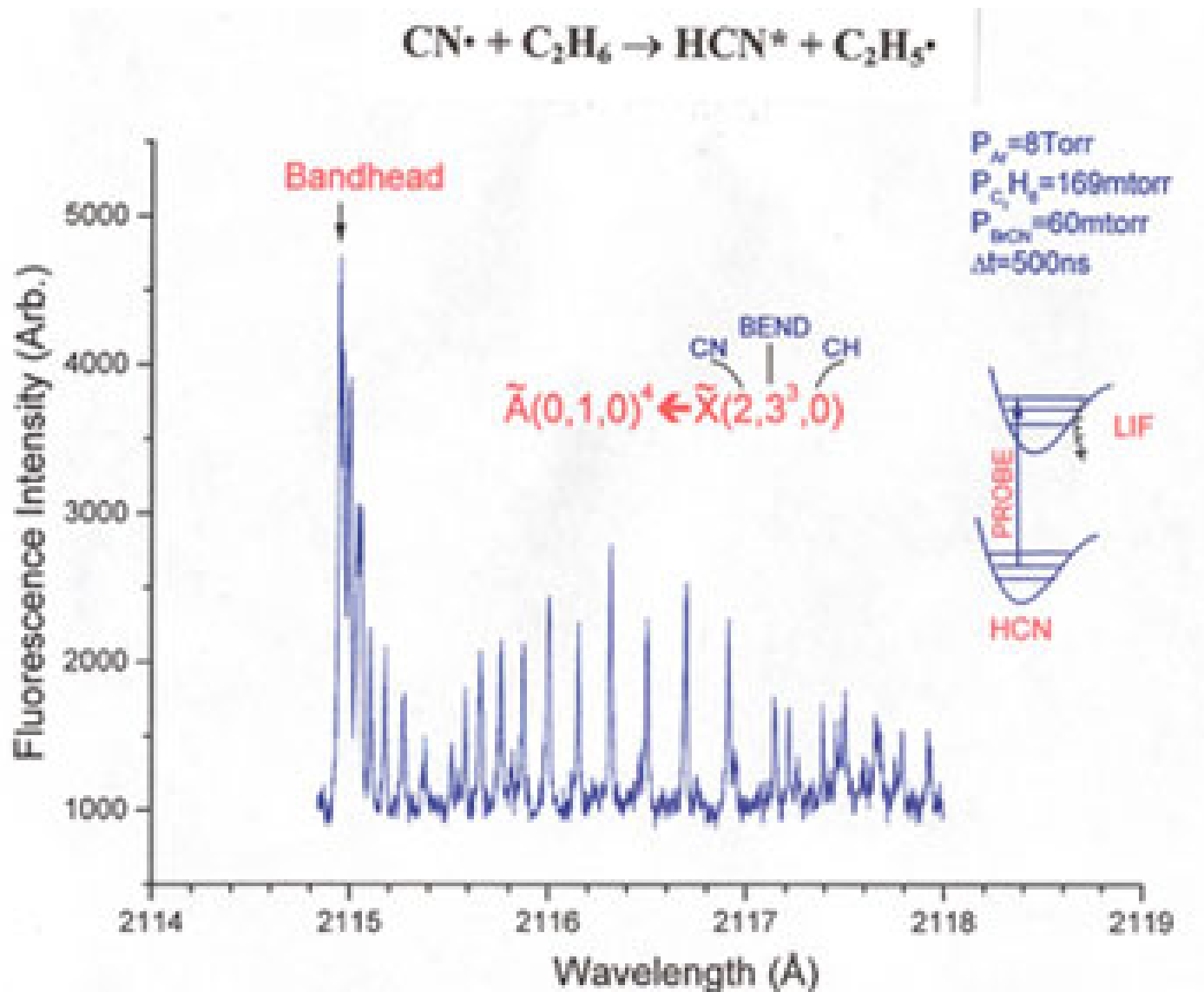
IO( $v'=2-v''=0$ ) around 445 nm

# LIF

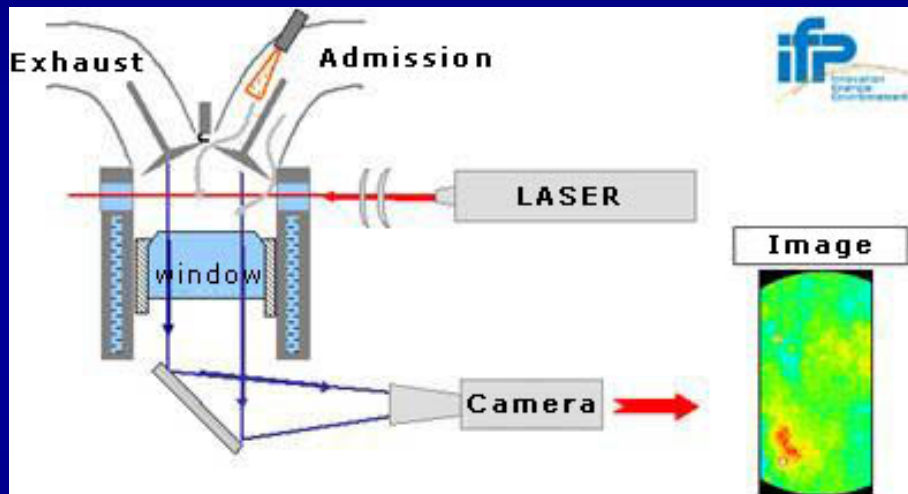
- + extremely sensitive
- + selective
- calibration
- handling
- costs



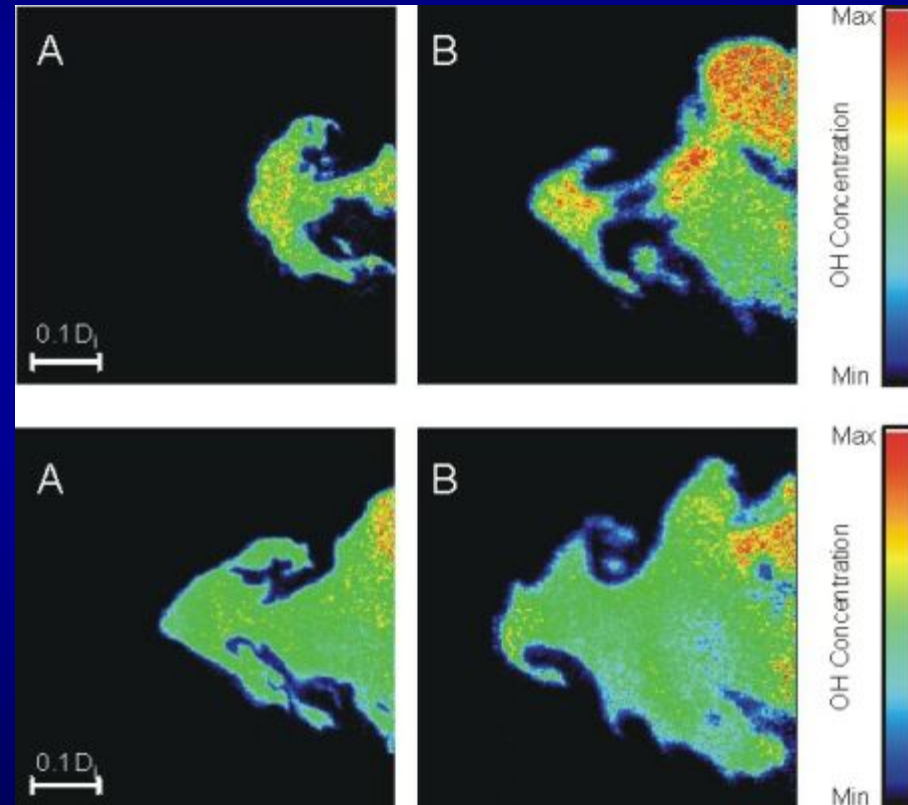
# Laser induced fluorescence (LIF)



# Laser induced fluorescence (LIF)



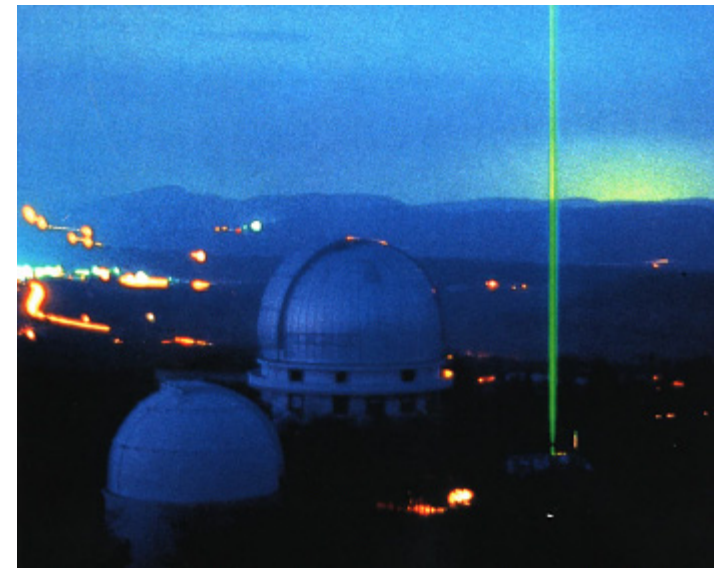
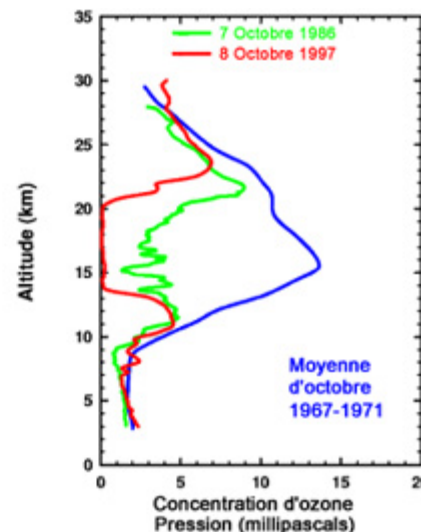
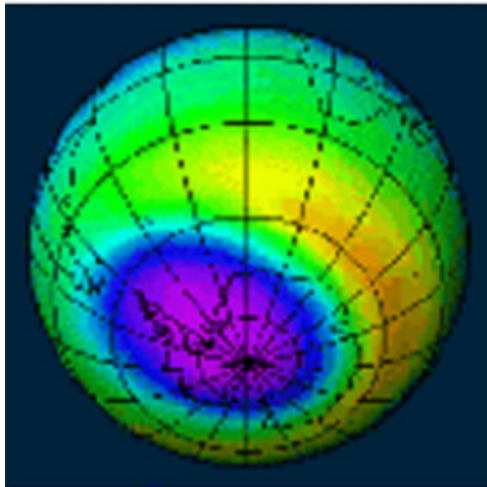
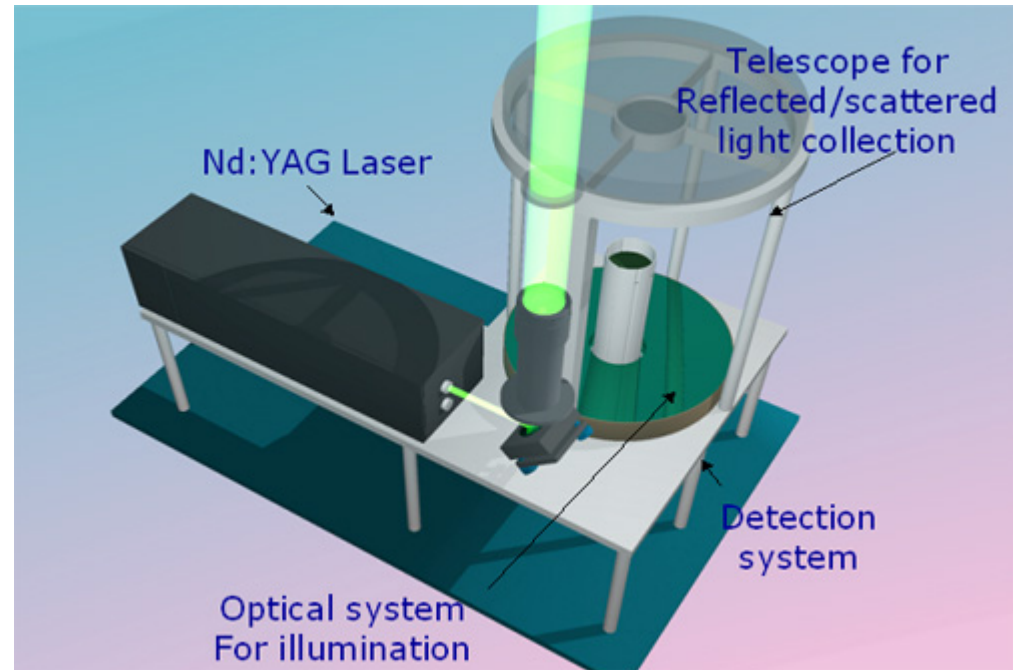
LIF in a running engine of a car



# LIDAR: Light Detection And Ranging

LIDAR: A remote-sensing technique that uses a laser light source to probe the characteristics of a target:

- Atmosphere control
  - Density
  - Temperature
  - Wind
  - Pollution
- Distance, speed measurement
- Rayleigh, Mie scattering
- Raman scattering
- Fluorescence
- Doppler shift



# Laser Induced Fluorescence: Na<sub>2</sub>

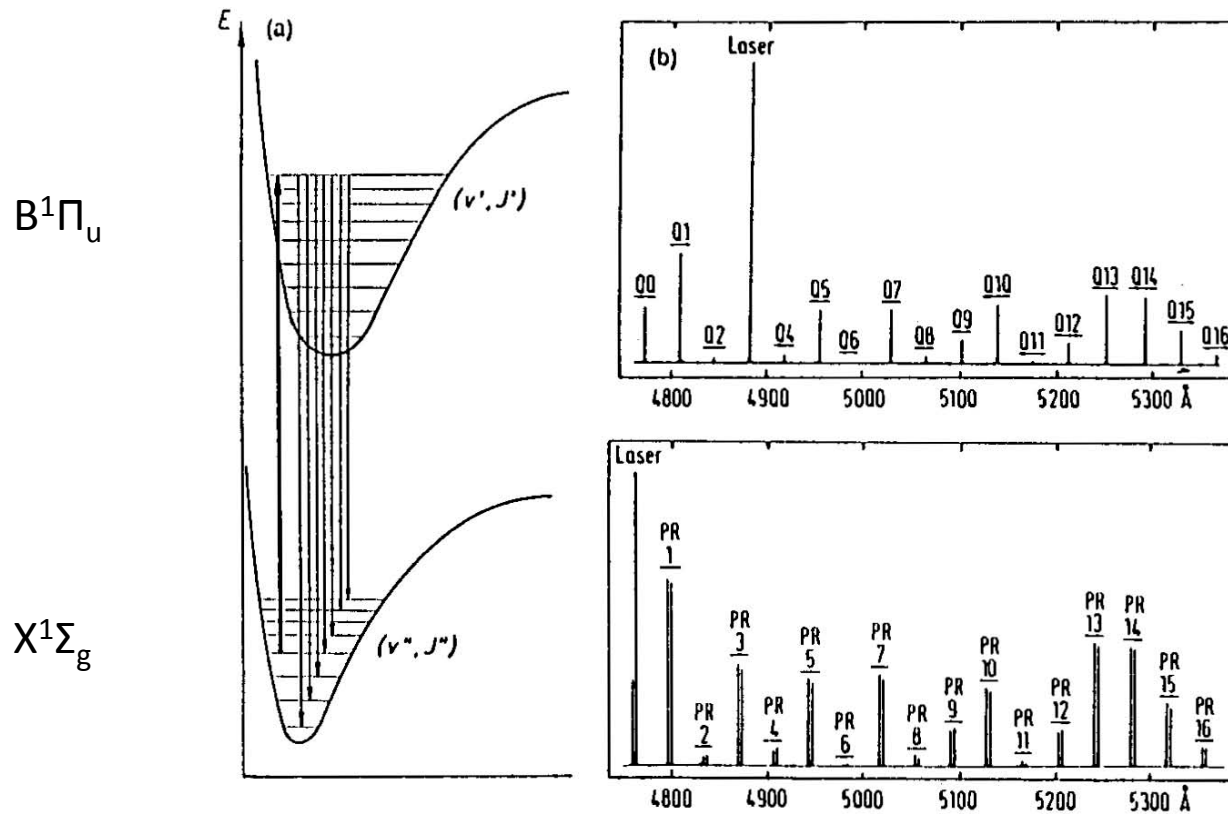
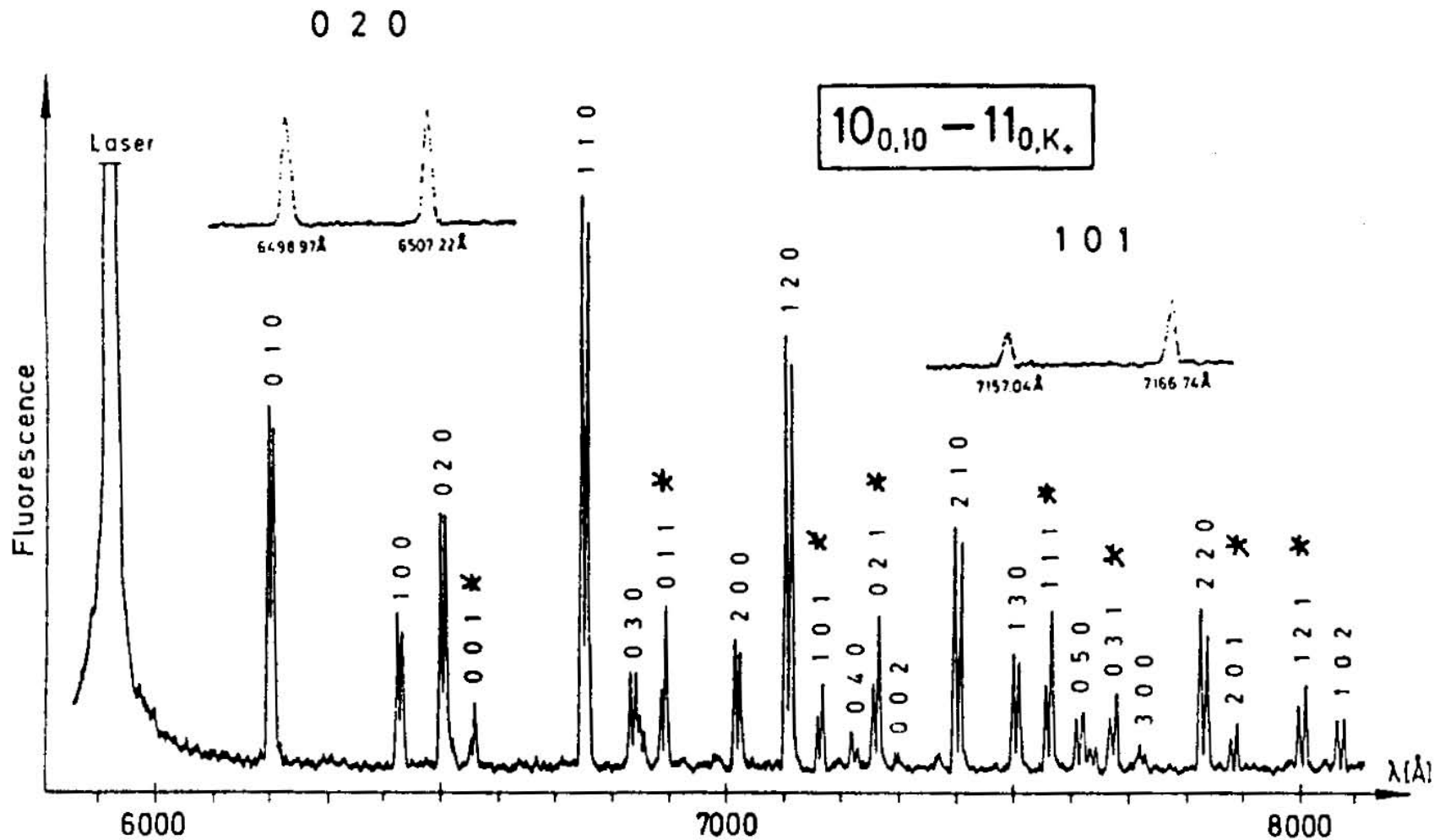


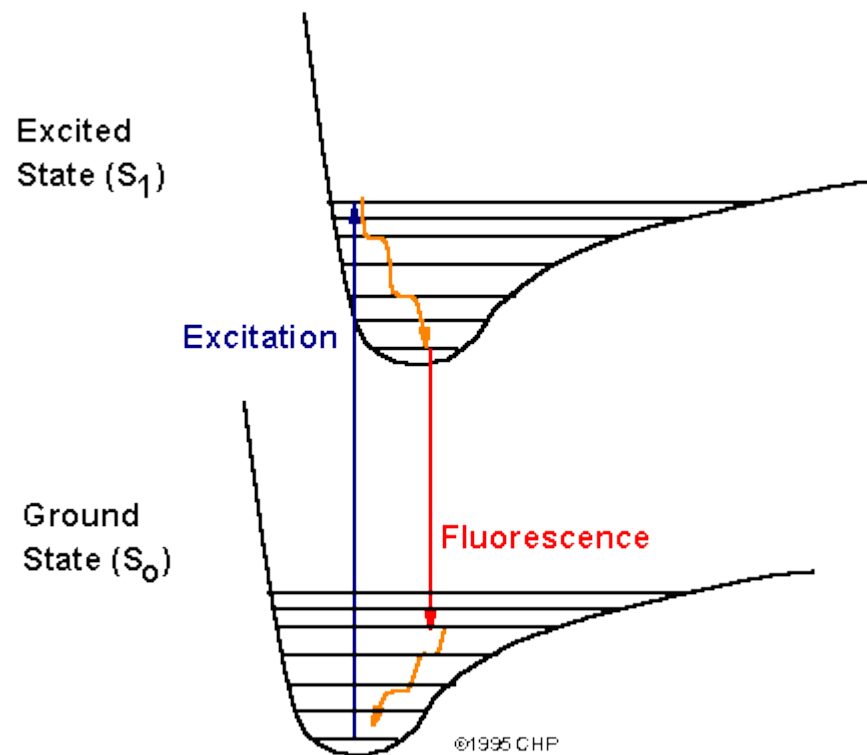
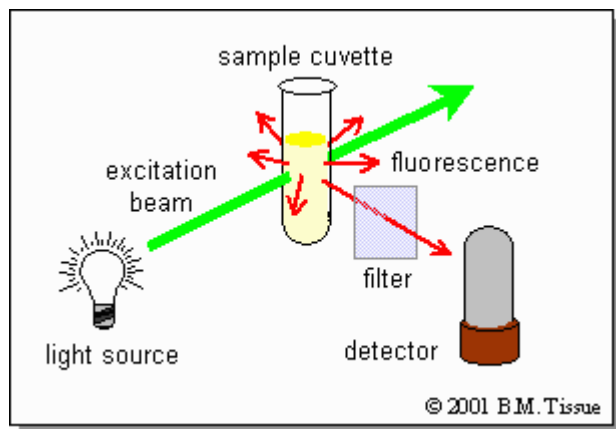
Fig.6.34. Laser-induced fluorescence of the Na<sub>2</sub> molecule excited by argon laser lines (a) term diagram (b) fluorescence lines with  $\Delta J = 0$  (Q-lines) emitted from the upper level ( $v'=3, J'=43$ ) of the  $B^1\Pi_u$  state, excited at  $\lambda = 488$  nm. (c) P and R doublets, emitted from the upper level ( $v'=6, J'=27$ )

Advantage: very high selectivity. 488 nm line excites a positive  $\Lambda$  component of the  $v' = 6, J' = 43$  which emits only Q lines. 476,5 nm line excites a negative  $\Lambda$  component of the  $v' = 6, J' = 27$  level which emits P and R lines.

# Laser Induced Fluorescence: NO<sub>2</sub>

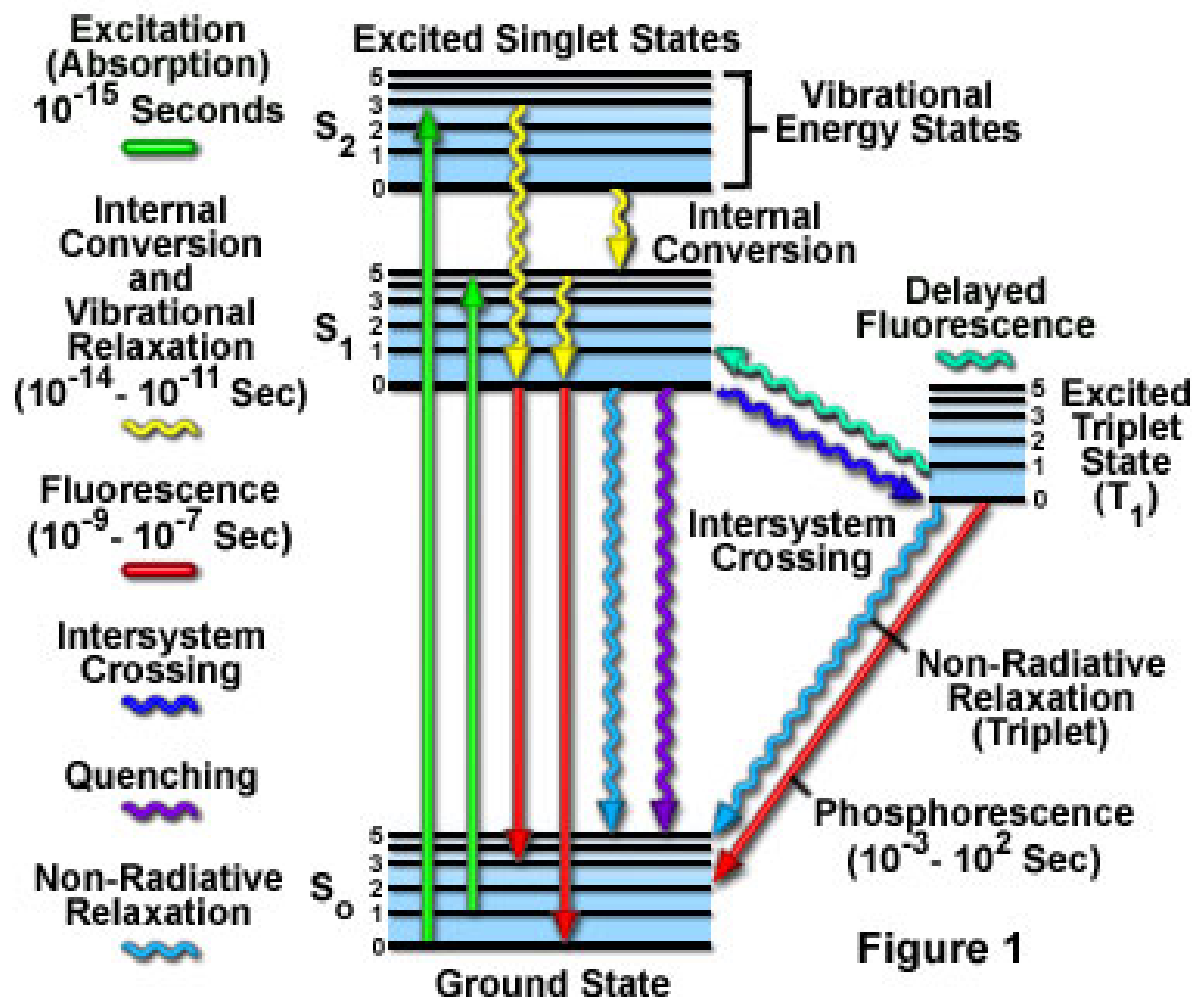


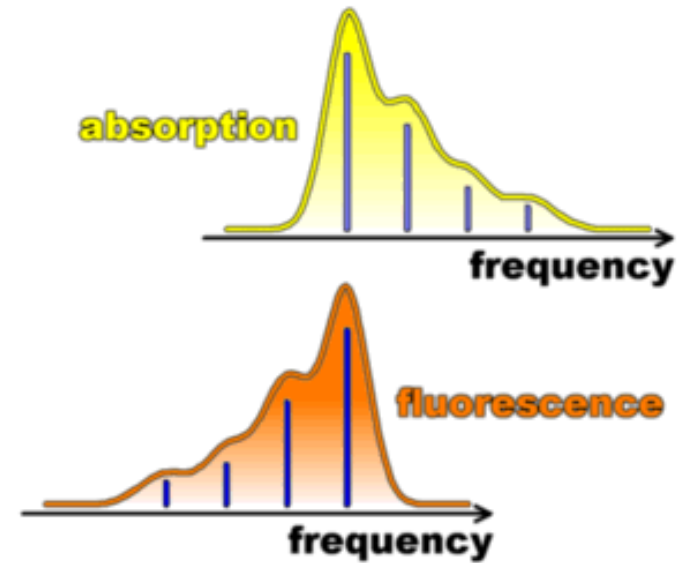
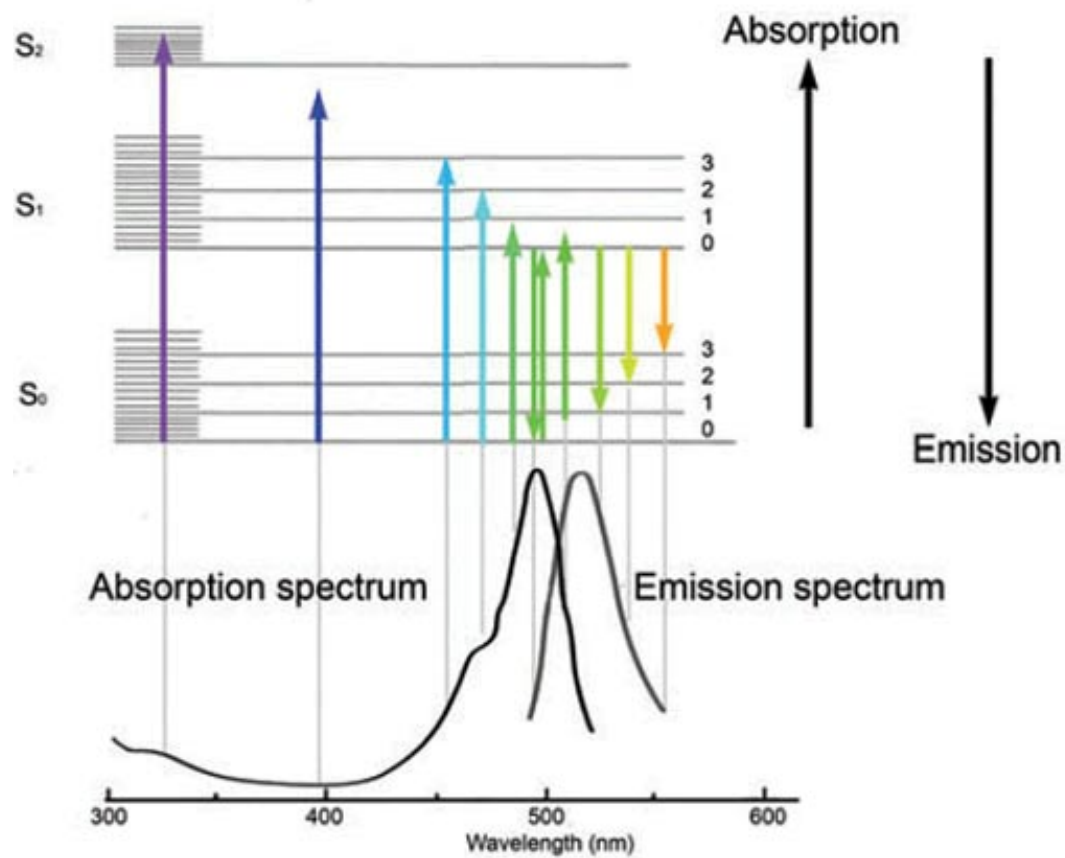
# Molecular Fluorescence Spectroscopy



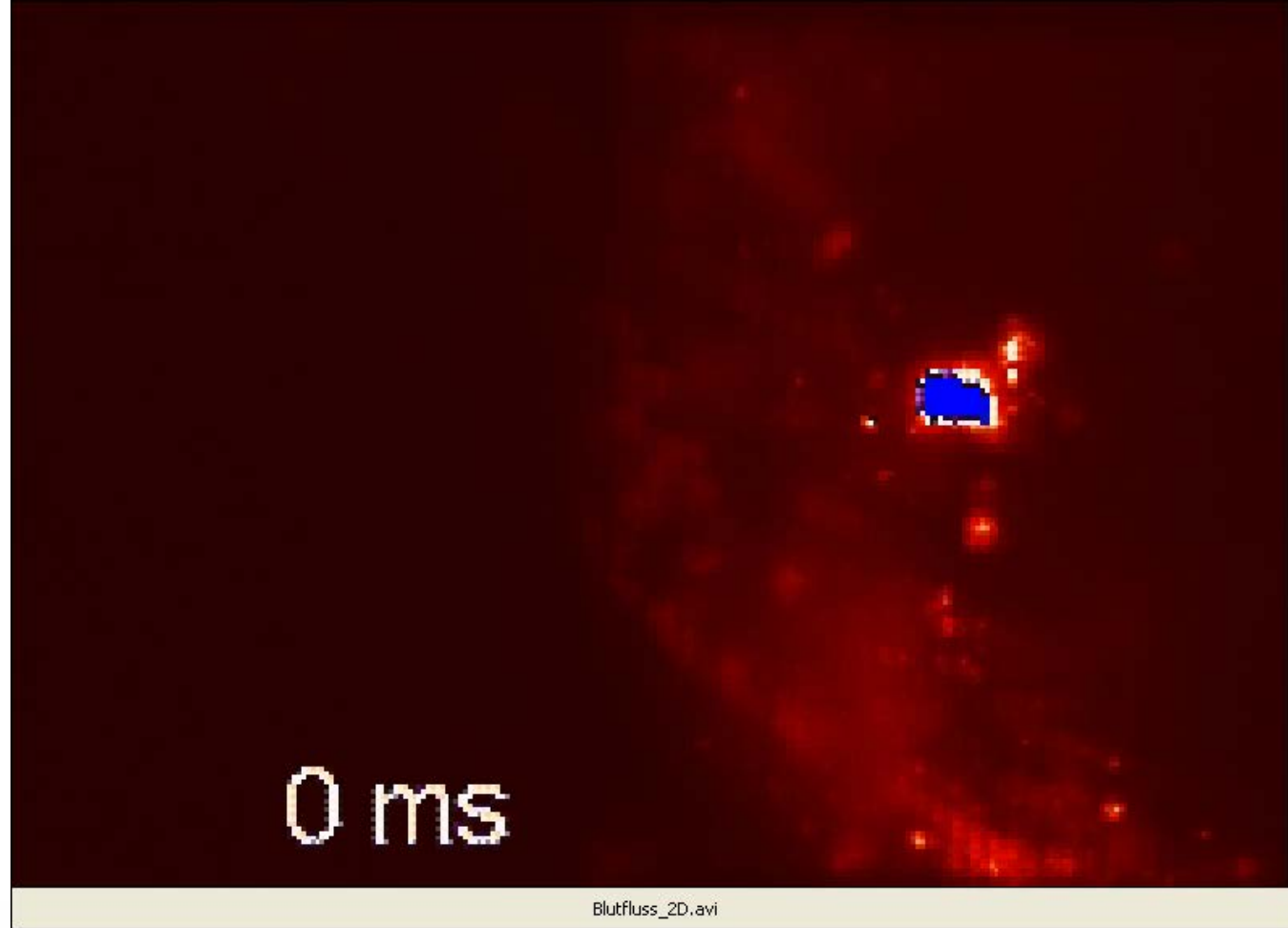
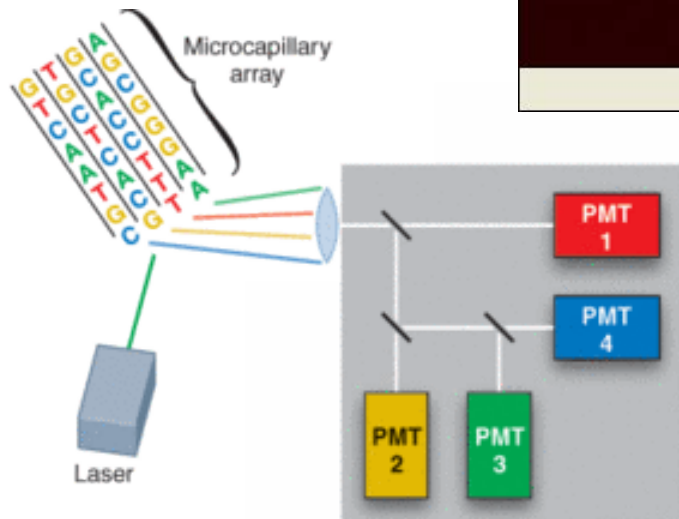
# Jablonski Diagram

Jablonski Energy Diagram

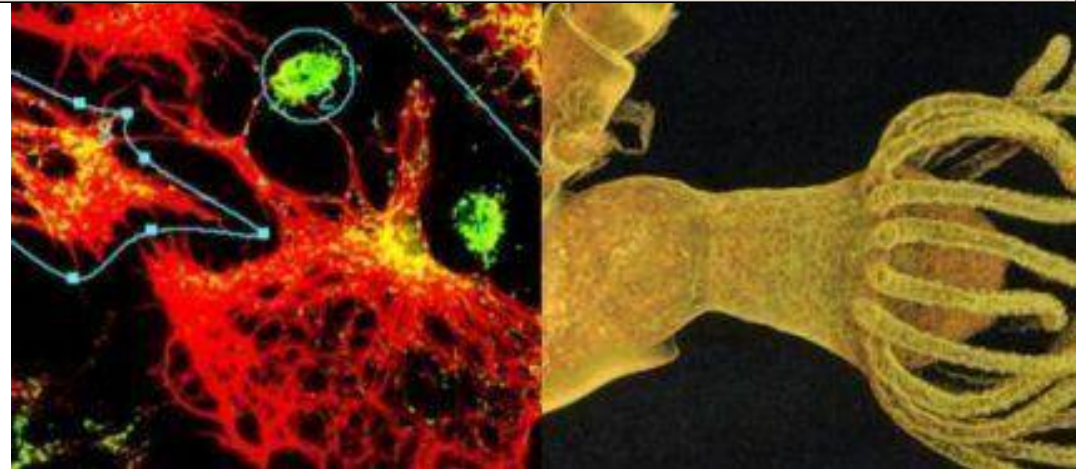




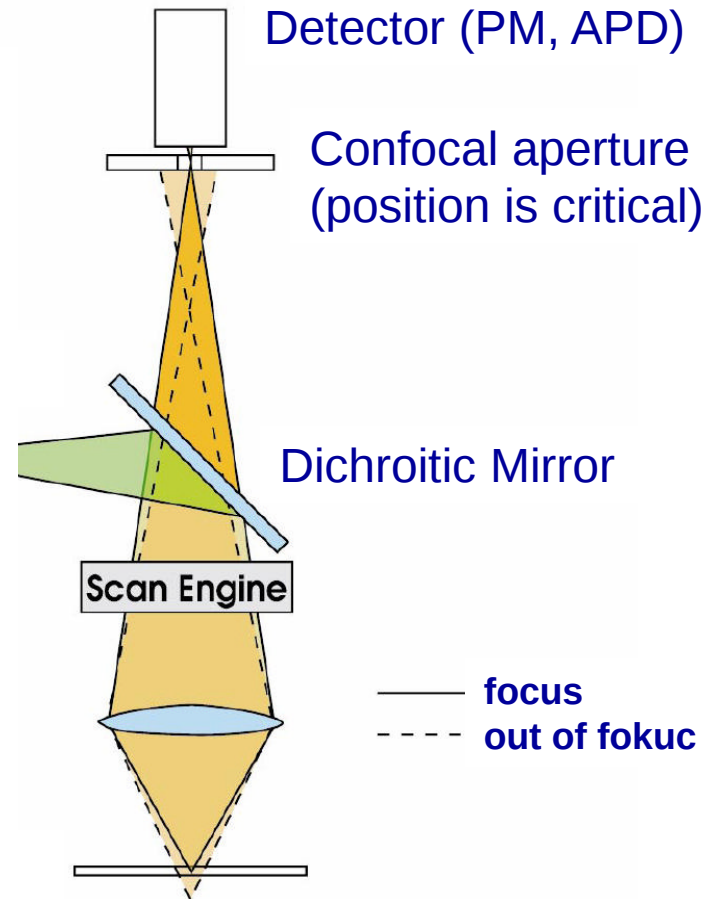
# Modern Microscopy is LIF



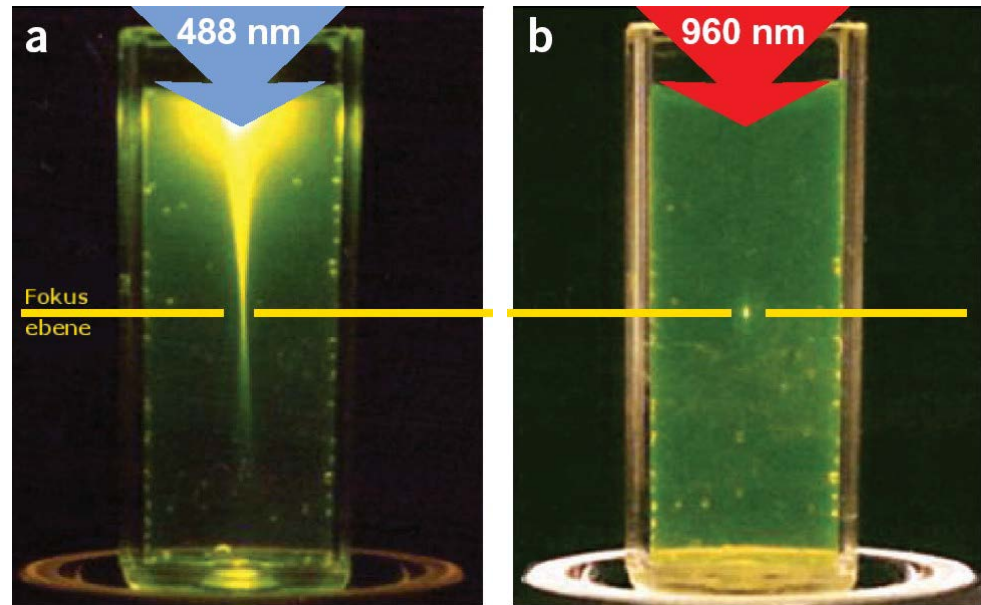
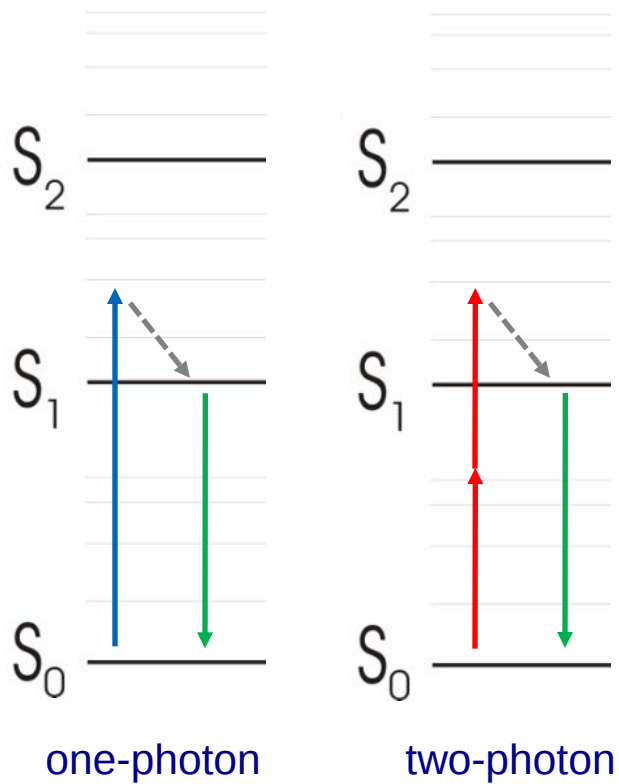
Blutfluss\_2D.avi



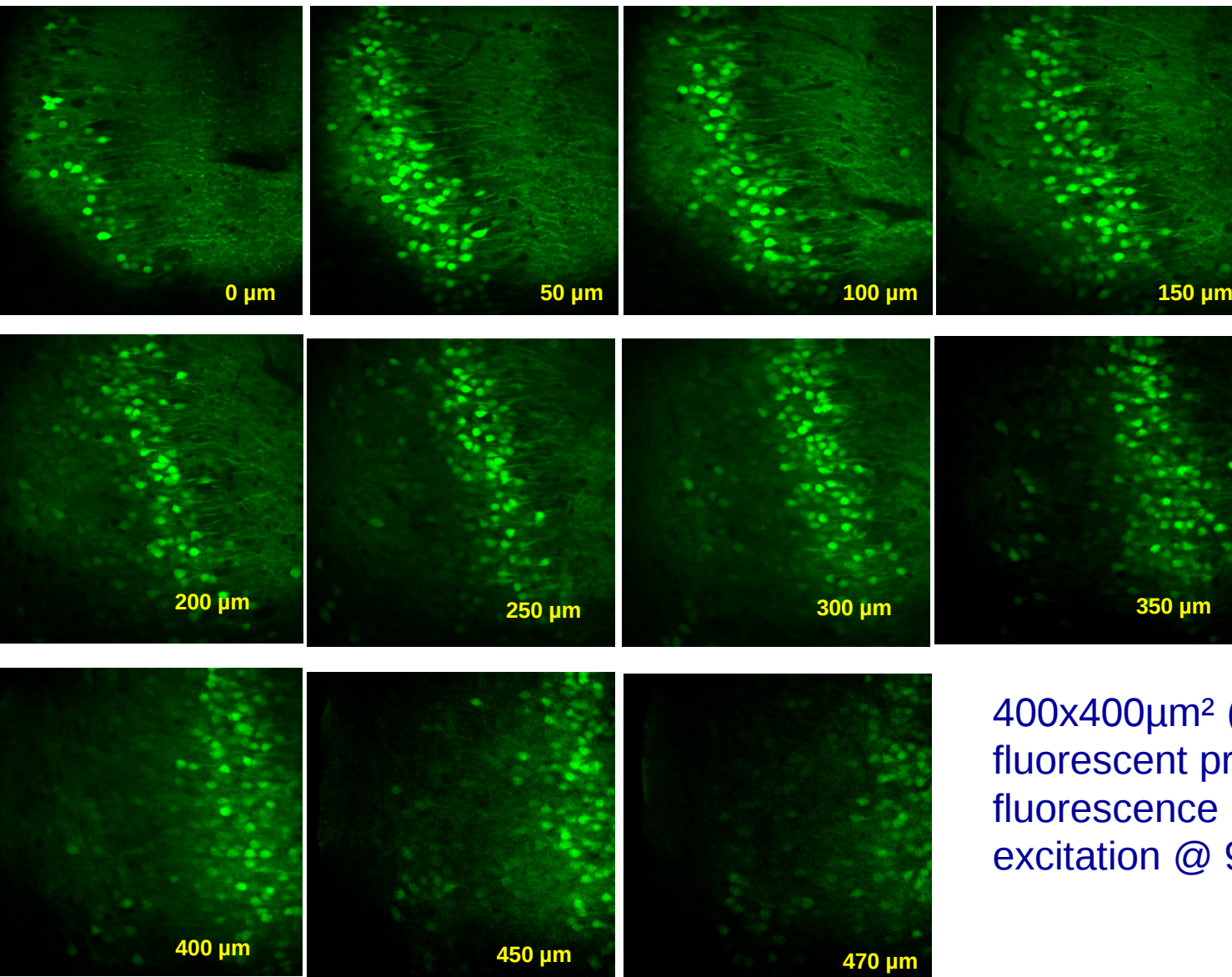
# Confocal Microscope



# one-photon vs. two-photon excitation

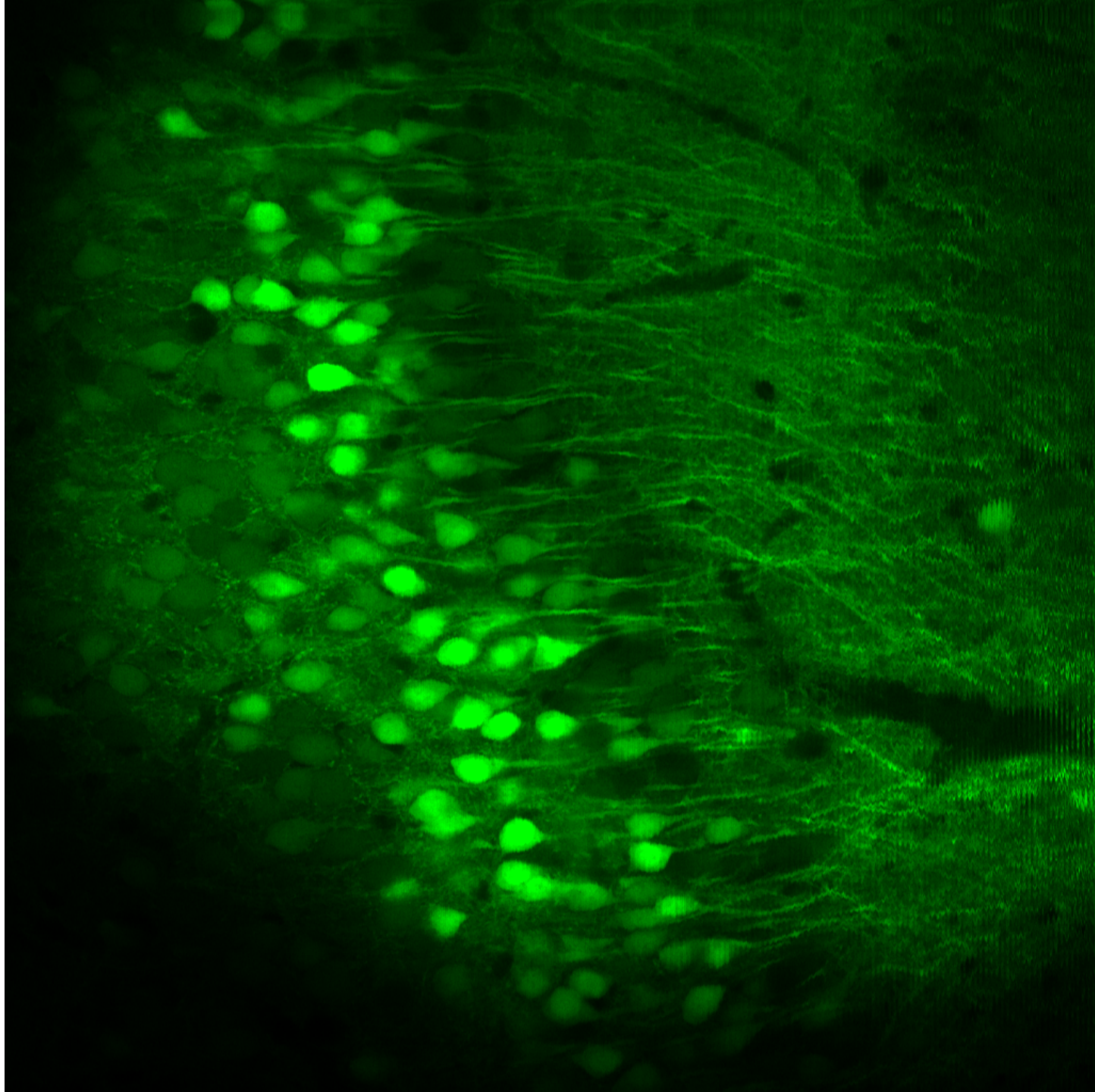


# Inside the brain of a mouse...



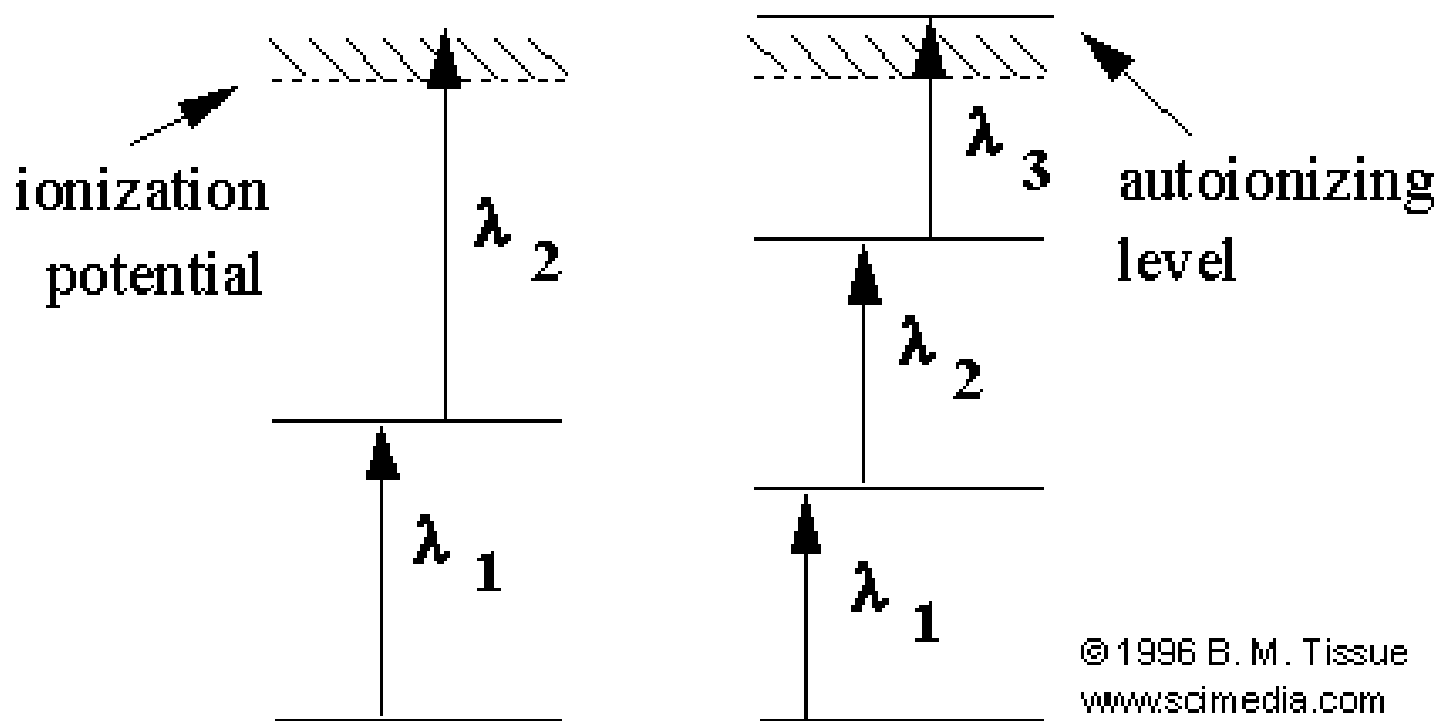
400x400 $\mu\text{m}^2$  (enhanced yellow  
fluorescent protein EYFP):  
fluorescence max. @ 535nm;  
excitation @ 920nm

**In  
3D...**



# Ionization Spectroscopy

Absorption of photons on the molecular transition  $E_i \rightarrow E_k$  is monitored by detection of the ions or electrons, produced by some means from the molecular excited state  $E_k$ . The ionization of the excited molecule may be performed by photons, by collisions, or by an external electric, or magnetic field.

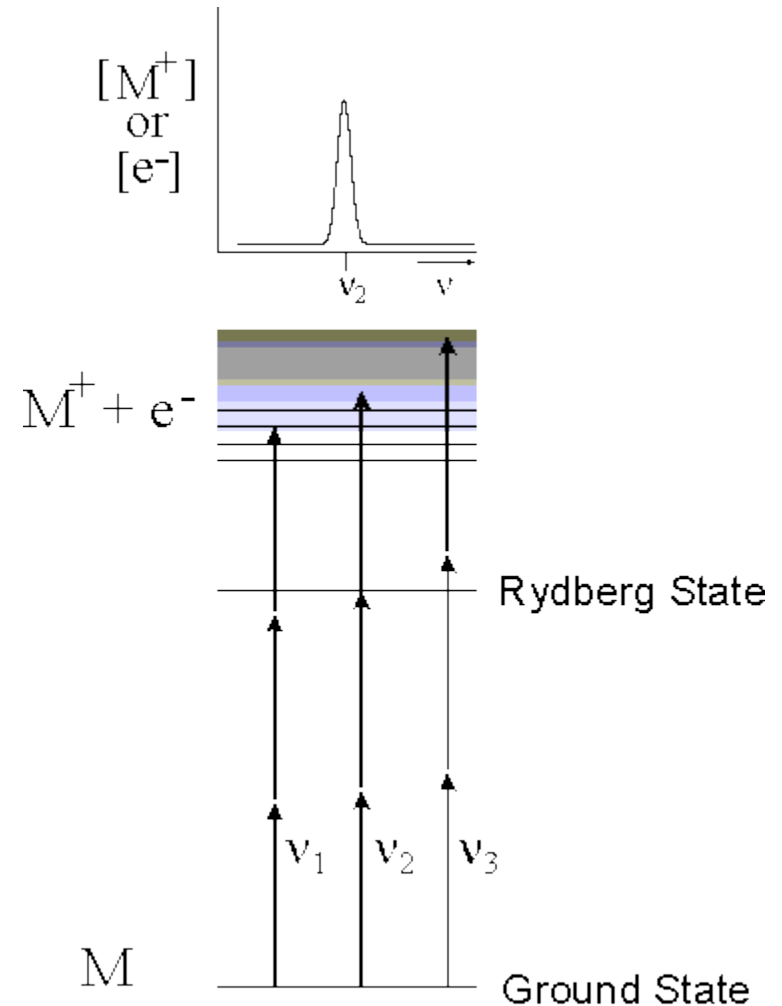


The ionization methods used in molecular spectroscopy and particularly, for determination of the internal-state distribution in reaction products of chemical reactions are in general called resonance-enhanced multiphoton ionization (**REMPI**).

# REMPI:

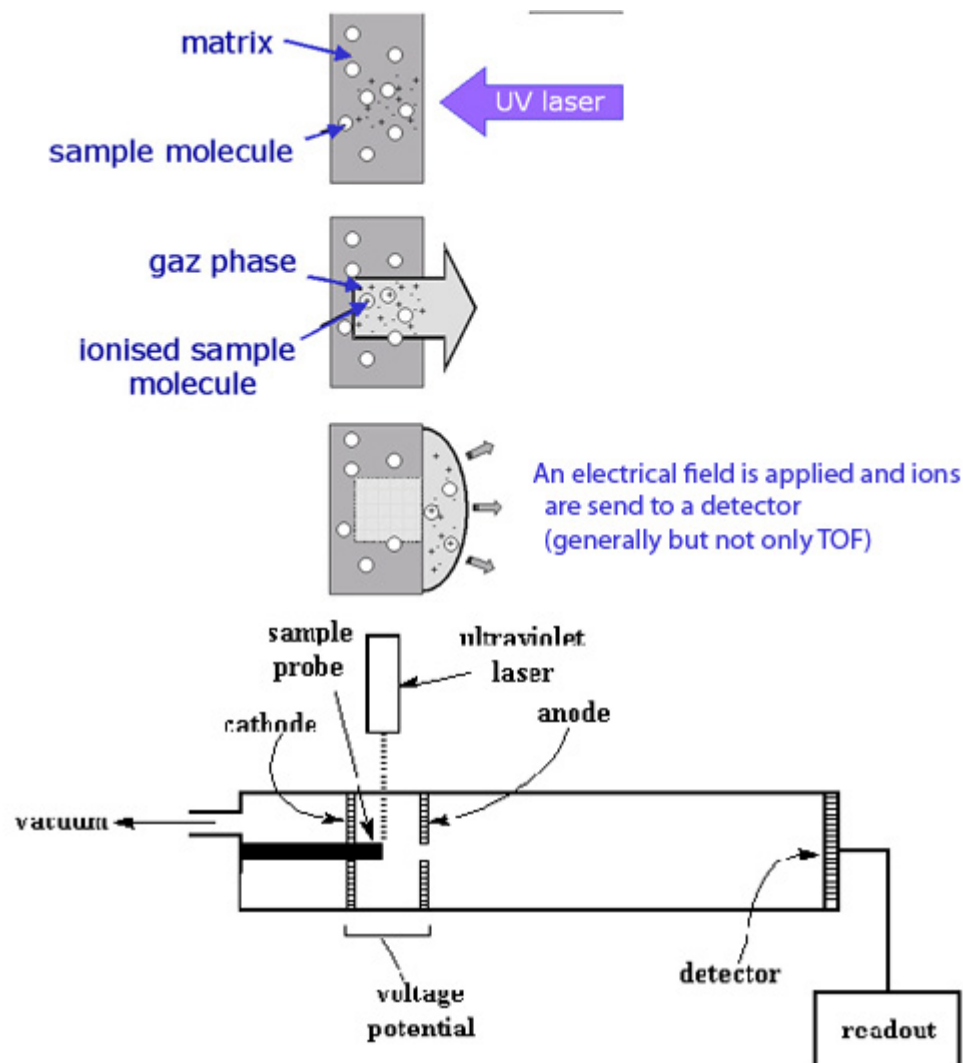
## Resonant Enhanced Multi-Photon Ionisation

REMPI involves a resonant single or multiple photon absorption to an electronically excited intermediate state followed by another photon which ionizes the atom or molecule.



# MALDI: Matrix Assisted Laser Desorption/Ionisation

A time of flight spectrometry technique, allowing the analysis of biomolecules and large organic molecules



A simplified diagram of a MALDI apparatus  
(After Creel, H., *Trends in Polym. Sci.*, 1993, 1(11), 336-342.)

**AND MUCH MORE TECHNIQUES.....**

**RAMAN**

**SERS**

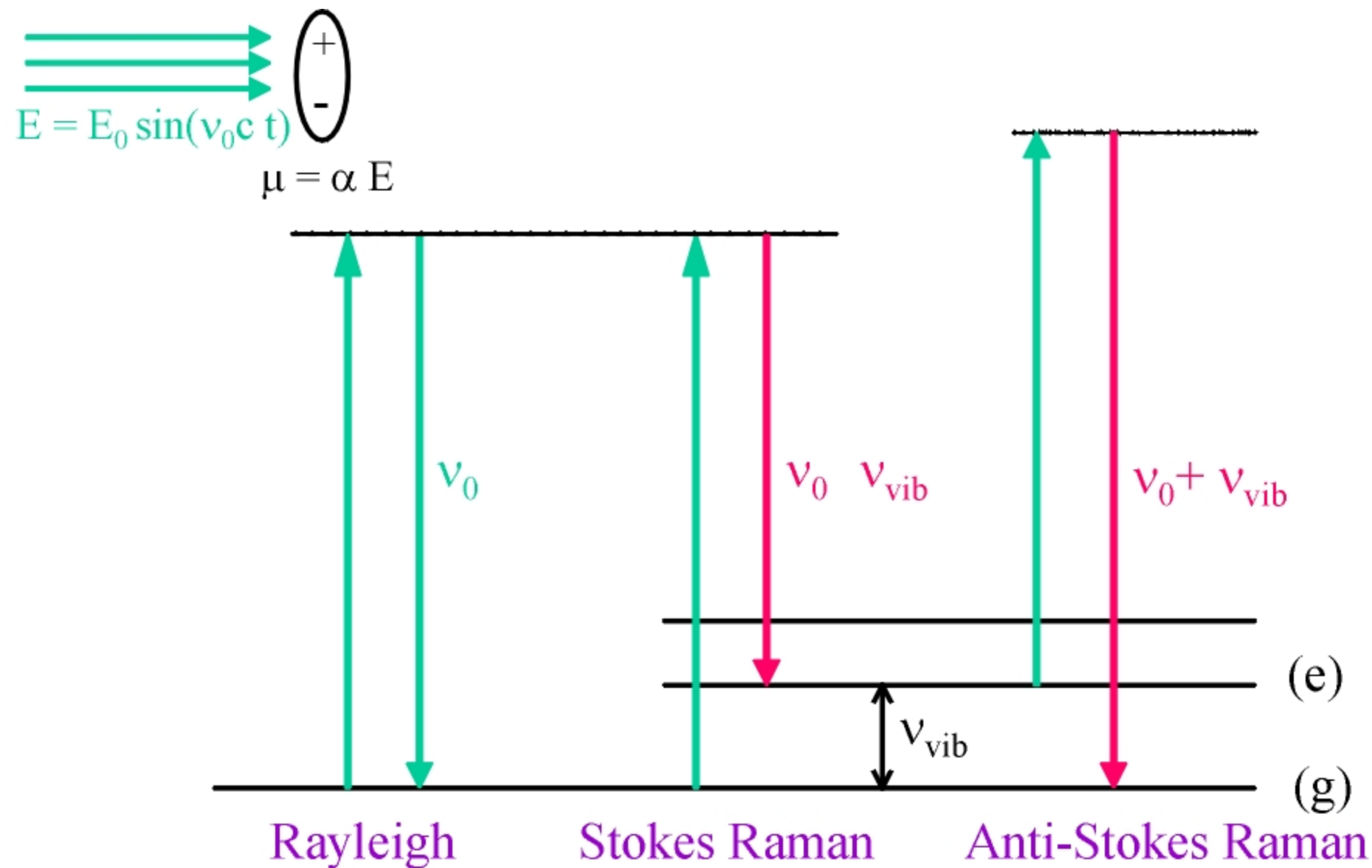
**CARS**

**FLUORESCENCE LIFETIME**

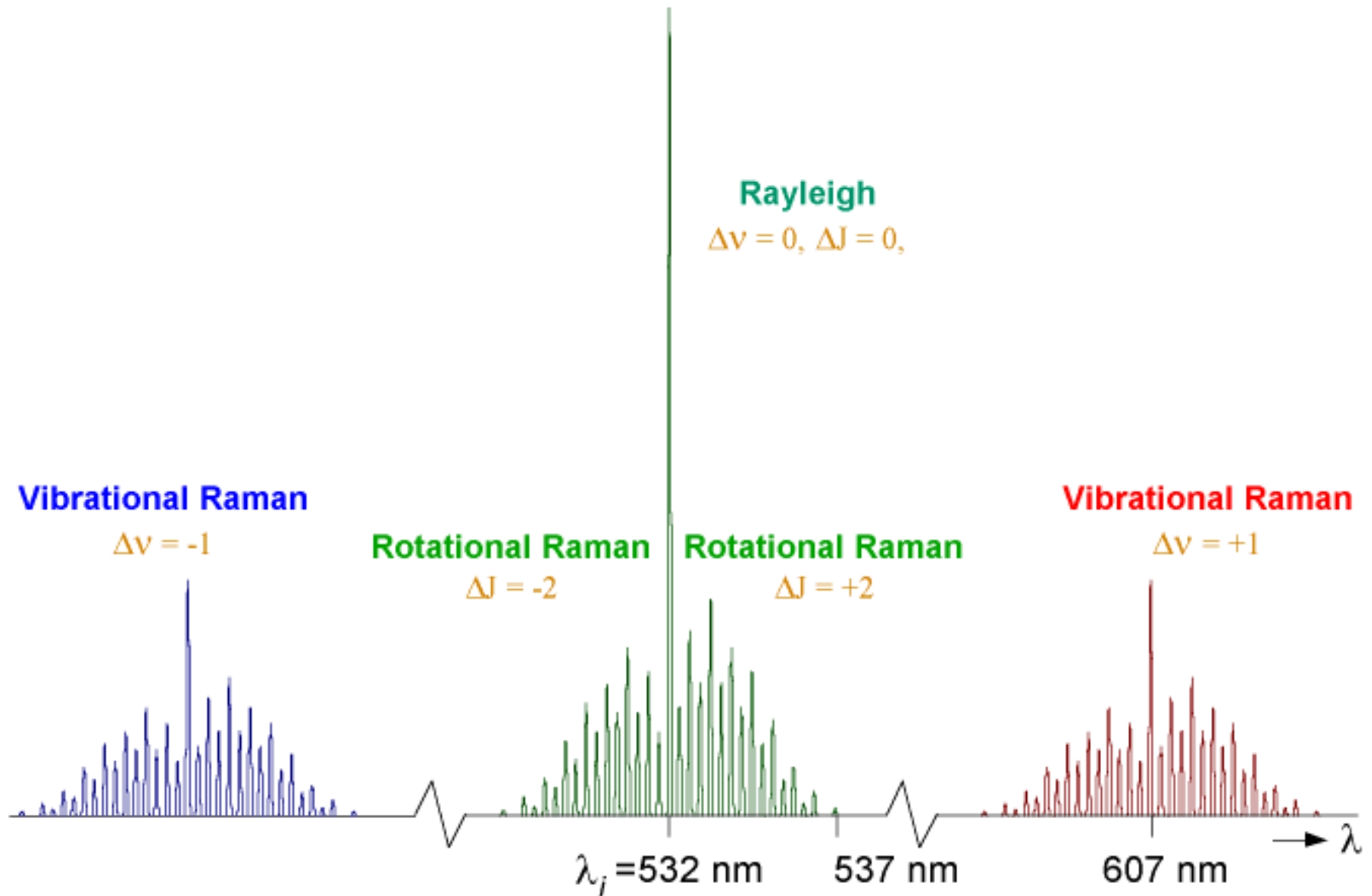
**FLUORESCENCE POLARISATION**

**HETERODYNE**

# Raman



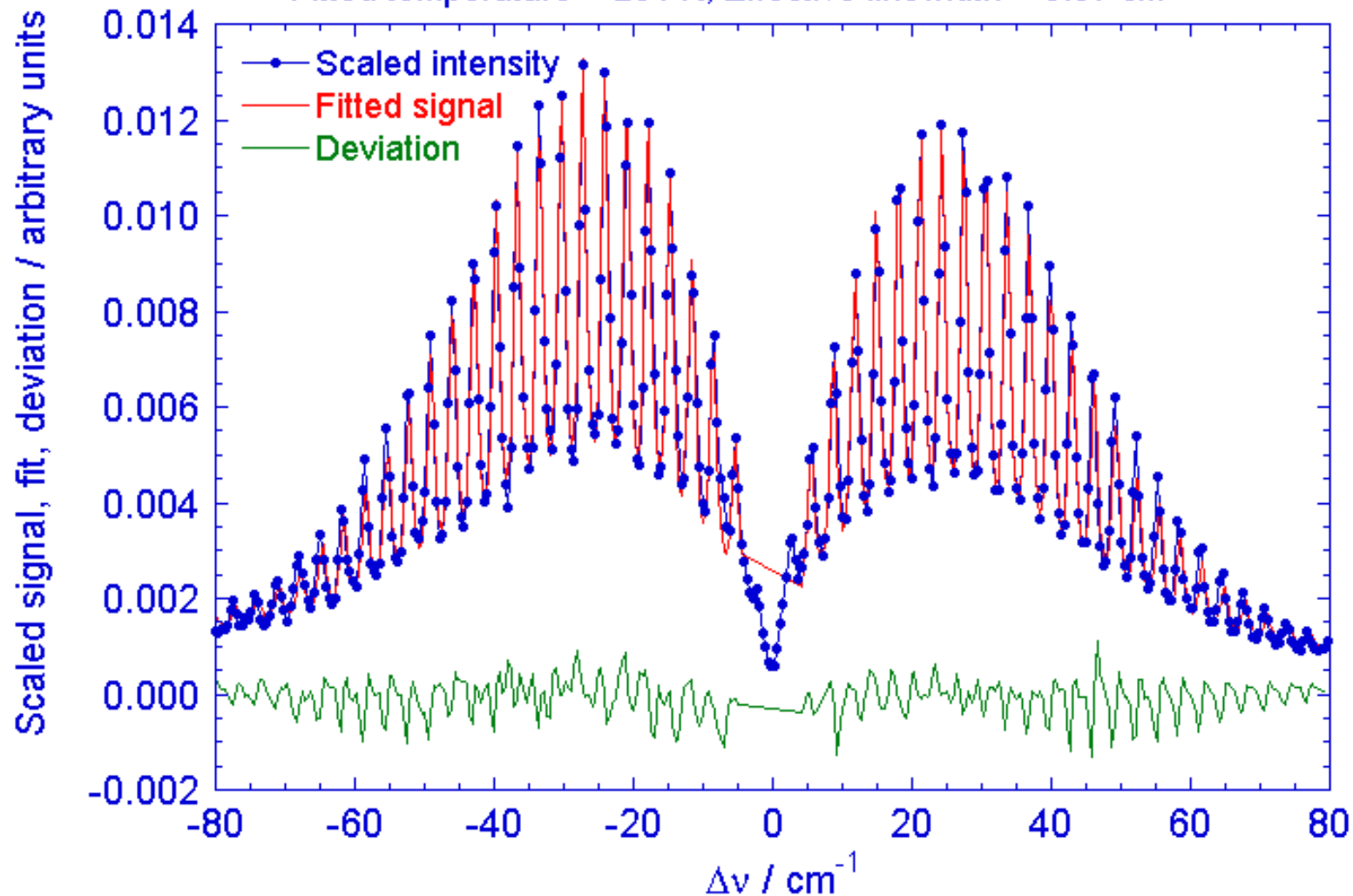
# Raman spectrum of N<sub>2</sub>



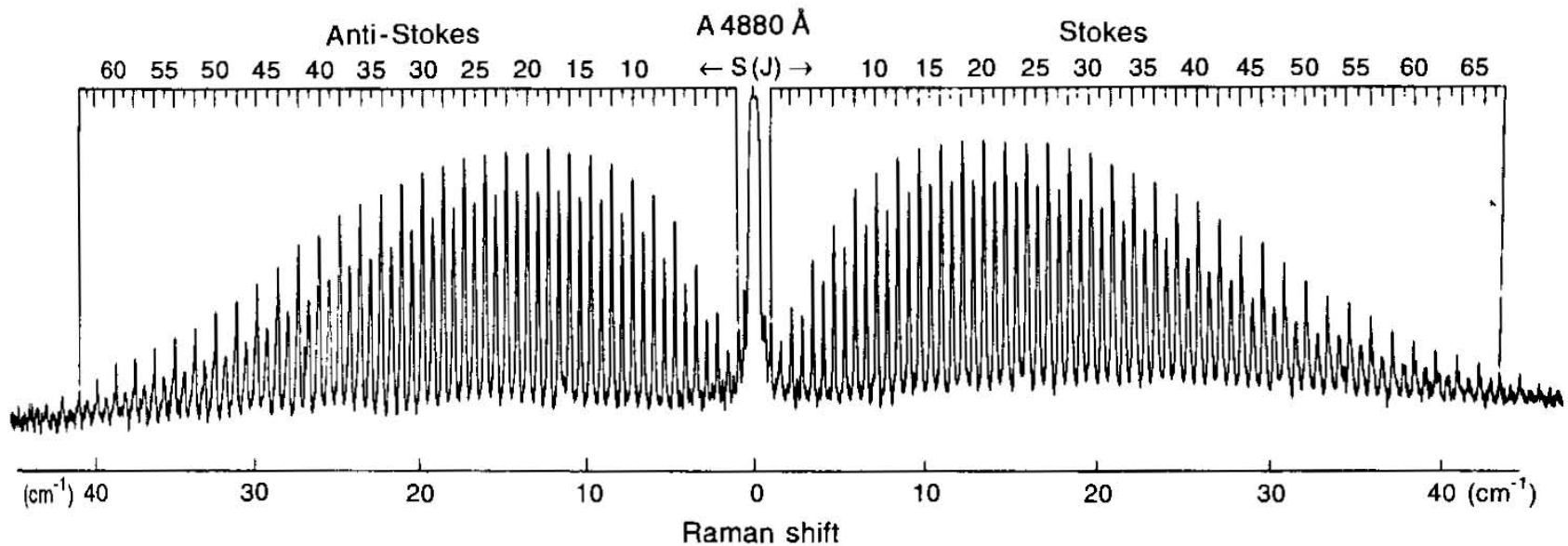
# Raman spectrum

Comparison of cell data with fitted  $\text{CO}_2$  Raman spectrum

Fitted temperature = 281 K, Effective linewidth =  $0.67 \text{ cm}^{-1}$



# Rotational Raman Spectroscopy: $C_2N_2$

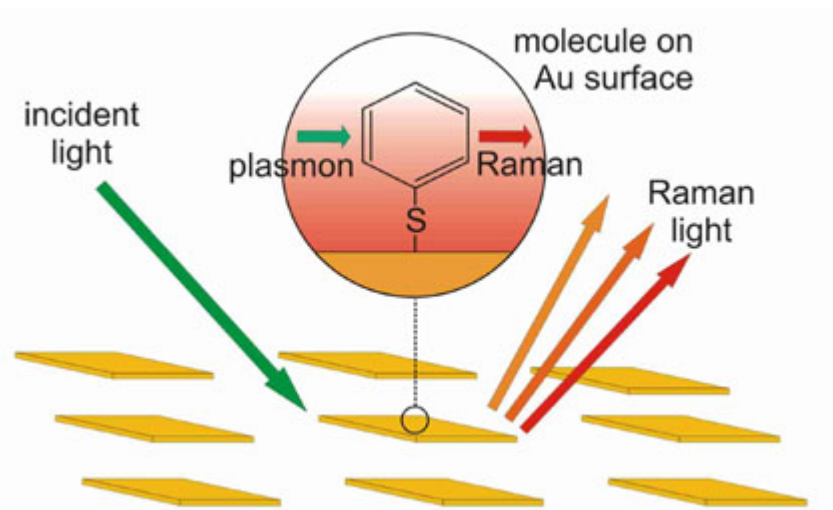


**Fig.8.3.** Rotational Raman spectrum of  $C_2N_2$  excited with the 488 nm line of the argon laser in the experimental setup of Fig.8.2 and recorded on a photographic plate with 10 min exposure time [8.20]

The general disadvantage of the Raman spectroscopy is very small scattering cross section which is about  $\sigma_{sc} \sim 10^{-30} cm^2$ . Therefore, the sensitivity of the method is not very high and the typical experimental problem is detection of a weak signal in the presence of an intense background radiation.

# Surface Enhanced Raman Scattering (SERS)

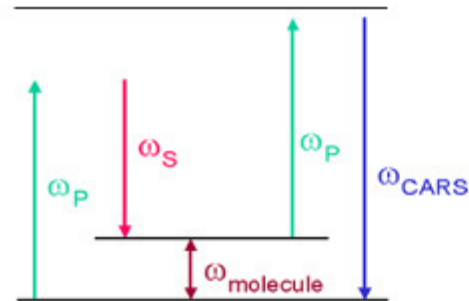
SERS is a surface sensitive technique that results in the enhancement of Raman scattering by molecules adsorbed on rough metal surfaces. Improvement of the detection limits by a factor of  $10^{12} - 10^{14}$ .



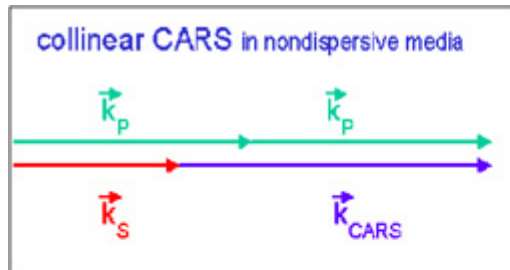
The excitation laser is selected to be in resonance with the surface absorption band, or surface plasmon associated with the metal surface. The analyte that adsorbs in the interaction region is perturbed, leading to enhanced spectral features. Since SERS is a direct measure of the analyte's bonding structure, unique spectral signatures are collected and false positives are minimized. SERS techniques have permitted trace level detection and identification of pollutants such as cyanide and pesticides in water supplies.

# CARS: Coherent Antistoke Raman Scattering

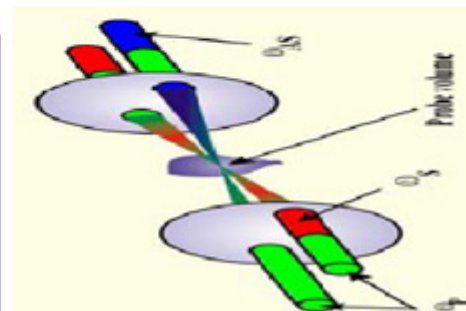
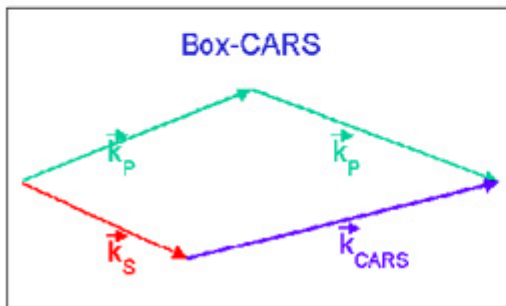
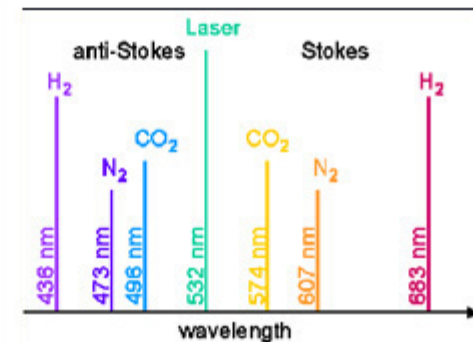
A (coherent non linear 4 wave mixing) diagnostic technique used to determine temperature and concentration in combustion processes.



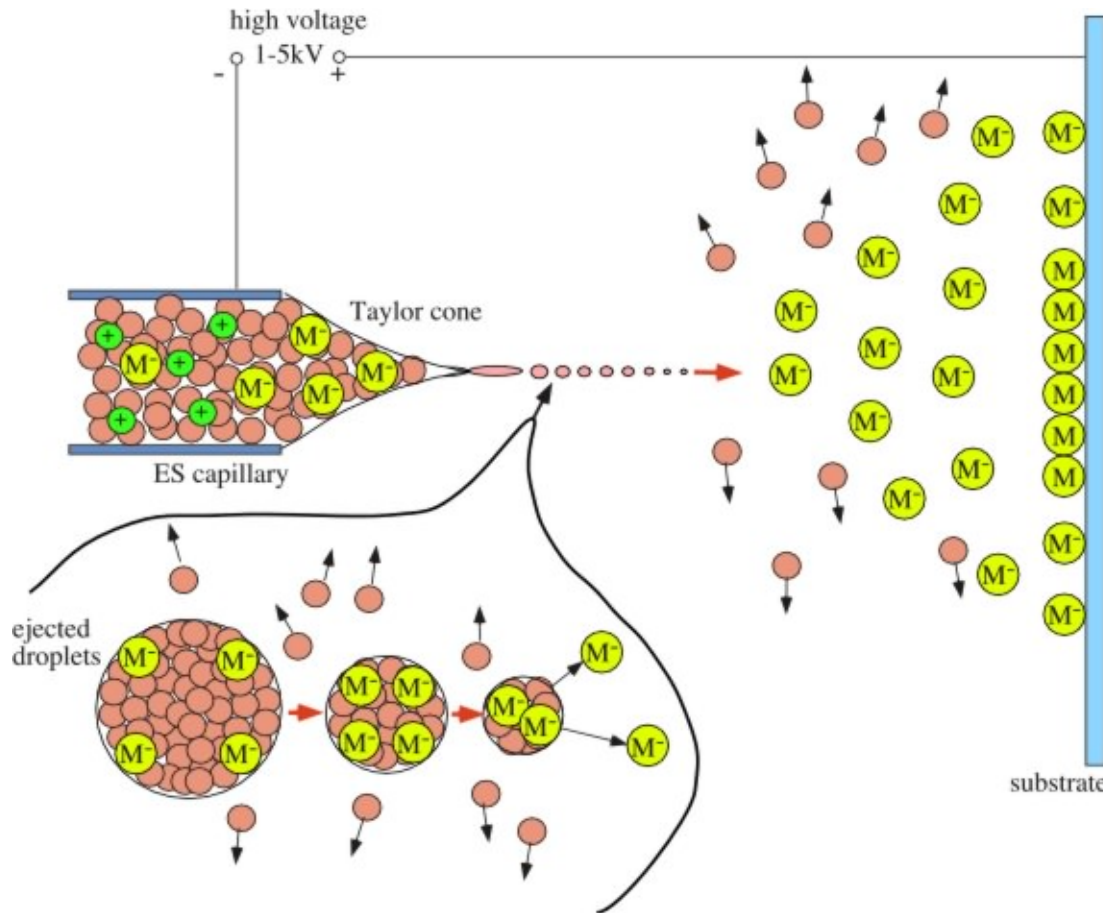
$\omega_P$ : **pump laser frequency**  
 $\omega_S$ : **stokes**  
 $\omega_{CARS}$ : **raman frequency of a molecular transition**



$$\vec{k}_P + \vec{k}_P = \vec{k}_S + \vec{k}_{CARS}$$



# Electrospray

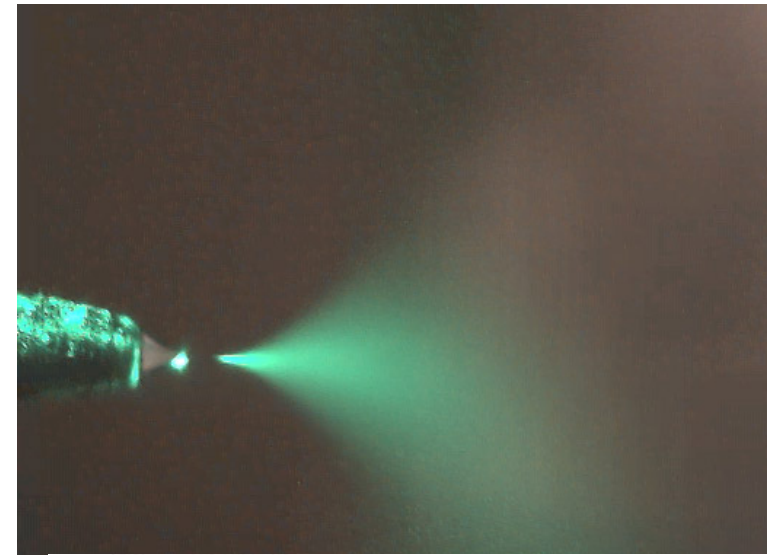


a) strong electric field extracts droplets from Taylor cone containing solute ions ( $M^+$ ); most counter ions ( $M^-$ ) remain in capillary

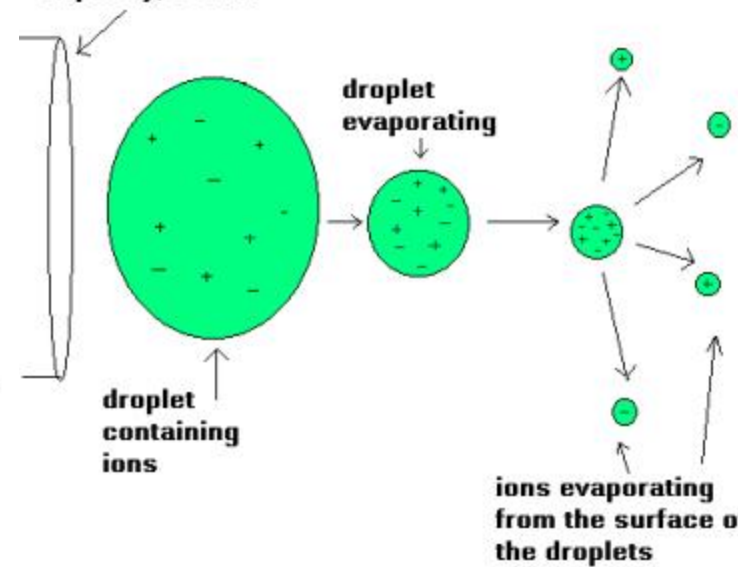
b) Solvent evaporates, droplets shrink, charge density increases

c) solute ions are ejected from the shrinking droplets; Space charge causes a plume

d) solute molecules form thin film on substrate



capillary, 3-4 kV



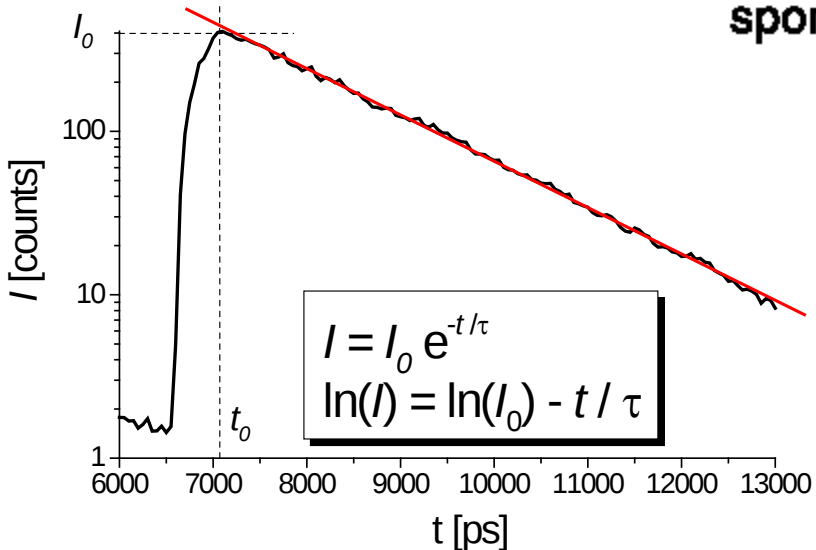
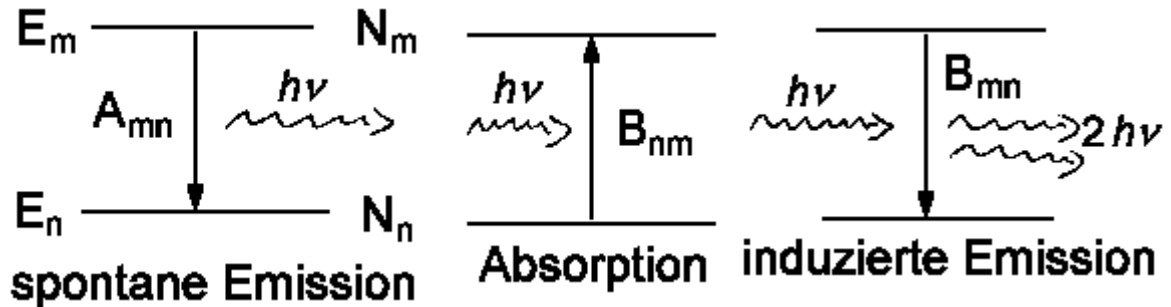
# Heterodyne detection

Heterodyne detection is a method of detecting radiation by non-linear mixing with radiation of a reference frequency. It is commonly used in telecommunications and astronomy for detecting and analysing signals.

So weit mit  
zustandsaufgelösten  
Messungen.

Jetzt:  
Die Geschwindigkeit

# Zusammenhang zwischen $R_{mn}$ , Emission $A_{mn}$ , Lebensdauer $\tau$ und induzierter Absorption $B_{mn}$



$$A_{mn}/B_{mn} = 8\pi h\nu^3/c^3$$

$$1/\tau = A_{mn} = \frac{8\pi^2 e^2}{3 h \epsilon_0 c^3} \cdot \nu_{mn}^3 |R_{mn}|^2$$

Zusammenhang zwischen  $R_{mn}$ , integriertem Absorptionsquerschnitt  $\sigma_0$ , induzierter Absorption  $B_{mn}$  und Oszillatorstärke  $f_{mn}$

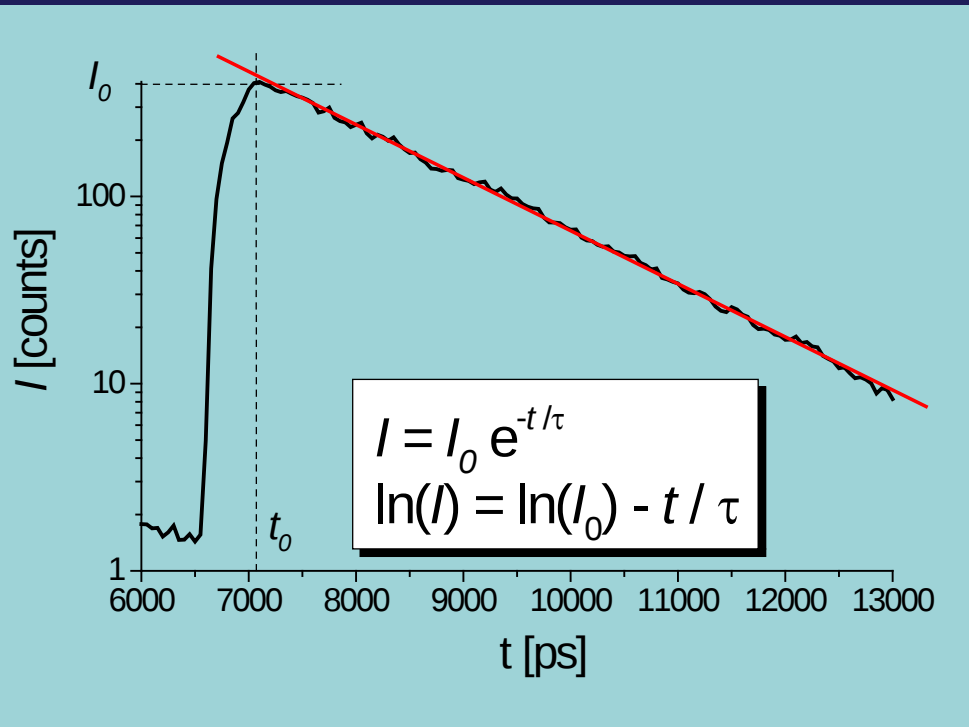
$$|R_{mn}|^2 = \frac{3 \epsilon_0 \hbar c}{\pi e^2 \nu} \cdot \sigma_o = \frac{6 \epsilon_0 \hbar^2}{e^2} \cdot B_{mn} = \frac{3 \hbar}{4 \pi \nu m_e} \cdot f_{mn}$$

$$\sigma_o = B_{mn} \cdot \frac{h \nu}{c} = \frac{\pi e^2 \nu}{3 \epsilon_0 \hbar c} \cdot |R_{mn}|^2 = \frac{e^2}{4 \epsilon_0 c m_e} \cdot f_{mn} \quad \begin{matrix} I_{trans} = I_0 \cdot e^{-\sigma N l} \\ \sigma_o = \int \sigma d\nu \end{matrix}$$

$$B_{mn} = \frac{c}{h \nu} \cdot \sigma_o = \frac{e^2}{6 \epsilon_0 \hbar^2} \cdot |R_{mn}|^2 = \frac{e^2}{4 \epsilon_0 h \nu m_e} \cdot f_{mn}$$

$$f_{mn} = \frac{4 \epsilon_0 c m_e}{e^2} \cdot \sigma_o = \frac{4 \epsilon_0 h \nu m_e}{e^2} \cdot B_{mn} = \frac{4 \pi \nu m_e}{3 \hbar} \cdot |R_{mn}|^2$$

# Fouriertransformation Zeit - Frequenz



Die Fouriertransformierte eines exponentiellen Zerfalls ist eine Lorentzkurve (s. nachfolgende Seite):

$$F(e^{-t/\tau}) \sim \frac{1}{(\nu - \nu_0)^2 + (\Delta\nu/2)^2}$$

Die natürliche Linienbreite ist daher mit der Lebensdauer verknüpft:

$$\Delta\nu = 1/2\pi\tau$$

Die Linienform wird durch eine Lorentzkurve bestimmt.

# Ein exponentieller Zerfall führt zur Lorentzkurve

Man beobachtet entsprechend eine exponentielle Abnahme der Strahlungsintensität:

$$I = I_0 e^{-t/\tau}$$

Da die Strahlungsintensität proportional zum Quadrat der Amplitude des elektrischen Feldes ist, gilt:

$$A(t) = A_0 e^{-t/2\tau} e^{i\omega_0 t}$$

Dabei ist  $\omega_0$  die Kreisfrequenz der ungedämpften Schwingung. Vor dem Zeitpunkt  $t=0$  sei kein Feld vorhanden. Man erhält nach einer Fourier-Transformation :

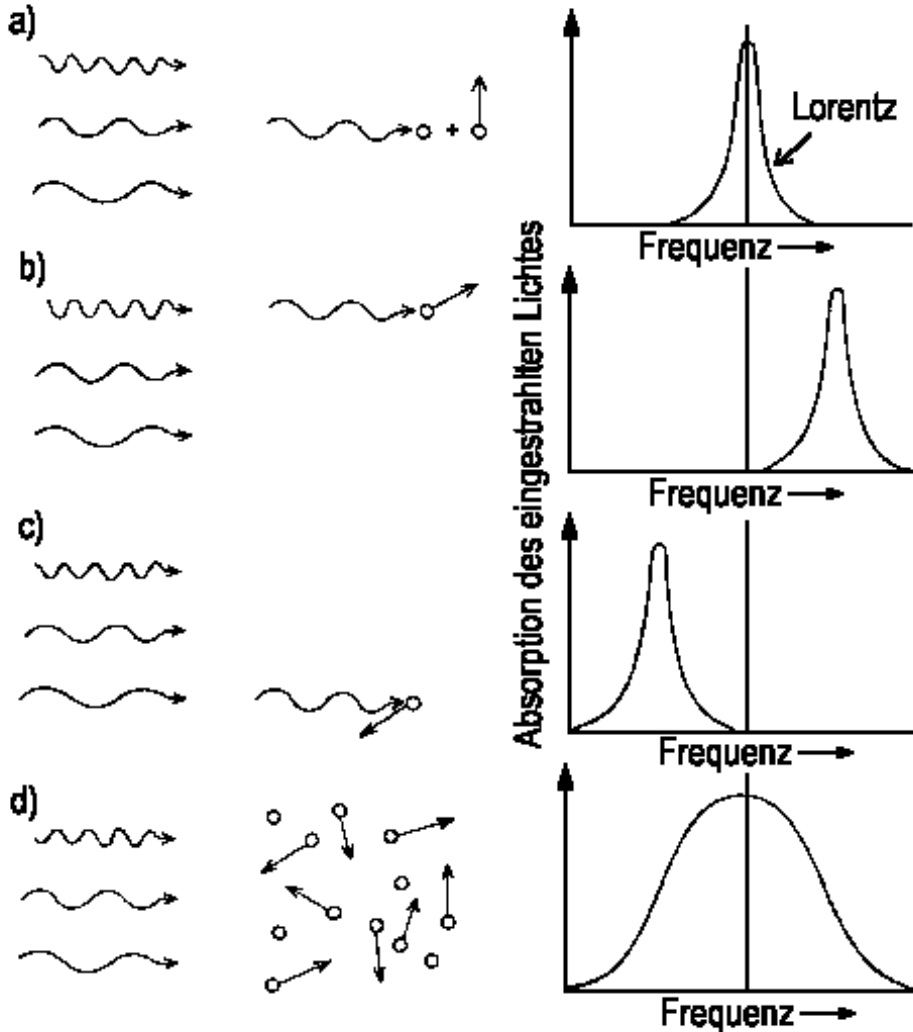
$$\mathbf{A}(\omega) = \int_0^\infty A_0 e^{-t/2\tau} e^{i\omega_0 t} e^{-i\omega t} dt = A_0 / (1/2\tau + i(\omega - \omega_0))$$

$$|\mathbf{A}(\omega)|^2 = A_0^2 / ((\omega - \omega_0)^2 + (1/2\tau)^2)$$

Da die Spektralverteilung der Intensität proportional zu  $|\mathbf{A}(\omega)|^2$  ist, hat die Linie die Form einer Lorentz-Kurve. Unter der Halbwertsbreite einer Spektrallinie versteht man ihre Breite auf der halben Höhe ihres Spitzenwertes. Für ein Lorentz-Profil ist diese:

$$\Delta\omega = 2\pi\Delta\nu = 1/\tau$$

# Lorentz- und Dopplerprofil



## Lorentzprofil

$$L(\nu, \nu_0) = \frac{1}{2\pi} \frac{\Delta\nu_L}{(\nu - \nu_0)^2 + (\Delta\nu_L/2)^2}$$

Aufgrund der Geschwindigkeit  $v$  der Moleküle wird  $\nu_0$  „verschoben“ (Dopplereffekt):

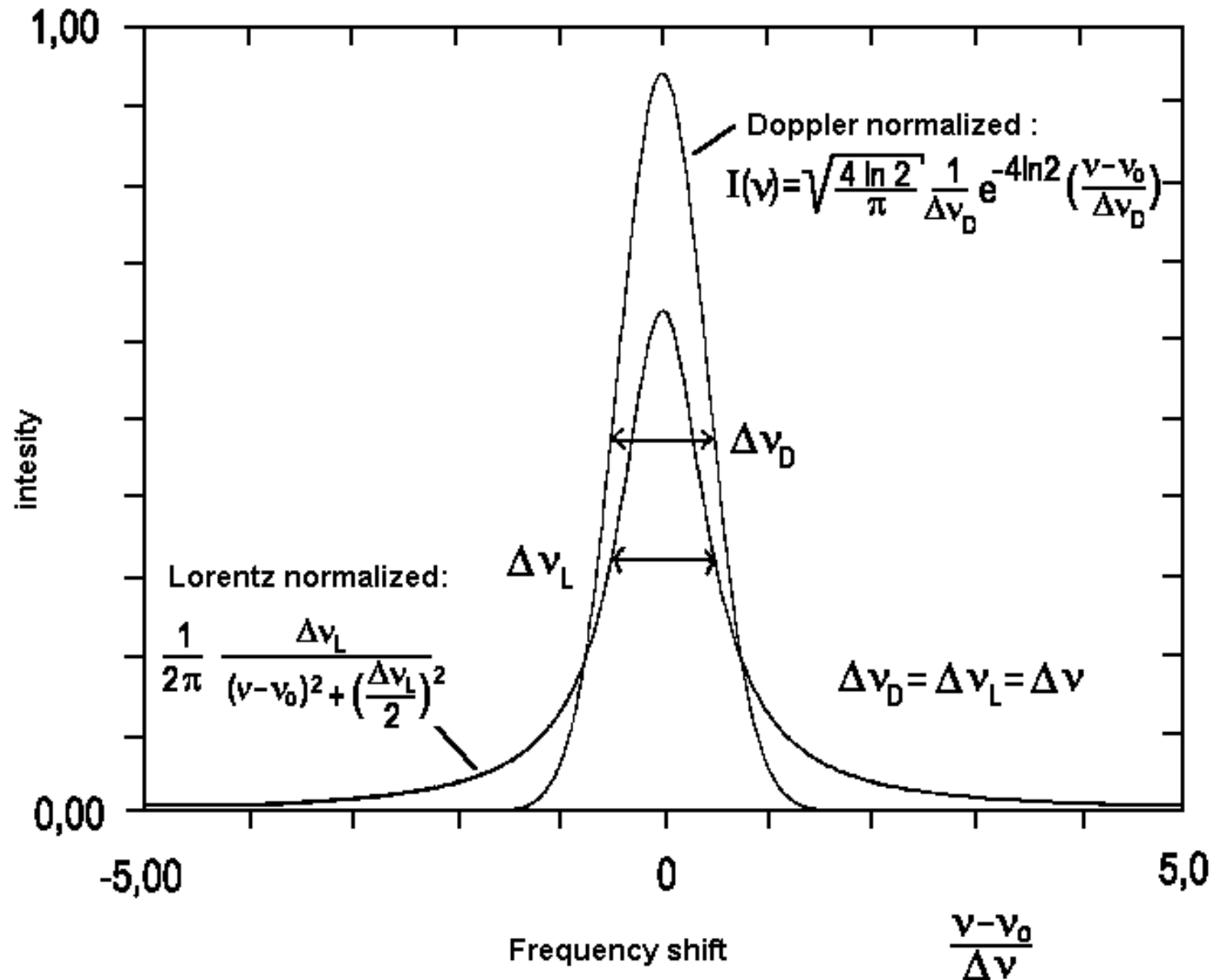
$$\nu = \nu_0(1 - v/c)$$

## Dopplerprofil:

$$I = I_0 \left( \frac{4 \ln 2}{\pi} \right)^{1/2} \cdot \frac{1}{\Delta\nu_D} e^{-4 \ln 2 ((\nu_0 - \nu)/\Delta\nu_D)^2}$$

$$\Delta\nu_D = 2 \nu_0 / c (2 \ln 2 kT / m)^{1/2}$$

# Lorentz and Doppler Line Shapes



## **Aufgabe:** Anregung von OH im UV (308nm)

1. Wie groß ist die natürliche Linienbreite ( $\tau = 700\text{ns}$ )?
2. Wie groß ist die Dopplerbreite bei Raumtemperatur?
3. Wie groß ist die Dopplerverschiebung, wenn OH in einer Reaktion mit einer (festen) Geschwindigkeit von 1000 m/s gebildet wird?
4. Zeichnen Sie ein Lorentz- und ein Dopplerprofil unter der Annahme gleicher Breite und gleicher Höhe.

